

# Introduction

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# Practical Issues

- Office hours are available by appointment
- See course website for most current information:  
<https://sites.google.com/site/muyimolin/teaching/rbe550>  
(Link to this site is on my homepage)
- Course capacity = 35
- For those not yet enrolled, keep coming to class to see if spots open up

# What you can expect to get from this course

- An understanding of modern motion planning methods
- Programming experience
- Hands-on experience working with motion planning
- \*\*\* Paper-reading, presentation, and research skills \*\*\*

# Prerequisites

- Undergraduate Linear Algebra
- Experience with 3D geometry
- Significant programming experience
  - We will use python and C++ in this course
  - You don't need to be an expert but I expect you to pick it up

# Python Example

```
#get the second TSR's offset from the handle to the hand
Tw1_e = linalg.inv(T0_w0*Tw0_e)*T0_RH1

#define bounds to allow rotation of the hand about z axis of the handle from -pi
Bw1 = mat([0, 0, 0, 0, 0, 0, 0, 0, -pi/2, 0])

#serialize the TSRs
TSRstring1 = SerializeTSR(0, 'NULL', T0_w0, Tw0_e, Bw0)
TSRstring2 = SerializeTSR(0, 'NULL', mat(eye(4)), Tw1_e, Bw1) #note the T0_w value k
TSRChainString = SerializeTSRChain(0,0,1,2,TSRstring1 + ' ' + TSRstring2, 'kitchen')

#set the desired amount to open the door
door_rot = pi/1.5
#set the desired amount to rotate the hand about the handle at the goal
handle_rot = -pi/2.1

#keep track of how many DOF of the mimic body are being mimiced
numTSRChainMimicDOF = 1;

#get goal transform
Tdoor_rot = MakeTransform(rodrigues([0, 0, door_rot]),mat([0, 0, 0]).T)
Thandle_rot = MakeTransform(rodrigues([0, 0, handle_rot]),mat([0, 0, 0]).T)
T0_doornew = T0_w0*Tdoor_rot;
T0_RH2 = T0_doornew*Tw0_e*Thandle_rot*linalg.inv(T0_doornew*Tw0_e)* T0_doornew*linalg

goalik = str2num(probs_cbirrt.SendCommand('DoGeneralIK exec nummanips 1 maniptm 0 %s
robot.SetActiveDOFValues(goalik)

#set robot to starting configuration
```

# C++ example

```
bool bGotSolution = false;
for(int i = 0; i < qGuesses.size(); i++)
{
    _planner->ClearTSRChainValues();
    // if a guess is valid, this will confirm it and return quickly, if not, it will
    if(ConstrainedNewConfig(qGuesses[i], q_near, _planner->vTSRChainValues_temp, false)
    {

        RrtNode * pikNode = new RrtNode(_planner->GetNumDOF(), ptree->GetFromGoal());
        pikNode->SetConfig(&qGuesses[i][0]);
        pikNode->SetTSRChainValues(_planner->vTSRChainValues_temp);

        ptree->AddNode(*pikNode); //this will automatically increment the size
        pikNode->Print();
        delete pikNode;
        //return true;
        bGotSolution = true;
    }
}
if(bGotSolution)
    RAVELOG_INFO("Constrained IK solution(s) found!\n");
else
    RAVELOG_INFO("No Constrained IK solution found\n");

return bGotSolution;
}

bool CBirrtPlanner::_CheckCollision(std::vector<dReal>& pConfig)
{
    collisioncheckcalls++;
#ifdef RECORD_TIMES
    double starttime = timeGetThreadTime();
#endif
}
```

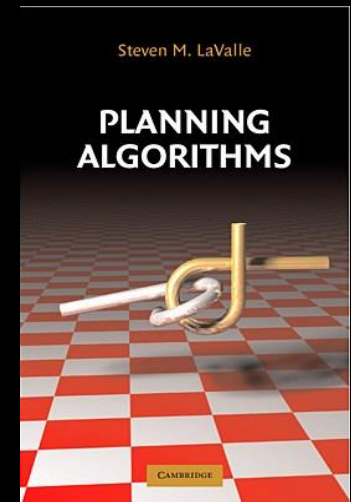
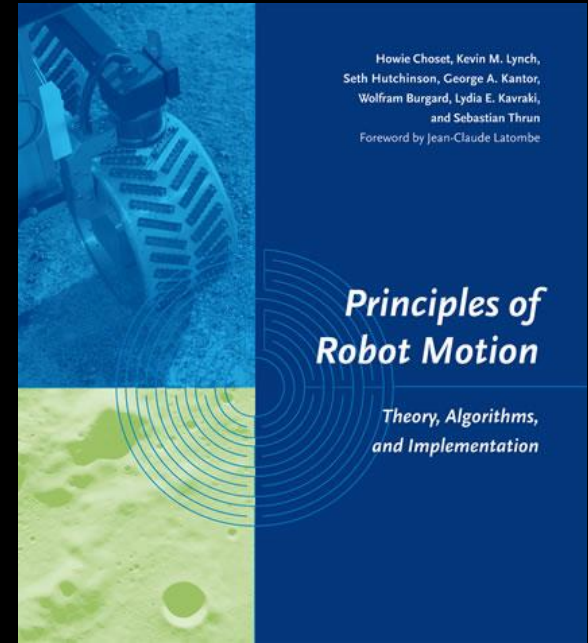
# Math expectations

- Linear algebra proficiency is a **MUST**
  - Matrix operations
  - Dot products, cross products, etc.
  - A review of linear algebra:
    - <http://cs229.stanford.edu/section/cs229-linalg.pdf>
- Be able to read math notation
  - Some examples from the textbook:

$$X_{obs} = \left( \bigcup_{t=1}^m X_{obs}^t \right) \cup \left( \bigcup_{tj, t \neq j} X_{obs}^{tj} \right)$$
$$X_{obs}^{tj} = \{(s_1, \dots, s_m) \in X \mid \mathcal{A}^t(\tau_t(s_t)) \cap \mathcal{A}^j(\tau_j(s_j)) \neq \emptyset\}$$
$$\mathcal{C}_{obs}^p = \{(q^a, q^p) \in \mathcal{C} \mid \text{int}(\mathcal{P}(q^p)) \cap \mathcal{O} \neq \emptyset\}$$

# Readings

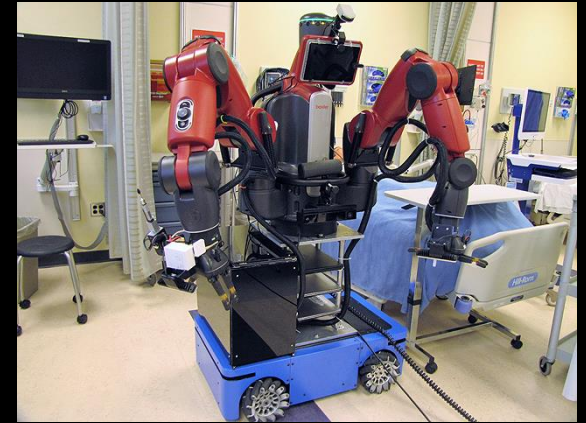
- Textbook
  - Principles of Robot Motion (by Howie Choset)
  - Referred as “**Principles**” in this course
  - Available online via library
- Week 1-7 ~ Textbook
- Week 8-14 ~ Research papers
- Students will present and discuss research papers
- Other reference:
  - Planning algorithms by S. M. LaValle
  - Available online





# Syllabus

- No exams!
- Three homeworks
  - Individual (no groups)
  - Learn to implement algorithms
  - Use openrave open-source motion planning framework
- Final Project
  - Human/robot motion planning
  - Individual project encouraged (tailor to your research), teams of 2 or 3 also allowed



# Piazza

- <https://piazza.com/wpi/spring2017/rbe550/home>
- **Piazza.com** for all class communication (question/answer about homeworks, paper discussion, etc.)

