

Section D02

NAME \_\_\_\_\_

Harry Potter

ver.A

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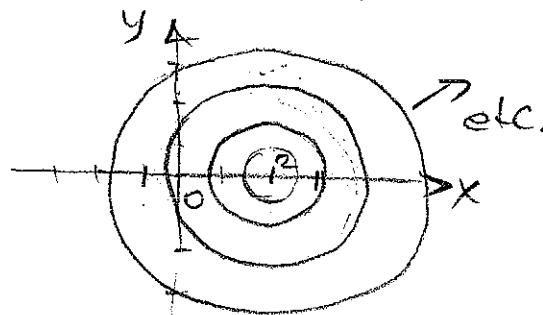
(30 points total)

1. (12.2, #6) (5 pts) State the largest possible domain of definition of the function  $f(x, y) = \sqrt{2x} + \sqrt[3]{3y}$

$\sqrt{2x}$  is real if  $x \geq 0$ ;  $\sqrt[3]{3y}$  is real for any  $y \Rightarrow$   
 $\Rightarrow$  domain of  $f(x, y)$ : all pts  $(x, y)$  for which  $x \geq 0$

2. (12.2, #37) (5 pts) Sketch a few typical level curves of the function  $f(x, y) = x^2 + y^2 - 4x$

Circles centered @  $(2, 0)$ :



3. (12.3, #14) (5 pts) Use the consequences of continuity to evaluate the limit  $\lim_{(x,y,z) \rightarrow (2,-1,3)} \frac{x+y+z}{x^2+y^2+z^2}$

$f(x, y, z) = \frac{x+y+z}{x^2+y^2+z^2}$  is continuous wherever  $x^2+y^2+z^2 \neq 0$ , i.e.  
 except  $(0, 0, 0)$

$$\lim_{(x,y,z) \rightarrow (2,-1,3)} f(x, y, z) = f(2, -1, 3) = \frac{2 - 1 + 3}{2^2 + (-1)^2 + 3^2} = \frac{4}{14} = \frac{2}{7}$$

4. Compute the partial derivatives of the functions:

$$(12.4, \#4) (7 \text{ pts}) f(x, y) = x^2 e^{xy}$$

$$f_x = 2x e^{xy} + x^2 y e^{xy} = x e^{xy} (xy + 2)$$

$$f_y = x^2 e^{xy}$$

$$(12.4, \#16) (8 \text{ pts}) f(u, v) = (2u^2 + 3v^2) \exp(-u^2 - v^2)$$

$$\begin{aligned} f_u &= 4u \exp(-u^2 - v^2) - (2u^2 + 3v^2) 2u \exp(-u^2 - v^2) = \\ &= 2u \left( 2 - 2u^2 - 3v^2 \right) \exp(-u^2 - v^2) \end{aligned}$$

$$\begin{aligned} f_v &= 6v \exp(-u^2 - v^2) - (2u^2 + 3v^2) 2v \exp(-u^2 - v^2) = \\ &= 2v \left( 3 - 2u^2 + 3v^2 \right) \exp(-u^2 - v^2) \end{aligned}$$