A Surface Geometry Model for LiDAR Depth Completion

Yiming Zhao †, Lin Bai ‡, Ziming Zhang, and Xinming Huang ‡

Abstract—LiDAR depth completion is a task that predicts depth values for every pixel on the corresponding camera frame, although only sparse LiDAR points are available. Most of the existing state-of-the-art solutions are based on deep neural networks, which need a large amount of data and heavy computations for training the models. In this letter, a novel non-learning depth completion method is proposed by exploiting the local surface geometry that is enhanced by an outlier removal algorithm. The proposed surface geometry model is inspired by the observation that most pixels with unknown depth have a nearby LiDAR point. Therefore, it is assumed those pixels share the same surface with the nearest LiDAR point, and their respective depth can be estimated as the nearest LiDAR depth value plus a residual error. The residual error is calculated by using a derived equation with several physical parameters as input, including the known camera intrinsic parameters, estimated normal vector, and offset distance on the image plane. The proposed method is further enhanced by an outlier removal algorithm that is designed to remove incorrectly mapped LiDAR points from occluded regions. On KITTI dataset, the proposed solution achieves the best error performance among all existing non-learning methods and is comparable to the best self-supervised learning method and some supervised learning methods. Moreover, since outlier points from occluded regions is a commonly existing problem, the proposed outlier removal algorithm is a general preprocessing step that is applicable to many robotic systems with both camera and LiDAR sensors. The code has been published at https://github.com/placeforyiming/RAL_Non-Learning_DepthCompletion.

Index Terms—Computer vision for transportation, range sensing, sensor fusion.

I. INTRODUCTION

LiDAR is playing an important role for modern mobile robots. Many LiDAR related perception tasks, such as LiDAR 3D detection [1] or point cloud semantic segmentation [2] attract many recent contributions. LiDAR-based depth completion is one of those tasks which aims to provide a full dense depth map for the camera from the sparse depth generated by mapping LiDAR points on the image. Before the booming of LiDAR technology, depth completion is usually referred as a challenge to complete missing depth from depth sensors like Microsoft Kinect [3]. The first LiDAR-based depth completion paper [4] proposed a unique sparsity challenge as each LiDAR scan contains only about 5% values on the corresponding image. The benchmark on KITTI LiDAR depth completion task has attracted many interesting research works [5].

A straightforward solution is using neural network as a regression function trained with labels. Most of those papers are borrowing ideas from recently developed deep learning algorithms, such as different post-process modules [6], or various network structures like encoder-decoder or hourglass [7], [8]. In contrast, this paper proposes a model-based explainable non-learning method to complete the depth map. In Fig. 1, we show one sample from our non-learning method. The generated depth map recovers the surroundings by embedding all the RGB values in the 3D world.

Motivation Many neural network methods have been proposed recently for the LiDAR depth completion task. Supervised learning requires labeled data, while self-supervised learning [7] is able to train the network without labels. The label-free merit allows the method to easily adapt new environments by avoiding offline labeling work. However, a recent paper reports a simple non-learning method with classical image processing operators that achieves comparable performance with deep learning methods [9]. Since the non-learning solution shares the same label-free merit, we are intrigued to think what is the hidden mechanism behind this simple method with image processing operations like dilation.

Fig. 1. Illustration of the depth completion task. From top to bottom: RGB image, sparse LiDAR input, dense completed depth map, and colored 3D points in real world. This sample comes from the validation dataset in KITTI.
Outlier Removal Since LiDAR and camera are two sensors observing the world from different views, there will be some small occluded regions that are only observed by the LiDAR sensor but not observed by the camera. Mapping those points on image plane will create many incorrect depth values. To further evaluate this kind of error, we directly calculate the error between the raw sparse LiDAR and the ground truth on the KITTI validation set. The RMSE (root mean square error) is 1595 mm that is even larger than the completed depth map generated by many models. This explains why dilation works as it replaces some of those erroneous values with the smallest value in the local patch. However, the dilation will also change values of many LiDAR points that are not occluded. To solve this challenge, we propose a generalized outlier removal algorithm as a preprocessing step for the non-learning depth completion method.

Local Surface Geometry Besides the outlier removal, we also investigate why filling in the empty pixel with the smallest value in a local patch will not generate large errors. We identify the relationship between the empty pixel with its surrounding points is decided by the local surface geometry. Thus, we make an assumption that most empty pixels are likely sharing the same surface with their nearest point. Then, the empty depth value is estimated as an initial guess from the nearest value plus a residual determined by the direction of the local surface and the relative distance. In fact, our model is able to produce solid performance on KITTI, which demonstrates the effectiveness of the sharing local surface assumption. Note that the sharing surface assumption implies the point cloud should contain enough geometry information of objects, such as the commonly used 64-line LiDAR. We will discuss the model performance in regarding to various input sparsity in Section V.