The screenshot shows the Piazza.com interface for a course page. The top navigation bar includes the Piazza logo, course information (RBE 595/C.S. 525), and tabs for Q & A, Course Page, and Manage Class. The user's name, Dmitry Berenson, is visible in the top right. The main content area is divided into several sections:

- Class at a Glance:** A summary box showing the status of the class. It includes three green checkmarks indicating: no unread posts, no unanswered questions, and no unresolved followups. To the right, statistics are listed: 9 total posts, 11 total contributions, 0 instructors' responses, 0 students' responses, and n/a avg. response time.
- Student Enrollment:** A bar chart showing 9 enrolled students out of 20 estimated.
- Share Your Class:** A section for sharing the class with colleagues, including a demo link: [https://piazza.com/demo\\_login?nid=hbfih3uhiz5gyzauth=25de093](https://piazza.com/demo_login?nid=hbfih3uhiz5gyzauth=25de093).

The left sidebar contains a search bar, a '+ New Post' button, and a list of pinned and recent posts. The bottom of the page shows a footer with 'Average Response Time: N/A', 'Special Mentions: There are no special mentions at this time.', and 'Online Now: 1 | This Week: 1'.

# Grading

- In-Class Participation and Preparation 15%
  - Attending class and asking questions during lecture
  - Participating in paper discussions
  - Participating in discussions on Piazza
- Research Paper Presentations 15%
- Homeworks 20%
- Final Project Proposal 10%
- Final Project Report 25%
- Final Project Presentation 15%

# Schedule

- Latest schedule is on course website:

<https://sites.google.com/site/muyimolin/teaching/rbe550>

	A	B	C	D	E	F	G
1	Date	Topic	Slides		Reading		Assignment
2	1/13/2017	L: Introduction to Motion Planning	<a href="#">link</a>	Principles: CH 1, 5	<a href="#">Graph Review</a>		Sign up for course on Piazza
3	1/18/2017	L: Planning for point robots	<a href="#">link</a>				Enter presentation topic preferences into Piazza
4	1/20/2017	L: Configuration Space	<a href="#">link</a>				<a href="#">Homework 1 Out</a>
5	1/25/2017	L: Discrete Motion Planning	<a href="#">link</a>				
6	1/27/2017	L: Transformations	<a href="#">link</a>				
7	2/1/2017	L: Collision Checking	<a href="#">link</a>	<a href="#">Probability Review</a>			Homework 1 Due
8	2/3/2017	L: Sampling-based Planning 1	<a href="#">link</a>	<a href="#">How to read a paper</a>			<a href="#">Homework 2 Out</a>
9	2/8/2017	L: Sampling-based Planning 2	<a href="#">link</a>	<a href="#">Non-holonomic motion planning guide</a>			
10	2/10/2017	L: Non-holonomic motion planning	<a href="#">link</a>	<a href="#">Paper Presentation Guidelines</a>	<a href="#">Presentation Grading Sheet</a>	<a href="#">Reviewing Guidelines</a>	
11	2/15/2017	Presentation		<a href="#">ANA*</a>	<a href="#">Adaptive Anytime Motion Planning For Robust Robot Navigation In Natural Environments</a>	<a href="#">LEARCH</a>	
12	2/17/2017	Presentation		<a href="#">Adaptive workspace biasing for sampling-based planners</a>	<a href="#">Demonstration-guided motion planning</a>	<a href="#">RRT*</a>	Homework 2 Due
13	2/22/2017						
14	2/24/2017	Presentation		<a href="#">Randomized Kinodynamic Planning</a>	<a href="#">A Sampling-Based Tree Planner for Systems with Complex Dynamics</a>	<a href="#">Simulation-Based LQR-Trees with Input and State Constraints</a>	<a href="#">Homework 3 Out</a>
15	3/1/2017	L: Grasping	<a href="#">link</a>				<a href="#">Submit Project Proposal (recommended)</a>
16	3/3/2017	SPRING BREAK					
17	3/8/2017	SPRING BREAK					
18	3/10/2017	SPRING BREAK					
19	3/15/2017	Presentation		<a href="#">Data Driven Grasp Synthesis using Shape Matching and Task-Based Pruning</a>	<a href="#">Grasping Objects with Holes: A Topological Approach</a>	<a href="#">Probabilistic Collision Checking With Chance Constraints</a>	<a href="#">Project Proposal Due</a>

# Presentations

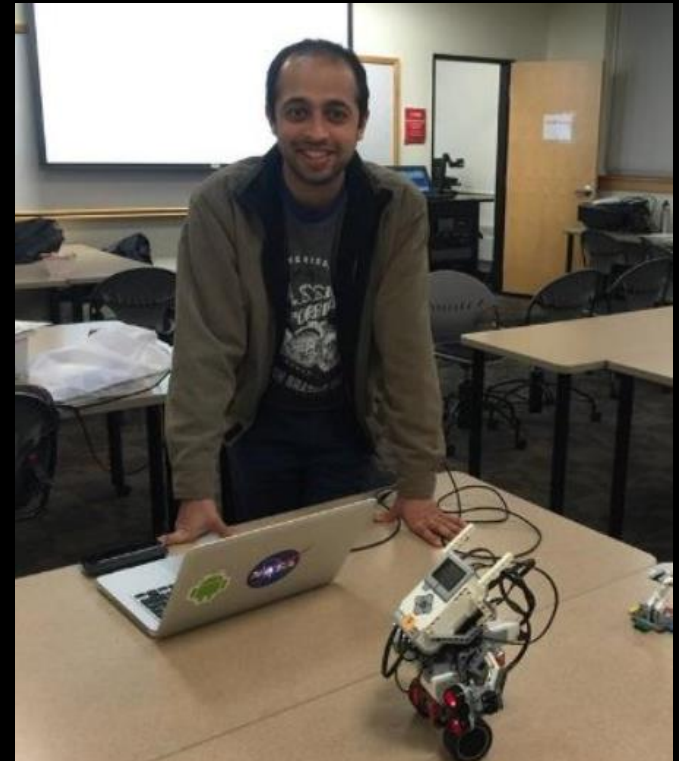
- In-depth understanding of a paper
- Tentatively 15 minutes long + 2 minutes of questions
  - Like a standard conference talk
- Evaluated on
  - Depth of understanding
  - Clarity of presentation
  - Presentation skill (don't run out of time!)

# Final Project

- Schedule meeting with me to discuss project topic and expectation
- Preparation (now ~ **March 1**)
  - Literature survey
  - Acquire necessary skills
  - Work on project proposal -- clear timeline
- Project proposal due **March 15**
- Final project progress report due **April 12**
- Final project presentation + Final report due on **April 28**

