Gpgti { "\*G+'ku'o quv'htgs wgpvn{ "gzr tguugf "kp" vgto u"qh<" Kinetic Energy for a mass (m) at a velocity (V) (an Extensive Property)

$$KE = \frac{1}{2}mV^2$$

Frequently, one is interested in the change of KE from State 1 to State 2:

$$\Delta \mathrm{KE} = \frac{1}{2} \mathbf{m} (\mathrm{V}_2^2 - \mathrm{V}_1^2)$$

Potential Energy for a mass (m) in a gravational potential field (g) at a height z (an Extensive Property)

PE = mgz

Frequently, one is interested in the change of PE from State 1 to State 2:

$$\Delta PE = PE_2 - PE_1 = m g (z_2 - z_1)$$

Internal Energy (U): A measure of energy at a macroscopic level due to the molecular translation, vibration, rotation (an Extensive Property). Internal Energy can also be expressed as an intensive property u=U/m (internal energy per unit mass).

Tabl	e A-4	(Continu	ied)					
Т	υ	и	h	S	υ	и	h	S
°C	m <sup>3</sup> /kg	kJ/kg	kJ/kg	kJ/kg · K	m <sup>3</sup> /kg	kJ/kg	kJ/kg	kJ/kg · K
	р	= 5.0 bar	= 0.50  M	APa	р	= 7.0 ba	r = 0.70	MPa
		$(T_{\rm sat} = 1)$	151.86°C)			$(T_{\rm sat} =$	164.97°C)	)
Sat.	0.3749	2561.2	2748.7	6.8213	0.2729	2572.5	2763.5	6.7080
180	0.4045	2609.7	2812.0	6.9656	0.2847	2599.8	2799.1	6.7880
200	0.4249	2642.9	2855.4	7.0592	0.2999	2634.8	2844.8	6.8865
240	0.4646	2707.6	2939.9	7.2307	0.3292	2701.8	2932.2	7.0641
280	0.5034	2771.2	3022.9	7.3865	0.3574	2766.9	3017.1	7.2233
320	0.5416	2834.7	3105.6	7.5308	0.3852	2831.3	3100.9	7.3697
360	0.5796	2898.7	3188.4	7.6660	0.4126	2895.8	3184.7	7.5063
400	0.6173	2963.2	3271.9	7.7938	0.4397	2960.9	3268.7	7.6350
440	0.6548	3028.6	3356.0	7.9152	0.4667	3026.6	3353.3	7.7571
500	0.7109	3128.4	3483.9	8.0873	0.5070	3126.8	3481.7	7.9299
600	0.8041	3299.6	3701.7	8.3522	0.5738	3298.5	3700.2	8.1956
700	0.8969	3477.5	3925.9	8.5952	0.6403	3476.6	3924.8	8.4391

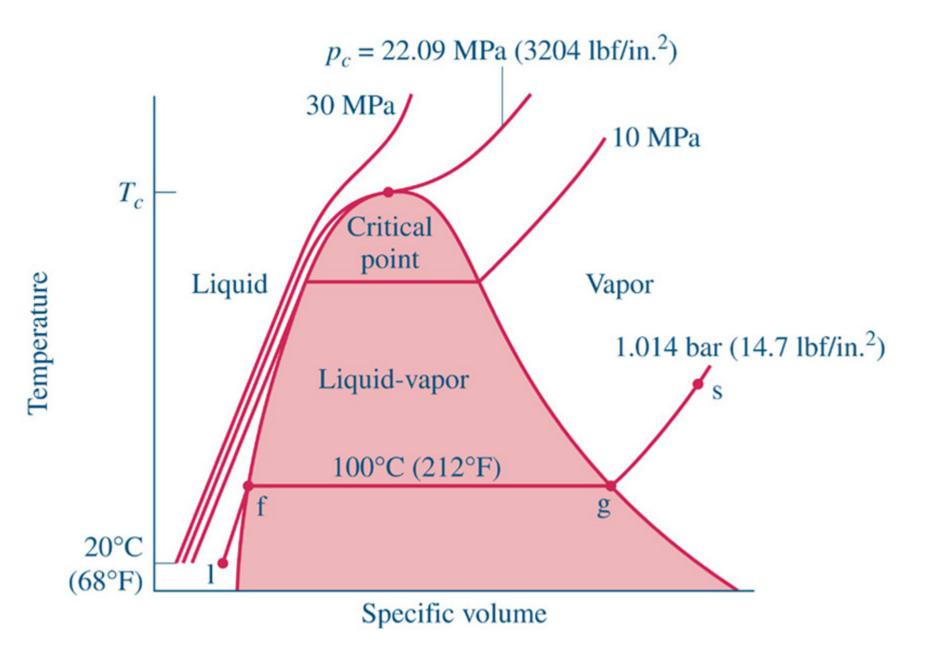
Frequently, internal energy is presented in tables, such as Table A-4 for superheated water vapor.