Contribution Due to the space limitation, we prepare more supportive materials about the sharing surface assumption and outlier removal algorithm in the supplementary file. We summarize two major contributions of this paper as following:

- We propose a general outlier removal algorithm to remove incorrect depth values projected on the image by points from occluded regions. Considering the displacement of LiDAR and camera is usually small, the parallax effect created by the displacement is also smaller than most objects’ size. This finding builds the intuition of our algorithm that those points with parallax effect should be identified as outliers. We further extend this intuition to three observations and successfully design an effective algorithm. The proposed outlier removal algorithm is parameter-free that only needs the image and LiDAR resolutions, i.e., 64 line or 32 line for LiDAR, 256 × 256 or 512 × 512 for image. Therefore, the algorithm can be directly applied to many LiDAR-camera systems as a pre-processing step.

- We propose a model-based explainable non-learning depth completion method and achieve good performance with several practical merits. On KITTI, we achieve the best performance among all non-learning methods, and also achieve similar or better performance compared with all recently developed self-supervised learning methods. As an explainable model, it also clearly indicates the working condition that the point cloud should contain enough geometry information. Our model also shares all the merits of non-learning methods, such as label-free, robust to changing environment, and computational friendly.

II. RELATED WORK

Classical methods for depth completion Before the wide adoption of outdoor LiDAR for autonomous driving, depth completion was researched as a task to fill up the depth map generated from the RGB-D camera. Some classical methods were proposed to solve the image inpainting or depth quality improvement problem for RGB-D depth map [10]–[14]. The ratio of missing data from RGB-D depth map is roughly around 10% to 30%, which is different from the sparsity of LiDAR points. Besides completing the generated depth map from the RGB-D camera, some researchers assumed only a few points have been matched by the stereo camera and complete this sparse input to dense by using optimization methods like compressive sensing [15]–[17]. The natural difference between LiDAR sensors and those RGB-D sensors urges researchers to design new methods for outdoor LiDAR depth completion. Recently, Ku et al. [9] proposed a fast method for LiDAR-based depth completion with simple image processing operators, including dilation, Gaussian blur, etc. This simple method even obtained the comparable result with some learning-based methods. We choose this method as one of our baseline comparisons.

Supervised learning methods for depth completion The recent success of deep neural networks on several computer vision tasks attracts researchers to solve the depth completion task by using neural networks. The supervised way treats the network as a regression model to directly output depth value. To handle sparse depth, various ideas were proposed in different aspects, like special designed layers [18], [19], encoder-decoder structure [7], fusion with semantic segmentation [20], [21], etc. Besides completion with LiDAR only, integrating image as a branch shows a relatively large improvement. Some works modeled RGB branch inspired by the use of surface normal [22]–[24]. Since LiDAR can capture the geometry information, the fusion of geometry information with image texture information was also investigated in [25], [26]. There are other ideas that also have been tried to solve this task. Imran et al. [27] proposed a new depth representation named Depth Coefficients. Chen et al. [6] designed a post-process module to further improve the model performance.

Self-supervised learning methods for depth completion Self-supervised learning can train the network without labels. Self-supervised depth prediction relies on the image warping and photometric loss to penalize the error [28], [29]. Ma et al. [7] extended the self-supervised depth prediction framework to depth completion by feeding the sparse points into the network and treating them as the ground truth for corresponding pixels. Moreover, Yang et al. [30] integrated their Conditional Prior Network to the self-supervised depth completion pipeline and got a better performance. Wong [31] further considered pose consistency and geometric compatibility for performance improvement. Yao [32] proposed a binary anisotropic diffusion tensor to eliminate smoothness constraint at intended positions and directions. Those self-supervised methods do not need labels,
which allows them to update weights online. This convenience is useful for many advanced situations like federated learning, domain adaptive learning, and user privacy protection.

**In summary** Self-supervised methods have label-free merit. On the contrary, supervised methods need labels but usually yield better performance. Moreover, from the view of input modality, sensor fusion methods with both LiDAR and RGB have better performance, but LiDAR only methods are not sensitive to the change of lighting conditions, thus is stable in extreme cases such as dark night. Our method is label-free and only needs LiDAR as input. We compare the performance with all label-free methods on the popular KITTI benchmark as well as show additional benefits through a night-time sample from the Waymo dataset qualitatively.