# First person to ask for help – TA Aditya Bhat

- Email - [abhat@wpi.edu](mailto:abhat@wpi.edu)
- Office: 85 Prescott 224



# Introduction to Motion Planning

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**Jane Li**

Assistant Professor

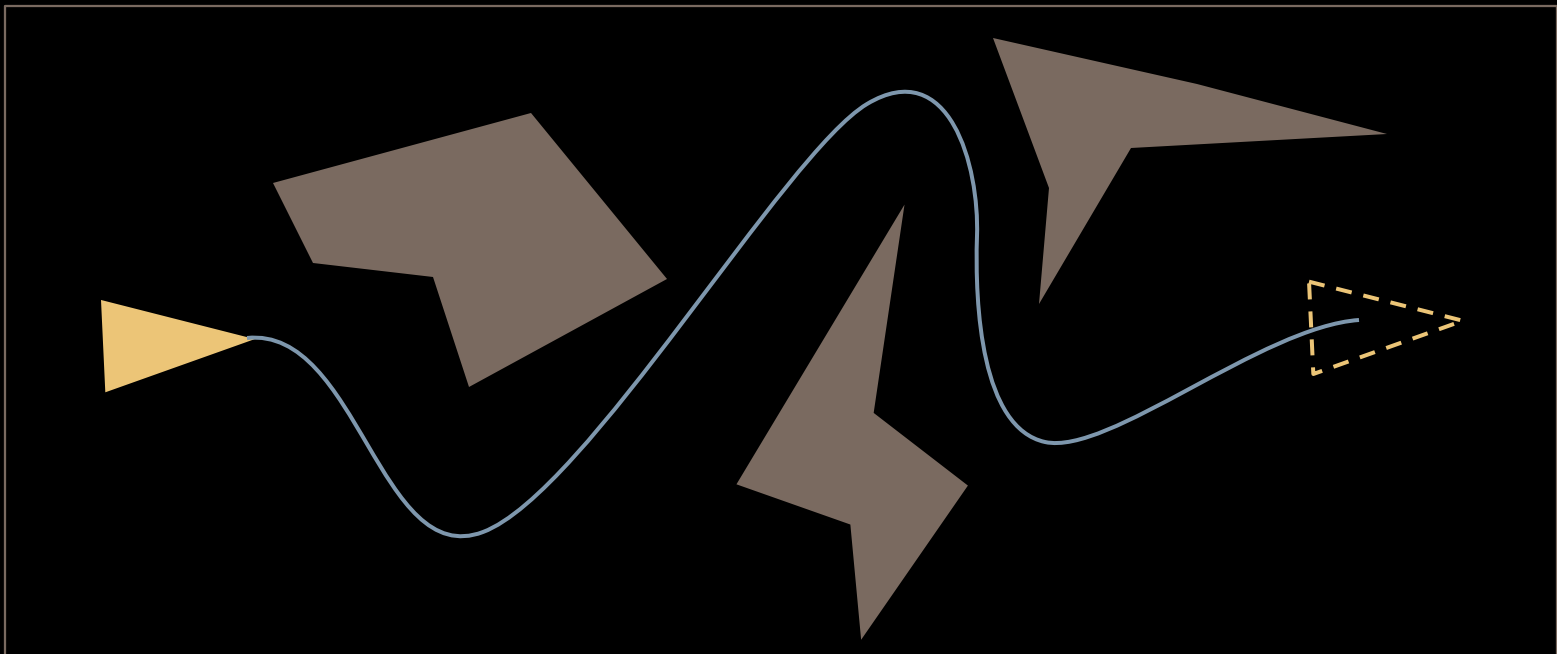
Mechanical Engineering & Robotics Engineering

<http://users.wpi.edu/~zli11>



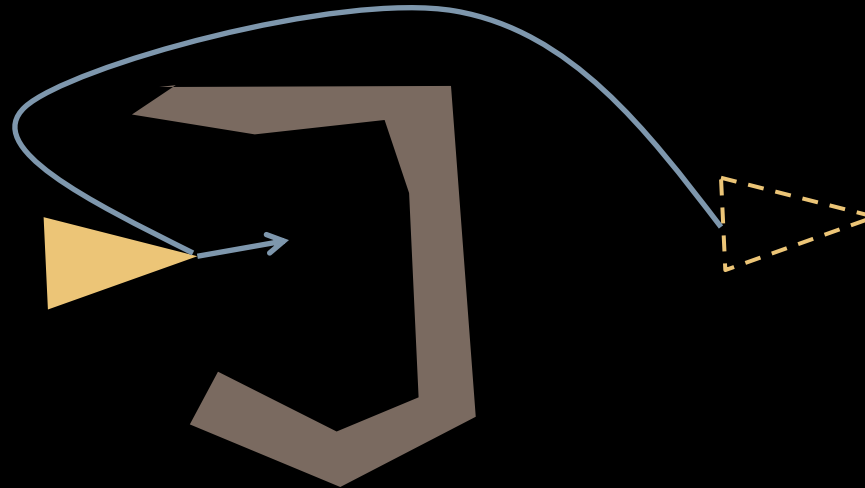
# What is motion planning?

- The automatic generation of motion
  - Path + velocity and acceleration along the path

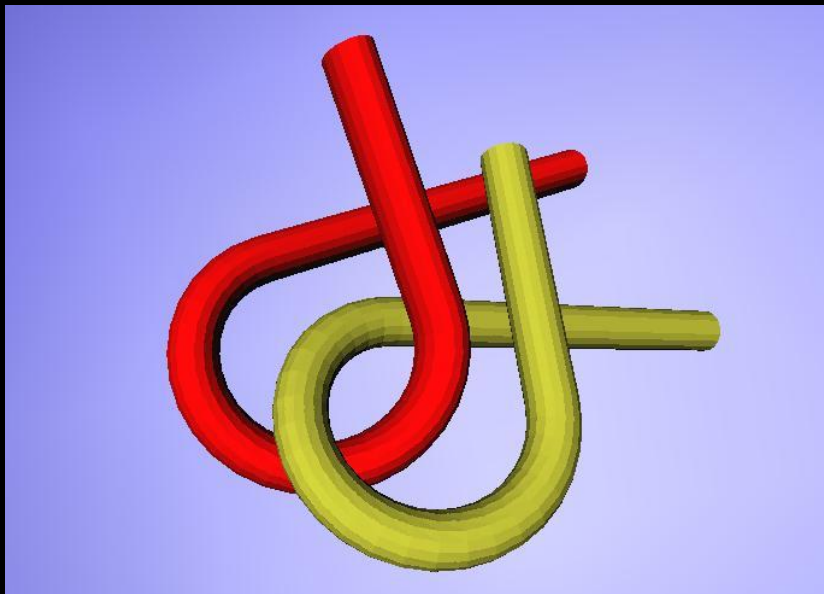


# Why Motion Planning Instead of Obstacle Avoidance?

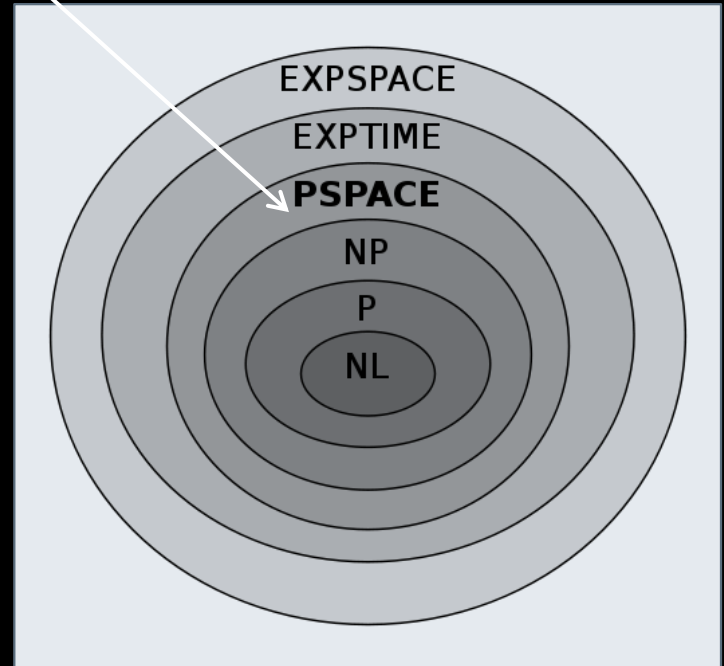
- Path planning
  - low-frequency, time-intensive search method for global finding of a (optimal) path to a goal
- Obstacle avoidance (aka “local navigation”)
  - fast, reactive method with local time and space horizon
- Distinction: Global vs. local reasoning



# Is motion planning hard?



Basic Motion  
Planning Problems

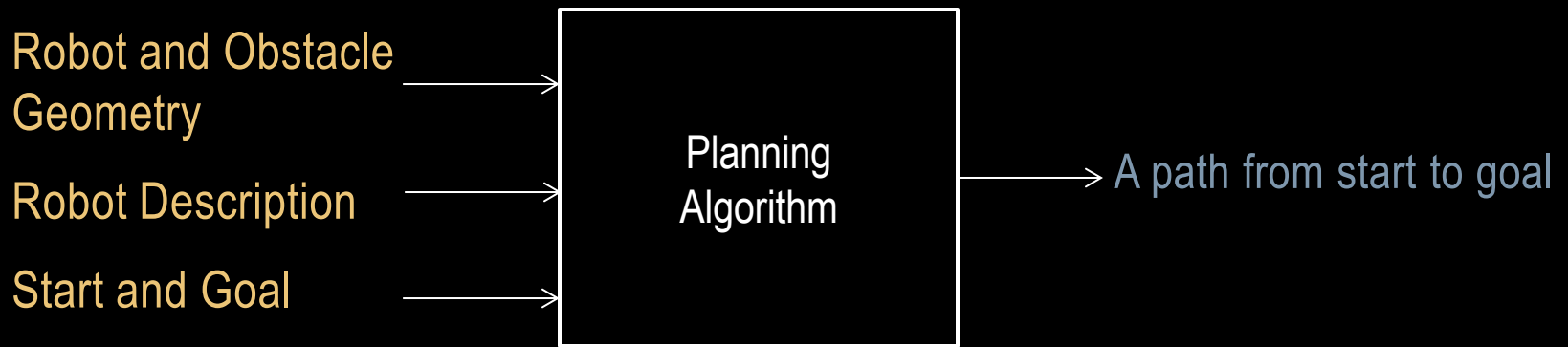


# Related Fields and Contents

- Intersection of three fields
  - **Robotics**
  - Control theory
  - AI
- Topics
  - Planning in **discrete space**
  - Planning in **continuous space**
  - Planning under **uncertainty**
  - Planning under **differential constraints**

# Basic Problem Statement

- Motion planning in robotics
  - Automatically compute a path for an object/robot that does not collide with obstacles.