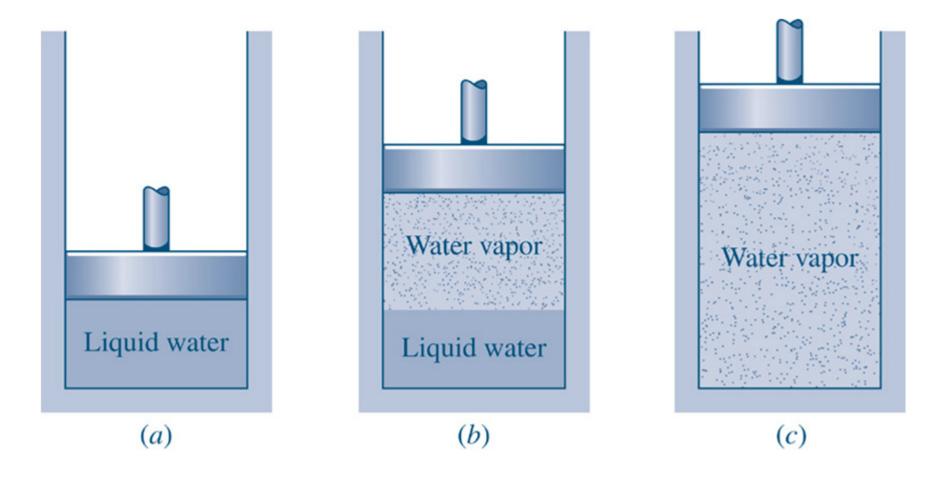
The Design and Analysis of many engineering systems requires thermodynamics (in addition to fluid mechanics, heat transfer, structural analysis, etc.)

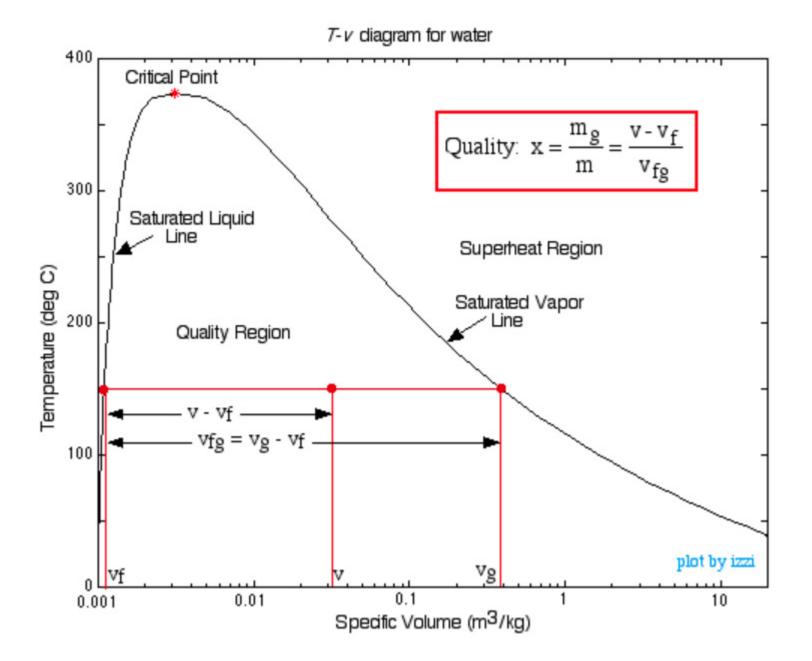
Consider a Simple Power System. Thermodynamics establishes the limits on the Maximum Power Out (Work Out) for a given Qin for a particular system of interest.

