


Section B01 & B02NAME JAMES BOND

Circle

Print

(30 points total)

1. (1.1, #37) (4 pts) Express the circumference
- C
- of a circle as a function of its area
- A
- .

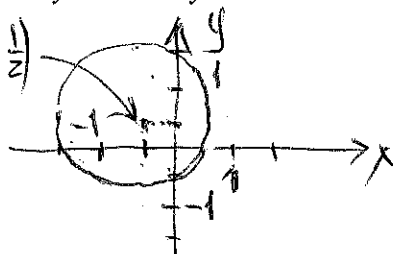


$$C = 2\pi r \rightarrow C = 2\pi \sqrt{\frac{A}{\pi}} = 2\sqrt{\pi A} \Rightarrow \underline{C(A) = 2\sqrt{\pi A}}$$

$$A = \pi r^2 \rightarrow r = \sqrt{\frac{A}{\pi}}$$

2. (1.2, #15) (5 pts) Sketch the translated circle corresponding to the equation
- $2x^2 + 2y^2 + 2x - 2y = 1$
- and indicate its center and radius.

$$2x^2 + 2y^2 + 2x - 2y = 1; \quad x^2 + x + \frac{1}{4} + y^2 - y + \frac{1}{4} = 1$$

$$x^2 + y^2 + x - y = \frac{1}{2}; \quad \left(x + \frac{1}{2}\right)^2 + \left(y - \frac{1}{2}\right)^2 = 1 \Rightarrow$$


3. (1.4, #17) (4 pts) Given
- $f(x) = \sin x$
- and
- $g(x) = x^3$
- , find
- $f(g(x))$
- and
- $g(f(x))$
- .

$$f(x) = x \sin x; \quad g(x) = x^3 \Rightarrow \begin{cases} f(g(x)) = f(x^3) = \sin x^3 \\ g(f(x)) = g(\sin x) = (\sin x)^3 = \sin^3 x \end{cases}$$

4. (2.1, #19) (6 pts) Find all points of the curve
- $y = x - (x/10)^2$
- at which the tangent line is horizontal.

$$y = x - \left(\frac{x}{10}\right)^2 = -\frac{x^2}{100} + x$$

$$m(a) = 0 \text{ when } a = 50;$$

$$m \text{ for } f \Rightarrow m(a) = -\frac{a}{50} + 1$$

$$y = -\frac{50^2}{10^2} + 50 = -\frac{2500}{100} + 50 = 25, \text{ so}$$

the tangent line is horiz. @ $(50, 25)$

5. (2.2, #13) (5 pts) Apply the limit laws to evaluate the limit
- $\lim_{z \rightarrow 8} \frac{z^{2/3}}{z - \sqrt{2z}}$

$$\lim_{z \rightarrow 8} \frac{z^{2/3}}{z - \sqrt{2z}} = \frac{\lim_{z \rightarrow 8} z^{2/3}}{\lim_{z \rightarrow 8} (z - \sqrt{2z})} = \frac{4}{4} = 1$$

6. (2.3, #21) (6 pts) Find the trigonometric limit
- $\lim_{x \rightarrow 0} x \cot 3x$

$$\lim_{x \rightarrow 0} x \cot 3x = \lim_{x \rightarrow 0} x \frac{\cos 3x}{\sin 3x} = \lim_{x \rightarrow 0} \frac{3x}{\sin 3x} \cdot \frac{\cos 3x}{3} = \lim_{x \rightarrow 0} \left(\frac{3x}{\sin 3x}\right) \lim_{x \rightarrow 0} \left(\frac{\cos 3x}{3}\right) =$$

$$= \lim_{x \rightarrow 0} \frac{1}{\left(\frac{\sin 3x}{3x}\right)} \lim_{x \rightarrow 0} \left(\frac{\cos 3x}{3}\right) = 1 \cdot \frac{1}{3} = \frac{1}{3}$$