# Basic Motion Planning Problem

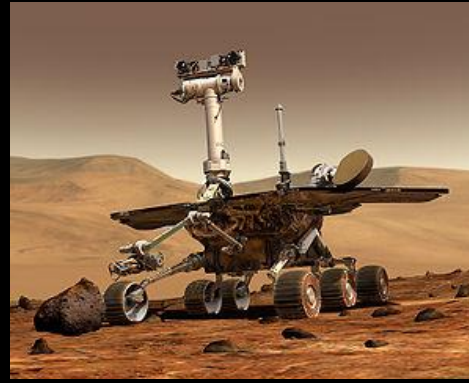
- Examples
  - Piano mover's problem – 3D
  - Sofa mover's problem – 2D
  - Generalized mover's problem
- Key to the problem
  - Make sure not point on the robot hits an obstacle
  - All **kinematic** motion planning

## More than kinematic motion planning ...

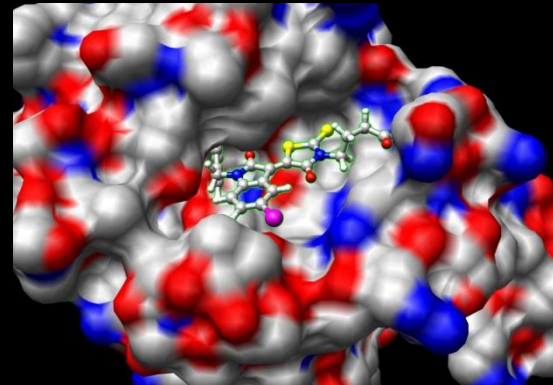
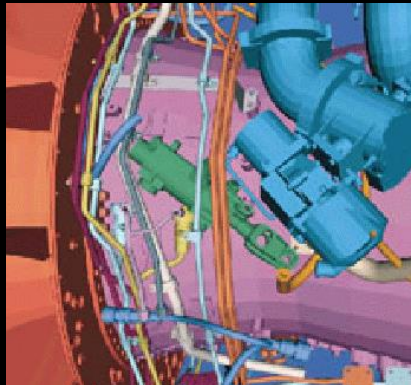
- Trajectory planning (speed & acceleration along the path)
- Nonholonomic constraints (e.g. parallel parking)
- Sensor-based motion planning (deal with uncertainty)
- SLAM (e.g. planetary exploration)
- Coverage path planning (e.g. vacuum robot, demining)
- Hyper-redundant robot (e.g. snake robot for search and rescue)
- Human-like motion (e.g. animated characters)
- Drug design (e.g. protein as linked rigid bodies)