### III. Methods

#### A. Outlier Removal

Though camera and LiDAR are usually mounted close to each other, there is still a small displacement between them. Due to their slightly different views, the multi-planar parallax will create some occluded regions which are observed by LiDAR but should not be observed by camera. Mapping those points on image plane leads to a large error as those points are coming from far away background. To address this challenge, we propose a general outlier removal algorithm that can work on arbitrary image and LiDAR resolutions. In Fig. 2, we show two examples that many points from the background are mapped onto foreground tree or cyclist. Our proposed solution will identify and remove those points and keep a clean boundary for objects.

Our removal algorithm is based on three observations:

- **Most outlier points will change the relative position with some nearby correct points as they are occluded by foreground objects.** Although there are some exceptions, for instance, the outlier is just mapped on the edge of the foreground, or the size of the foreground object is small. We argue most outliers will have this property.

- **Outlier points have relatively larger depth values compared with nearby correct depth values since they are coming from further background.**

- **Outlier points will create denser regions on image since they are mixed with points belong to the foreground.**

We further illustrate those three observations in Fig. 3. They build the foundation of our outlier removal algorithm.

Here, we assume that we have an image with the resolution $W \times H$, and a LiDAR with $L$ lines. There are $N$ points in total which are mapped on the image plane. Average distances between two points in two directions on image plane can be roughly estimated as $\frac{W}{N}$ and $\frac{H}{L}$. Therefore, for a specific point $i$ on the image plane $(\mu_i, \nu_i)$, we define a set of nearby points in a local region as:

$$S(i) = \left\{ n | \forall n \in (1, .., N), |\mu_j - \mu_i| < \frac{W}{N} \& |\nu_j - \nu_i| < \frac{H}{L} \right\}$$

In the LiDAR coordinate, we choose the spherical representation for the point $i$ as $(r_i, \theta_i, \phi_i)$. The depth value on the image plane is defined as $z_i$.

In our outlier removal algorithm, the `condition_1` and `condition_2` are indicators to check if the point $i$ meet our first and second observations, respectively. Our third observation suggests outliers are coming from denser regions. Since the local region $S(i)$ is defined with average distances in $H$ and...
Algorithm 1: Outlier Removal.

\begin{verbatim}
for i in (1,2,...,N) do
  for j in S(i) do
    condition_1 ← False, condition_2 ← False
    if \((\mu_i - \mu_j) \cdot (\theta_i - \theta_j) < 0\) or
      \((\nu_i - \nu_j) \cdot (\phi_i - \phi_j) < 0\) then
      condition_1 ← True
    if \(z_i > z_j + \epsilon\) then
      condition_2 ← True
    if condition_1 == True and
      condition_2 == True then
      remove i
      break
\end{verbatim}

W directions, the third observation suggests that \(S(i)\) should contain extra points if point \(i\) is an outlier. The \(\epsilon\) is a small value, and we choose \(\epsilon = 1.0\) m in this paper.

B. Surface Geometry Model for Depth Completion

Geometric Model Here we demonstrate a geometric model to complete the depth of empty pixel from its nearest pixel with value. We illustrate our intuition in Fig. 4.

As we can see, those empty green points share the same surface with the blue point in a small local patch. Let \([x, y, z]\) and \([x', y', z']\) be the 3D locations of one green point and the blue point. Further assuming that the intrinsic matrix of the camera is known and fixed as \(K\), we can calculate the location of a 3D point \([x, y, z]\) in the camera coordinate as:

\[
[x, y, z]^T = (z' + \Delta z)K^{-1}[u, v, 1]^T, \tag{1}
\]

where \([u, v]\) and \([\Delta u, \Delta v]\) denote the 2D location and the offset between the two points in the depth image, respectively, \(\Delta z\) denotes the difference between the estimated depth and the ground-truth, and \((\cdot)^{-1}\) and \((\cdot)^T\) denote the matrix inverse and transpose operators, respectively. Similarly, we can compute \([x', y', z']^T\) as follows:

\[
[x', y', z']^T = z'K^{-1}[u + \Delta u, v + \Delta v, 1]^T. \tag{2}
\]

Now considering the simplest pinhole model with focal length \([f_u, f_v]\) and component point \([p_u, p_v]\), we can get

\[
x = (z' + \Delta z)(u - p_u)/f_u, \quad y = (z' + \Delta z)(v - p_v)/f_v,
\]

\[
x' = z'(u + \Delta u - p_u)/f_u, \quad y' = z'(v + \Delta v - p_v)/f_v.
\]

Since we know that \([u, v, z]\) and \([u + \Delta u, v + \Delta v, z']\) come from the same surface, we have the equation:

\[
n \cdot [x - x', y - y', \Delta z]^T = 0, \tag{3}
\]

where \(n\) is the normal vector of the surface.

