

↑ v i g

$$\Delta x = v_{0x} t$$

$$\Delta x = v_0 \cos \theta t$$

$$\Delta x = \frac{2v_0 \cos \theta \sin \theta}{g}$$

$$\Delta x = \frac{\sin(2\theta) v_0^2}{g}$$

max when $2\theta = 90^\circ$
so $\theta = 45^\circ$
when maxed

$$y = v_0 t + \frac{1}{2} g t^2$$

$$0 = 0 + v_0 \sin \theta t - \frac{1}{2} g t^2$$

$$0 = t(v_0 \sin \theta - \frac{1}{2} g t)$$

$$v_0 \sin \theta = \frac{1}{2} g t$$

$$t = \frac{2v_0 \sin \theta}{g}$$

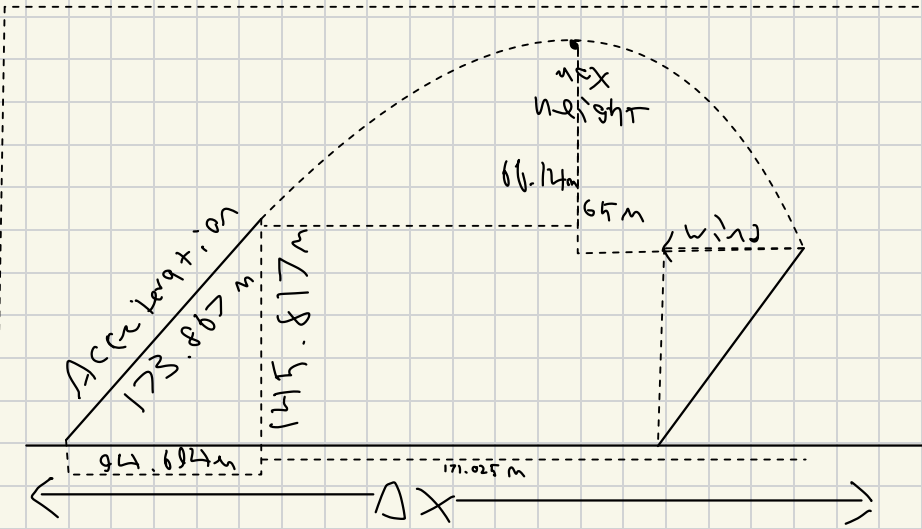
$\sin \theta = \cos(90 - \theta)$ and vice versa

$\sin(2\theta) = 2 \sin \theta \cos \theta$

$\sin 20^\circ = \cos 70^\circ$

$\sin 70^\circ = \cos 20^\circ$

Launch angle	57°	deg
Engine burn time	8.1	sec
Net acceleration of rocket while engine burns	5.3	m/s ²
Vertical distance rocket falls from max height before parachute opens	65	m
Rocket with parachute constant vertical speed	10.0	m/s
Wind and rocket with parachute constant horizontal speed	18	m/s



① Attempting to find the distance travelled during first stage.

$$x = x_0 + v_0 t + \frac{1}{2} g t^2$$

$$x = 0 + 0 + \frac{1}{2} (5.3) (8.1)^2$$

$$x = 173.867 \text{ m } 57^\circ \text{ North of East}$$

② Break vector into x and y components

$$\sin \theta = \frac{y}{h} \quad \cos \theta = \frac{x}{h}$$

$$\sin 57^\circ = \frac{y}{173.867} \quad \cos 57^\circ = \frac{x}{173.867}$$

$$173.867 \sin 57^\circ = y \quad 173.867 \cos 57^\circ = x$$

$$y = 145.817 \text{ m} \quad x = 94.694 \text{ m}$$

③ find velocities at end of 1st phase.

$$v = v_0 + g t$$

$$v = 0 + (5.3)(8.1)$$

$$v = 42.93$$

$$\sin \theta = \frac{v_y}{v}$$

$$\sin 57^\circ = \frac{v_y}{42.93}$$

$$42.93 \sin 57^\circ = v_y$$

$$v_y = 36.00 \text{ m/s}$$

$$\cos \theta = \frac{v_x}{v}$$

$$\cos 57^\circ = \frac{v_x}{42.93}$$

$$42.93 \cos 57^\circ = v_x$$

$$v_x = 23.38 \text{ m/s}$$

⑤ find Δx over phase 2

$$y = v_0 t + \frac{1}{2} g t^2$$

$$146.955 = 145.817 + 36t + 4.9t^2$$

$$t = 2.315 \text{ s}$$

$$\Delta x = v t$$

$$\Delta x = v_x t$$

$$\Delta x = (23.38)(2.315)$$

$$\Delta x = 54.17$$

④ find max height of phase 2

$v_{y1} = v_{0y}$

Phase 1 Phase 2

$$v_{y1}^2 = v_{0y1}^2 + 2g\Delta y$$

$$0 = 1296.30 + 2(-9.8)\Delta y$$

$$\Delta y = 66.14 \text{ m above end of phase 1}$$

6. find distance for phase 3

$$\Delta y = v t$$

$$65 = (10) t$$

$$t = 6.5 \text{ s}$$

$$\Delta x = v t$$

$$\Delta x = (-18)(6.5)$$

$$\Delta x = -117 \text{ m}$$

7. add all Δx's from previous steps

$$94.694 + 171.025 - 117 = 148.719 \text{ m east}$$