# Applications

- Automatically generate motion



- Automatically validate





# Applications: Mobile Robots



Roomba Create



Mars Rovers



DARPA Urban Challenge



Google Self-Driving Car

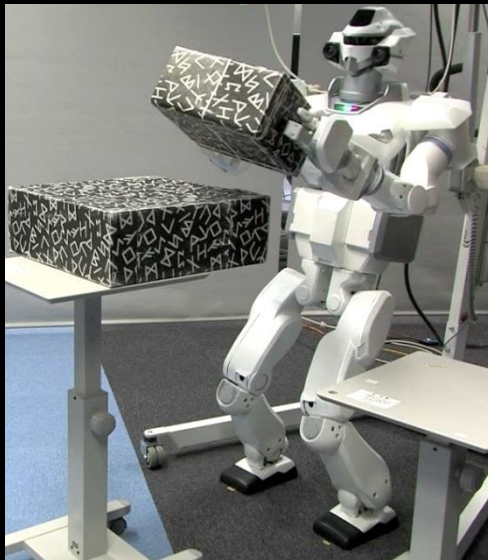
# Applications: Robotic Manipulation



Factory Automation



Personal Robots



Humanoid Robots



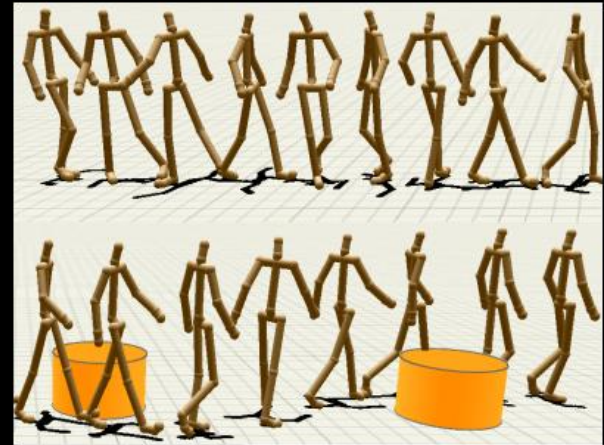
Personal Robots



# Applications: Computer Games/Graphics



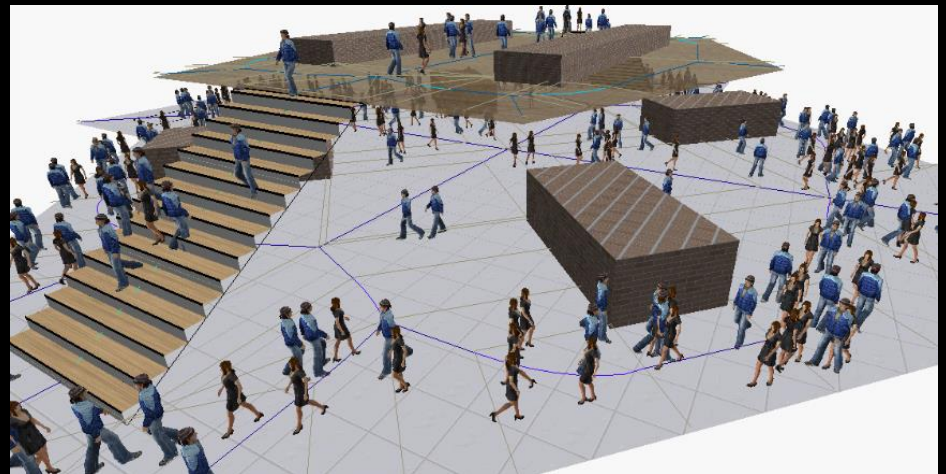
Path Finding in Games



Character Animation

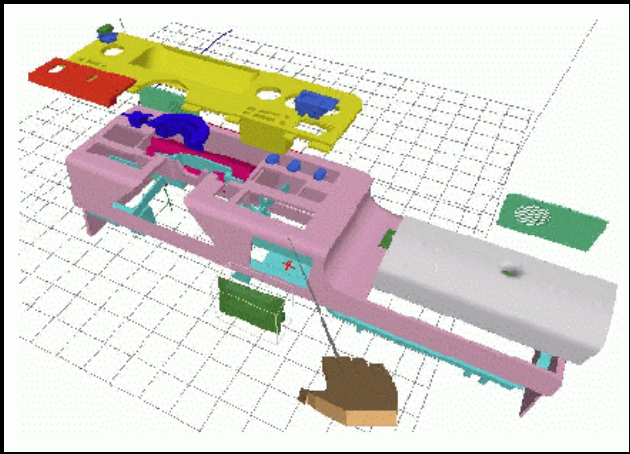
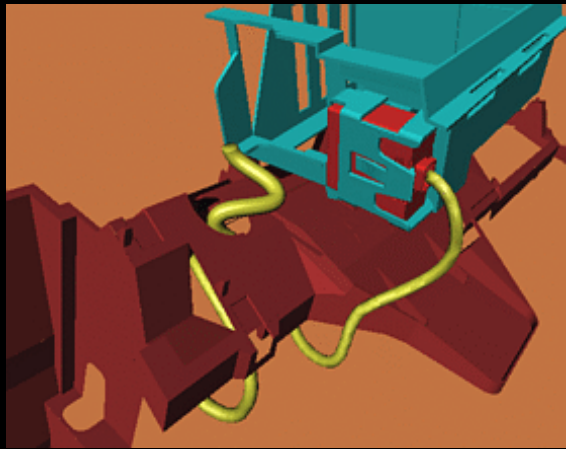
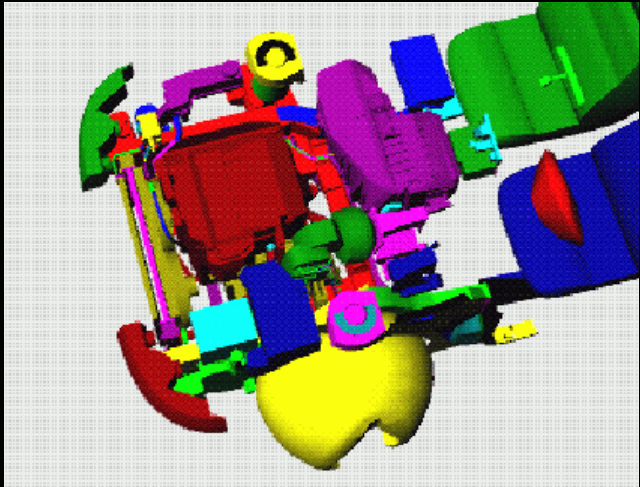
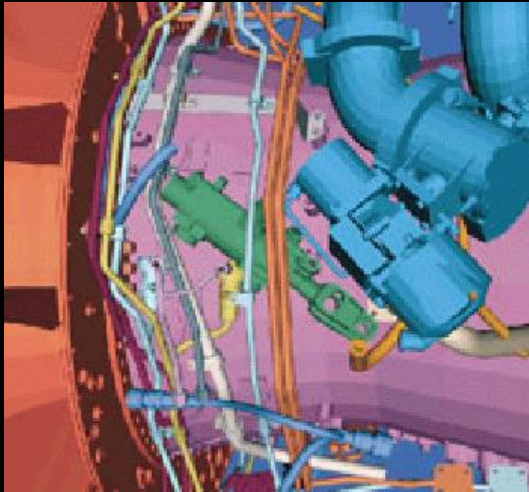


Retargeting Motion Capture



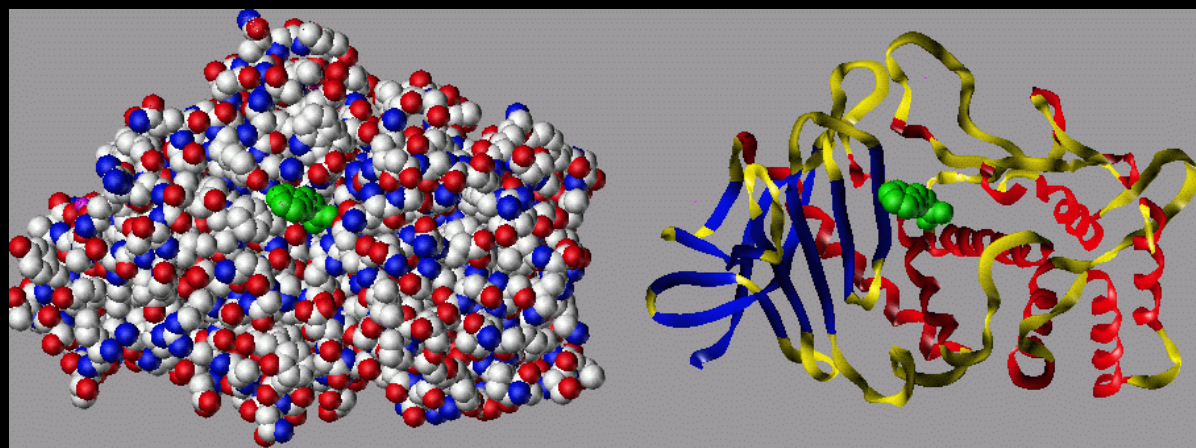
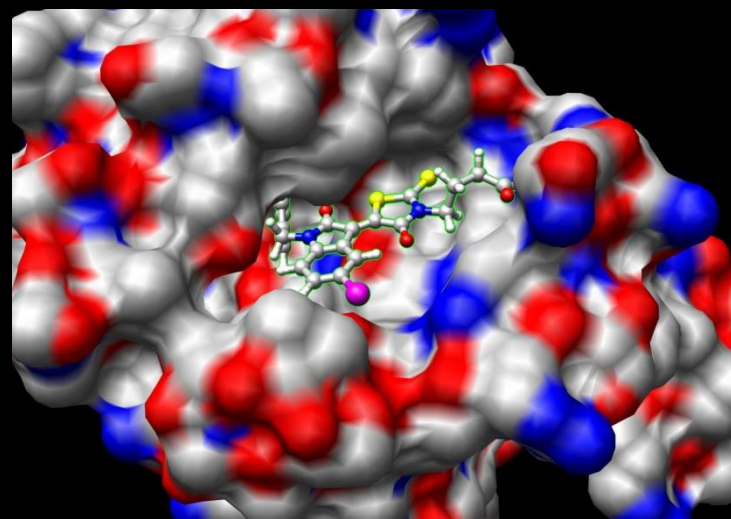
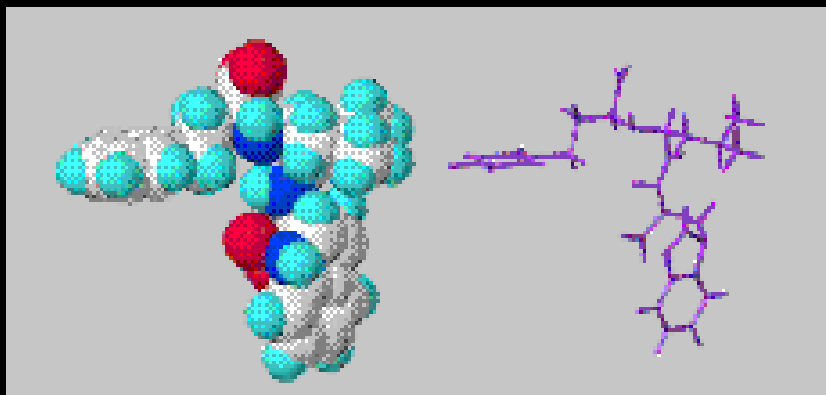
Animation of Crowds

# Applications: Assembly Planning



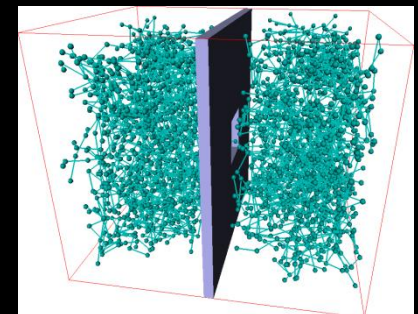
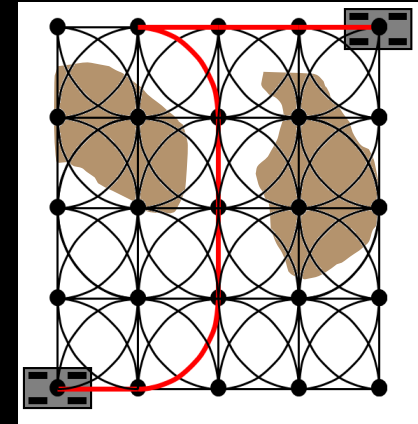
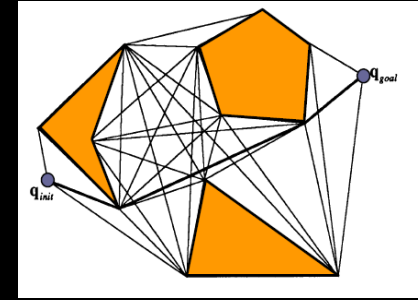