	ropy g∙K	Entr kJ/kg	Internal Energy Enthalpy kJ/kg kJ/kg				Specific Volume Inte m <sup>3</sup> /kg		APa /	ressure Conversions: bar = 0.1 MPa = $10^2$ kPa	
Prob	Sat. Vapor s <sub>g</sub>	Sat. Liquid s <sub>f</sub>	Sat. Vapor h <sub>g</sub>	Evap. $h_{\rm fg}$	Sat. Liquid h <sub>r</sub>	Sat. Vapor <i>u</i> g	Sat. Liquid u <sub>r</sub>	Sat. Vapor v <sub>g</sub>	Sat. Liquid $v_{\rm f} \times 10^3$	Temp. °C	= 10 <sup>-</sup> Press. bar
(	8.4746	0.4226	2554.4	2432.9	121.46	2415.2	121.45	34.800	1.0040	28.96	0.04
(	8.3304	0.5210	2567.4	2415.9	151.53	2425.0	151.53	23.739	1.0064	36.16	0.06
(	8.2287	0.5926	2577.0	2403.1	173.88	2432.2	173.87	18.103	1.0084	41.51	0.08
(	8.1502	0.6493	2584.7	2392.8	191.83	2437.9	191.82	14.674	1.0102	45.81	0.10
(	7.9085	0.8320	2609.7	2358.3	251.40	2456.7	251.38	7.649	1.0172	60.06	0.20
(	7.7686	0.9439	2625.3	2336.1	289.23	2468.4	289.20	5.229	1.0223	69.10	0.30
(	7.6700	1.0259	2636.8	2319.2	317.58	2477.0	317.53	3.993	1.0265	75.87	0.40
(	7.5939	1.0910	2645.9	2305.4	340.49	2483.9	340.44	3.240	1.0300	81.33	0.50
(	7.5320	1.1453	2653.5	2293.6	359.86	2489.6	359.79	2.732	1.0331	85.94	0.60
0	7.4797	1.1919	2660.0	2283.3	376.70	2494.5	376.63	2.365	1.0360	89.95	0.70
(	7.4346	1.2329	2665.8	2274.1	391.66	2498.8	391.58	2.087	1.0380	93.50	0.80
(	7.3949	1.2695	2670.9	2265.7	405.15	2502.6	405.06	1.869	1.0410	96.71	0.90
1	7.3594	1.3026	2675.5	2258.0	417.46	2506.1	417.36	1.694	1.0432	99.63	1.00
1	7.2233	1.4336	2693.6	2226.5	467.11	2519.7	466.94	1.159	1.0528	111.4	1.50
2	7.1271	1.5301	2706.7	2201.9	504.70	2529.5	504.49	0.8857	1.0605	120.2	2.00

 Table A-3
 Properties of Saturated Water (Liquid–Vapor): Pressure Table







http://www.engineeringthermodynamics.org/Intro/Chapt.1\_6/Chapter2a.html

CHAPTER-1

#### http://www.engineeringthermodynamics.org/Intro/Chapt.1\_6/Chapter2a.html

p =	1.0 MPa	p = 1.5  MPa			
$T(^{\circ}C)$	$v (m^3/kg)$	$T(^{\circ}C)$	$v (m^3/kg)$		
200	0.2060	200	0.1325		
240	0.2275	240	0.1483		
280	0.2480	280	0.1627		

**3.7** The following table lists temperatures and specific volumes of water vapor at two pressures:

Data encountered in solving problems often do not fall exactly on the grid of values provided by property tables, and *linear interpolation* between adjacent table entries becomes necessary. Using the data provided here, estimate

- (a) the specific volume at  $T = 240^{\circ}$ C, p = 1.25 MPa, in m<sup>3</sup>/kg.
- (b) the temperature at p = 1.5 MPa, v = 0.1555 m<sup>3</sup>/kg, in<sup>o</sup>C.
- (c) the specific volume at  $T = 220^{\circ}$ C, p = 1.4 MPa, in m<sup>3</sup>/kg.

Tabl	e A-5	Properties of Compressed Liquid Water								
T	$v \times 10^3$	u	h	s	$v \times 10^3$	u	h	s		
℃	m <sup>3</sup> /kg	kJ/kg	kJ/kg	kJ/kg · K	m <sup>3</sup> /kg	kJ/kg	kJ/kg	kJ/kg ∙ K		
			= 2.5 MP (23.99°C)	a	p = 50  bar = 5.0  MPa $(T_{\text{sat}} = 263.99^{\circ}\text{C})$					
20	1.0006	83.80	86.30	.2961	.9995	83.65	88.65	.2956		
40	1.0067	167.25	169.77	.5715	1.0056	166.95	171.97	.5705		
80	1.0280	334.29	336.86	1.0737	1.0268	333.72	338.85	1.0720		
100	1.0423	418.24	420.85	1.3050	1.0410	417.52	422.72	1.3030		
140	1.0784	587.82	590.52	1.7369	1.0768	586.76	592.15	1.7343		
180	1.1261	761.16	763.97	2.1375	1.1240	759.63	765.25	2.1341		
200	1.1555	849.9	852.8	2.3294	1.1530	848.1	853.9	2.3255		
220	1.1898	940.7	943.7	2.5174	1.1866	938.4	944.4	2.5128		
Sat.	1.1973	959.1	962.1	2.5546	1.2859	1147.8	1154.2	2.9202		