Then, the depth value \(z\) for empty pixel can be written as:

\[
z = z' + \Delta z, \tag{4}
\]

where

\[
\Delta z = \left(\frac{\Delta u}{f_u}, \frac{\Delta v}{f_v}, 0\right) \cdot n
\]

Eq. 5 indicates the residual is decided by the nearest value itself, the offsets in image coordinate, the local surface normal, and camera parameters.

Surface Normal A common way to calculate the surface normal is fitting the local plane from the nearest neighbors of the query point [33]. However, those K-Nearest Neighbor based methods are too slow to process 64 line LiDAR point cloud which contains almost 20 k points only in the front view. Fortunately, the special property of LiDAR sensor stimulates some more practical solutions. Following Badino’s method [34], we map LiDAR points from Cartesian coordinate system \((x, y, z)\) to spherical coordinate system \((r, \theta, \phi)\). Then, the normal vector is the derivative of function \(r(\theta, \phi)\) in Cartesian coordinate, denoted as:

\[
n = \nabla_{(\hat{x}, \hat{y}, \hat{z})} r(\theta, \phi), \tag{6}
\]

where \((\hat{x}, \hat{y}, \hat{z})\) is the unit vector in Cartesian coordinate. Eq. (6) has solution:

\[
n = \left(\begin{array}{c}
\hat{x} \\
\hat{y} \\
\hat{z}
\end{array}\right) R_{\theta, \phi} \left(\begin{array}{c}
1 \\
\frac{\partial r}{\partial \theta} \\
\frac{\partial r}{\partial \phi}
\end{array}\right),
\]

where

\[
R_{\theta, \phi} = \left(\begin{array}{ccc}
\cos \theta \sin \phi & \sin \theta & 0 \\
-\sin \theta \sin \phi & \cos \theta & 0 \\
0 & 0 & 1
\end{array}\right).
\]

This method [34] provides a fast way to calculate normal just like edge detection. We add one extra step to fill in those empty pixels, which gives us smooth normal for all points. We show an example of the calculated normal vector in Fig. 5. The consistency between the normal image and the RGB supports the sharing surface assumption that most pixel shares the same surface with the nearest LiDAR point.
Distance Transform [35] (DT) is an operator usually applied to binary images to generate distance maps (DM), which are grayscale images of the same size of the original images consisting of the distance as well as the offset to the closest available signal as each pixel value. For certain sampling functions, the complexity of DT is linear to the image size [36]. This gives us a fast way to find \( z^\prime \) and \( (\Delta \mu, \Delta \nu) \) needed for calculating \( \Delta z \) in Eq. (5). It also distributes calculated normal vector to each empty pixel.

C. Pipeline Summary

The whole pipeline of our non-learning method is summarized as four steps:

- **Step 1**: Project sparse points on spherical range image, calculate normal vector for each point, then project those points back on the original camera image plane.

- **Step 2**: Run outlier removal algorithm to remove incorrect values on sparse depth image.

- **Step 3**: Run DT (distance transform) algorithm to prepare \( z^\prime \), \( n \), \( (\Delta \mu, \Delta \nu) \) for each pixel on the original image plane.

- **Step 4**: Apply Eq. (4) and Eq. (5) to calculate depth for each pixel. Then, smooth the result with Gaussian filter.

We visualize each step of our solution in Fig. 5.

IV. EXPERIMENTS

A. Dataset

We conduct experiments on the KITTI dataset. The KITTI dataset is a benchmark and collection of sparse LiDAR scans and corresponding semi-dense depth maps which serve as the ground-truth. The dataset consists of 85 898 training samples, 1000 validation samples and 1000 test samples. The ground-truth for test dataset is invisible. People need to submit their predicted test results to the server in order to receive the metric scores.

On KITTI, four evaluation metrics are used to evaluate model performance:

- **RMSE**: Root mean squared error [mm]
- **MAE**: Mean absolute error [mm]
- **iRMSE**: Root mean squared error of the inverse depth [1/km]
- **iMAE**: Mean absolute error of the inverse depth [1/km]

B. Outlier Removal

The error of sparse depth map has been reported by some works [4], [24]. Here, we evaluate the error quantitatively. We calculate the error of samples on the validation set for those pixels which have values in both sparse input depth and ground truth. The error is surprisingly large as reported in the top row of Table I. After removing those outliers, the error of sparse input has been significantly reduced.