# Applications: Computational Biology



# Approaches

- Exact algorithms
  - Either find a solution or prove none exists
  - Very computationally expensive
  - Unsuitable for high-dimensional spaces
- Discrete Search
  - Divide space into a grid, use  $A^*$  to search
  - Good for vehicle planning
  - Unsuitable for high-dimensional spaces
- Sampling-based Planning
  - Sample the C-space, construct path from samples
  - Good for high-dimensional spaces
  - Weak completeness and optimality guarantees



# What matters?

- Motion planning algorithms are judged on
  - Completeness
  - Optimality
  - Speed (AKA efficiency)
  - Generality
- These vary in importance depending on the application

# What matters: Completeness

- Will the algorithm **solve all solvable** problems?
- Will the algorithm **return no solution** for unsolvable problems?
- What if the algorithm is **probabilistic**?
  
- For what application(s) is completeness **very important**?
- For what application(s) is completeness **not important**?



# What matters: Optimality

- Will the algorithm generate the **shortest** path?
- Will the algorithm generate the **least-cost** path (for an arbitrary cost function)?
- Do we need **optimality** or is **feasibility** enough?
  
- For what application(s) is completeness **very important**?
- For what application(s) is completeness **not important**?

## What matters: Speed (AKA Efficiency)

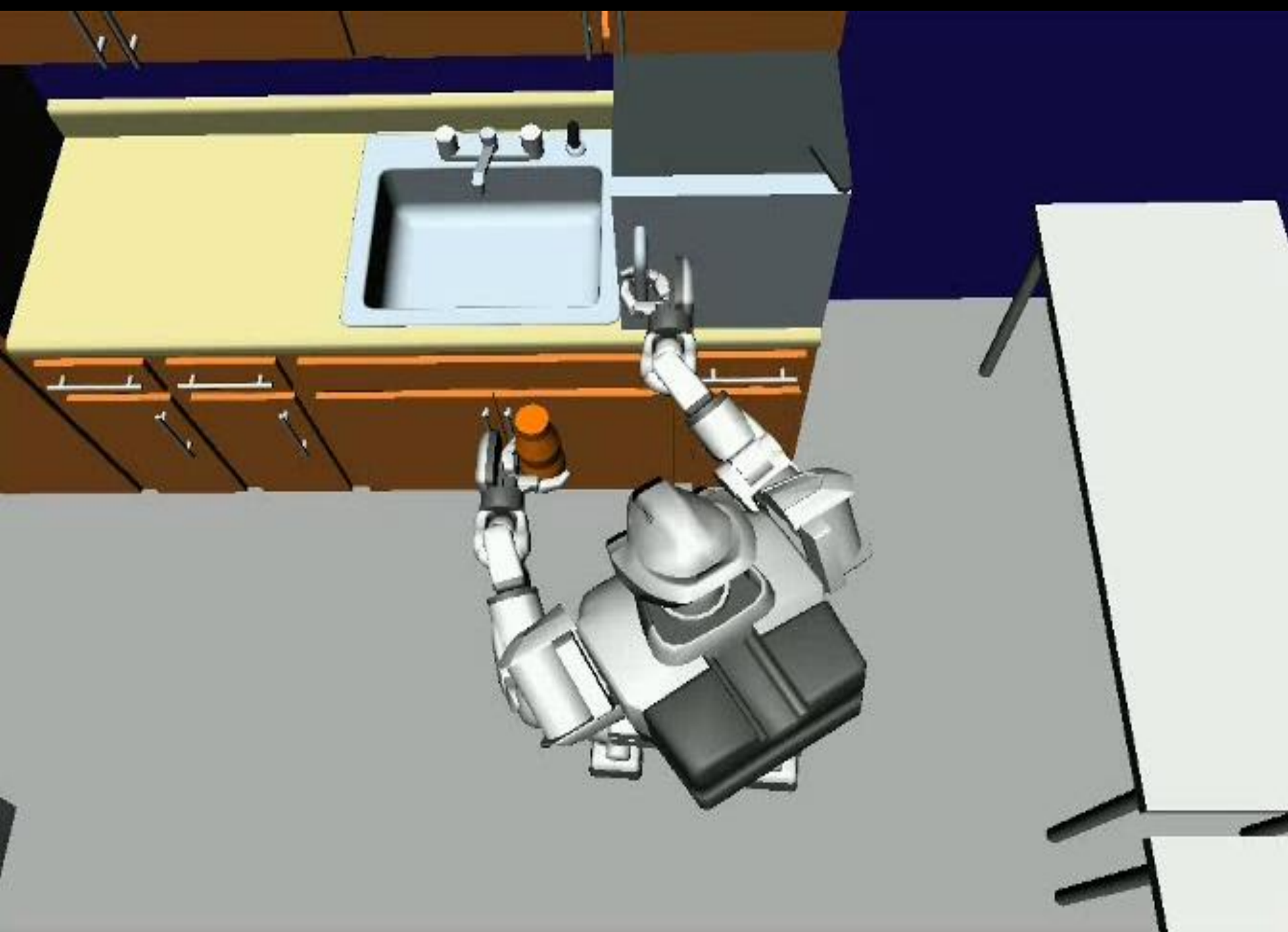
- How long does it take to generate a path for **real-world** problems?
- How does the **run-time scale with dimensionality** of the problem and **complexity of models**?
- Is there a **quality vs. computation** time tradeoff?
  
- For what application(s) is completeness **very important**?
- For what application(s) is completeness **not important**?

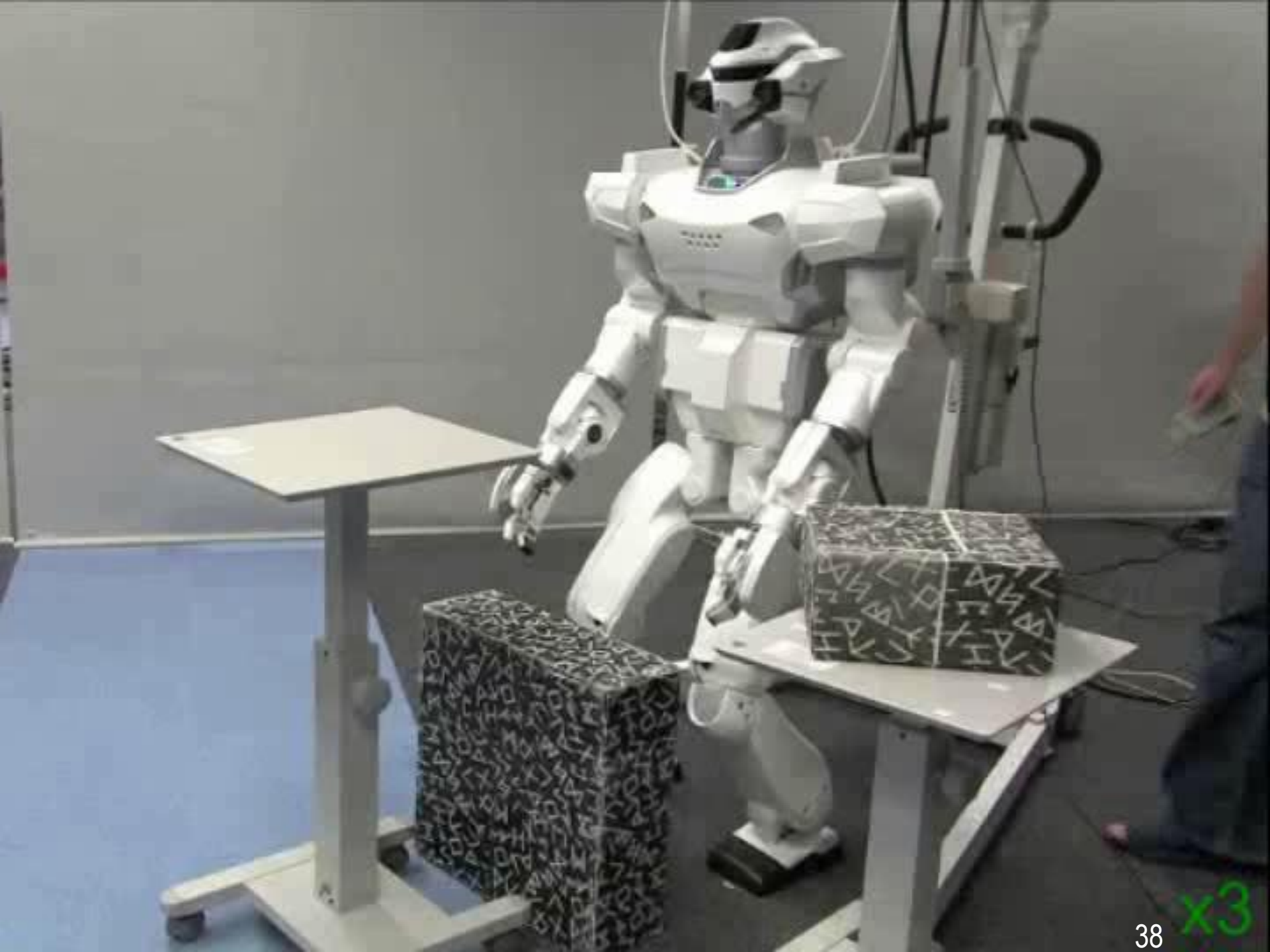
# What matters: Generality

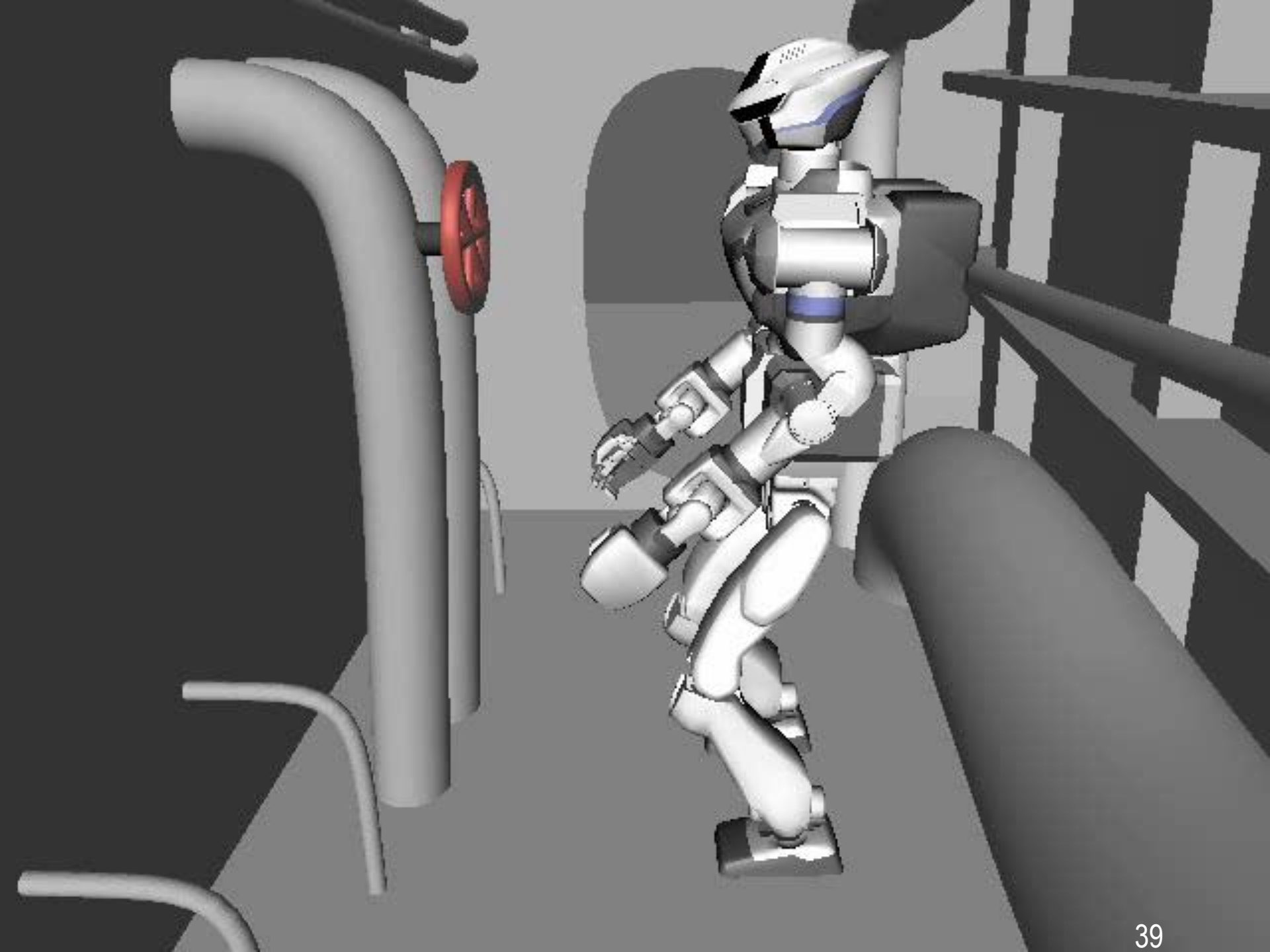
- What types of problems **can** it solve?
- What types of problems **can't** it solve?
  
- For what application(s) is completeness **very important**?
- For what application(s) is completeness **not important**?