Our outlier removal algorithm is also beneficial to other methods. For instance, self-supervised depth completion methods utilize raw sparse input as ground truth for corresponding pixels. Simply removing outliers will improve the performance, shown in Table II by using SparseToDense [7] as an example.

C. The Performance of Surface Geometry Model

As a non-learning method, our surface geometry model has the advantage of directly working in any new environment without extra labeling work. This is also the major contribution of recent developed self-supervised depth completion methods [31], [32]. So we compare the performance of our method with all
non-learning methods and self-supervised methods on KITTI’s test leaderboard in Table III. We achieve the best MAE and the second best RMSE among all non-learning and self-supervised learning methods. Our method even can outperform some earlier supervised solutions. Recent developed supervised models are prone to use a large network with 10 million or even 100 million parameters [24], [41], [42], thus have better performance. As a reference, we also list two state-of-the-art supervised methods in Table III.

To complete the depth, two different input modality settings can be used. Sensor fusion models with RGB and LiDAR as input usually have better performance. However, it is still questionable if the method works under various lighting conditions. On the contrary, models with single LiDAR as input will not be affected by the change of lighting condition. The method proposed in this paper has such advantage as it only relies on geometry information.

D. Ablation Study

Effectiveness of Outlier Removal To better evaluate our outlier removal algorithm, we show the model performance on KITTI validation set in Table IV. It clearly shows that removing outliers can significantly improve the performance of our model. From both Table I and Table IV, our outlier removal method should be considered as a general preprocessing step for many camera-LiDAR sensor fusion tasks.

Effectiveness of Each Step Table IV illustrates the effectiveness of our outlier removal module. To further clarify the benefit of each step, in Table V, we show the change of RMSE, MAE and density after each step. We can see every step brings some improvements, and surface geometry connects all those steps together as an explainable non-learning model. The first two rows are the same as the Table I, one may check that table for more details.

V. DISCUSSION

A. Input Sparsity and Model Performance

The sharing surface assumption implies the point cloud should contain geometry information of objects, which is the case for commonly used 64-line LiDAR. It is worth to mention that recent papers even demonstrate a good result of panoptic segmentation on 64-line LiDAR only [2]. Here we discuss the performance of our method with sparser LiDAR density. By following the settings in SparseToDense [7], we group the 64-line LiDAR to downsample it as simulations of 32-line and 16-line LiDARs. We compare the performance of our model with the self-supervised results of SparseToDense [7] in Fig. 6. Our solution outperforms the baseline for both 32-line and 64-line cases, but the self-supervised baseline starts to take the lead in 16-line case. This phenomenon verifies the condition of our algorithm - The point cloud cannot be too sparse; otherwise it may lose the geometry information. We also display these three different density LiDAR raw inputs and completed maps in Fig. 6.
Fig. 7. Illustrate the ability of our method to provide depth maps for multi-cameras at night. This data sample is picked from the Waymo dataset.

B. Other Applications

On KITTI’s depth completion benchmark, we conduct the numerical evaluation and compare the performance with other depth completion methods. As a non-learning solution working on LiDAR only, our method has several benefits beyond numerical evaluation. First, our model is able to support driving under various lighting conditions, such as night-time driving. Second, owing to the label-free merit, our model is able to easily provide depth maps for cameras facing different directions. To illustrate those benefits, we give an example of our method on the Waymo dataset [43]. As a recently published driving dataset, the Waymo dataset has more versatile driving scenarios. However, there is no depth completion benchmark on it which prohibits us to quantitatively evaluate our surface model. Instead, we use it to qualitatively demonstrate extra benefits of our solution in Fig. 7. Based on the point cloud from the top LiDAR sensor, our method successfully provides dense depth maps for five cameras mounted around the car at night.

VI. CONCLUSIONS

In this letter, we propose a novel non-learning depth completion method based on surface geometry. The method achieves the best MAE and the second-best RMSE compared with all label-free methods, including all non-learning and self-supervised learning methods on KITTI’s leader board. This proposed algorithm is computationally efficient and can be used in any environment, therefore it is truly a practical solution to LiDAR depth completion task. Moreover, several individual modules, such as outlier removal or distributing normal vectors on the image plane, may also be beneficial to other robotics applications with both LiDAR and camera sensors.

REFERENCES