$w = 4.98\text{kg}$



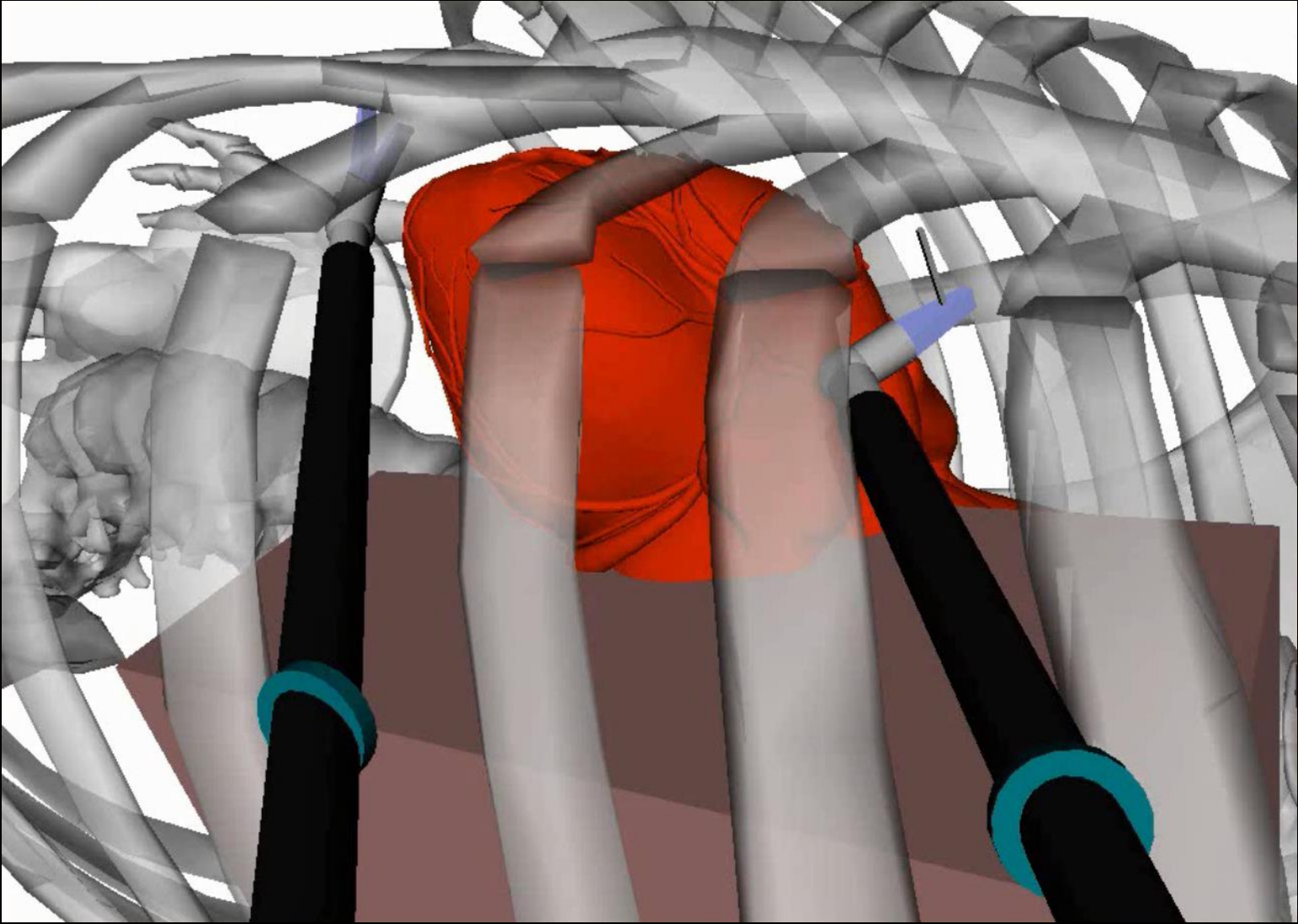






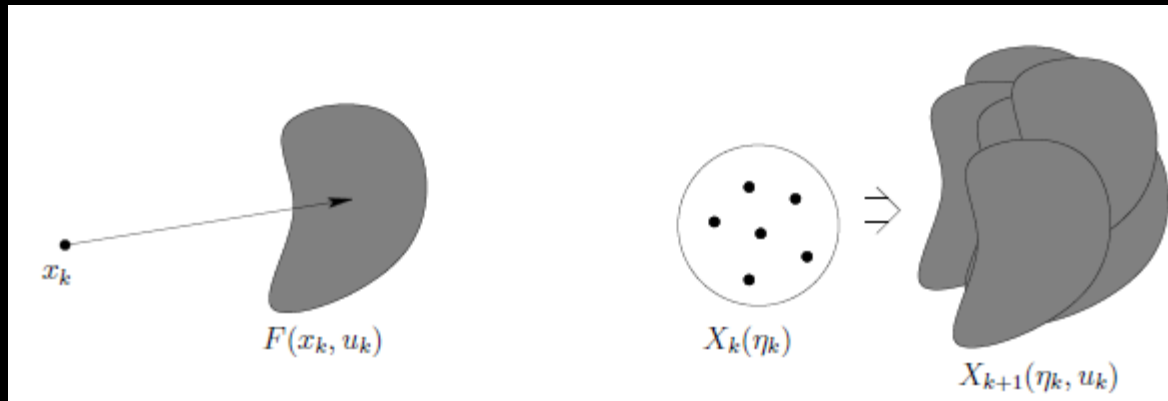
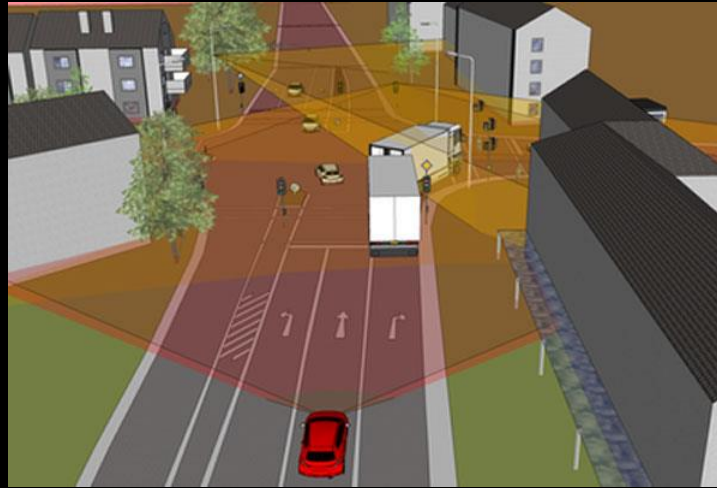


# Robotic Surgery



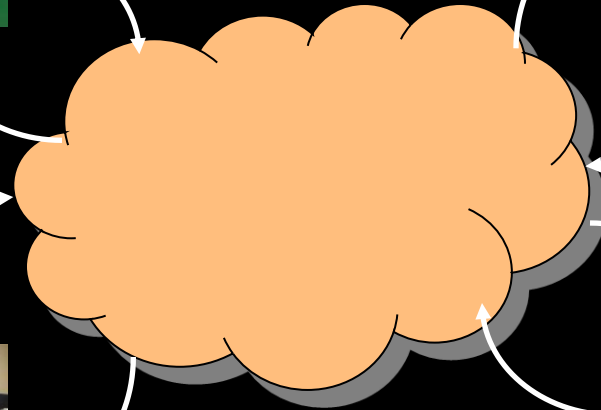


# Information Space and Sensor Uncertainty



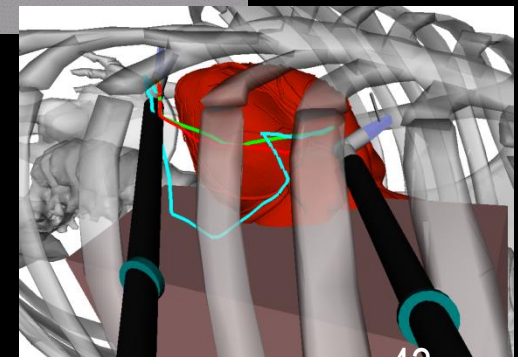
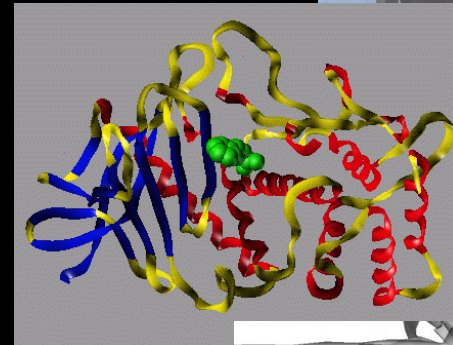
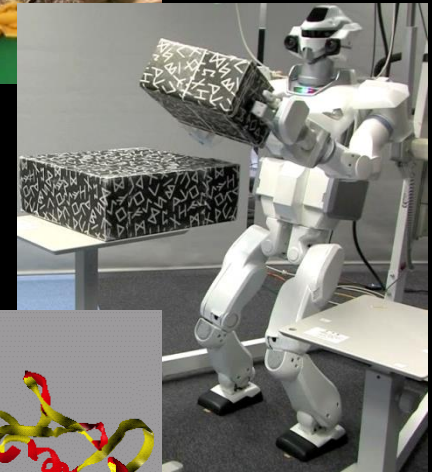
Consider multiple states of the world

# Planning with the Cloud



# Summary

- Robot motion planning is used for...
  - Vehicles
  - Robots
  - Digital Characters
  - Molecules
  - Design verification
- Types of planning methods
  - Exact algorithms
  - Discrete Search
  - Sampling-based planners
- *Many frontiers to explore*



# Homework

- Reading
  - Recap:
    - CH 1 - Introduction
    - Principles Appendix G - Analysis of Algorithm and Complexity Classes
  - Next class:
    - Graph Review (short)
    - Principles CH 4.0-4.1, 4.4 - Potential Fields
    - Principles CH 5.0-5.2 - Roadmaps, Voronoi diagram
    - Principles CH 6.0-6.1 - Cell decomposition
- Sign up for course on Piazza

**End**

# NP Complete