#### 

We rarely use the Compressed Liquid tables. Generally, the values are very close to those in the saturated tables at the given temperature. That is, changing the pressure of a liquid does not significantly change the state properties (other than pressure).

	ropy g∙K	Entr kJ/kg	Internal Energy Enthalpy kJ/kg kJ/kg				Specific Volume Inte m <sup>3</sup> /kg		APa /	ressure Conversions: bar = 0.1 MPa = $10^2$ kPa	
Prob	Sat. Vapor s <sub>g</sub>	Sat. Liquid s <sub>f</sub>	Sat. Vapor h <sub>g</sub>	Evap. $h_{\rm fg}$	Sat. Liquid h <sub>r</sub>	Sat. Vapor <i>u</i> g	Sat. Liquid u <sub>r</sub>	Sat. Vapor v <sub>g</sub>	Sat. Liquid $v_{\rm f} \times 10^3$	Temp. °C	= 10 <sup>-</sup> Press. bar
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(	7.9085	0.8320	2609.7	2358.3	251.40	2456.7	251.38	7.649	1.0172	60.06	0.20
(	7.7686	0.9439	2625.3	2336.1	289.23	2468.4	289.20	5.229	1.0223	69.10	0.30
(	7.6700	1.0259	2636.8	2319.2	317.58	2477.0	317.53	3.993	1.0265	75.87	0.40
(	7.5939	1.0910	2645.9	2305.4	340.49	2483.9	340.44	3.240	1.0300	81.33	0.50
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0	7.4797	1.1919	2660.0	2283.3	376.70	2494.5	376.63	2.365	1.0360	89.95	0.70
(	7.4346	1.2329	2665.8	2274.1	391.66	2498.8	391.58	2.087	1.0380	93.50	0.80
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1	7.3594	1.3026	2675.5	2258.0	417.46	2506.1	417.36	1.694	1.0432	99.63	1.00
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 Table A-3
 Properties of Saturated Water (Liquid–Vapor): Pressure Table

In engineering thermodynamics the change in energy of a system is composed of three contributions:

- Kinetic energy
- Gravitational potential energy
- Internal energy

## **Change in Kinetic Energy**

- The change in kinetic energy is associated with the motion of the system as a whole relative to an external coordinate frame such as the surface of the earth.
- For a system of mass *m* the change in kinetic energy from state 1 to state 2 is

$$\Delta KE = KE_2 - KE_1 = \frac{1}{2} m \left( V_2^2 - V_1^2 \right) \quad (Eq. 2.5)$$

#### where

V<sub>1</sub> and V<sub>2</sub> denote the velocities at their respective states.
 The symbol Δ denotes: final value minus initial value.

## **Change in Gravitational Potential Energy**

The change in gravitational potential energy is associated with the position of the system in the earth's gravitational field.

For a system of mass *m* the change in potential energy from state 1 to state 2 is

$$\Delta PE = PE_2 - PE_1 = mg(z_2 - z_1)$$
 (Eq. 2.10)

#### where

*z*<sub>1</sub> and *z*<sub>2</sub> denote the elevations relative to the surface of the earth at states 1 and 2, respectively.
 *g* is the acceleration of gravity.

## **Change in Internal Energy**

- The change in internal energy is associated with the makeup of the system, including its chemical composition.
- There is no simple expression comparable to Eqs. 2.5 and 2.10 for evaluating internal energy change for a wide range of applications. In most cases we will evaluate internal energy change using data from tables in appendices of the textbook.
- Like kinetic and gravitational potential energy, internal energy is an extensive property.
  - Internal energy is represented by U.
  - The specific internal energy on a mass basis is u.
  - The specific internal energy on a molar basis is  $\overline{u}$ .

# Change in Energy of a System

In summary, the change in energy of a system from state 1 to state 2 is

$$E_2 - E_1 = (U_2 - U_1) + (KE_2 - KE_1) + (PE_2 - PE_1)$$
(Eq. 2.27a)  

$$\Delta E = \Delta U + \Delta KE + \Delta PE$$
(Eq. 2.27b)

► It is frequently the *changes* in the *energy* of a system between states that have significance.

## **Energy Transfer by Work**

Energy can be transferred to and from closed systems by two means only:

► Work

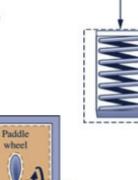
Heat

You have studied work in mechanics and those concepts are retained in the study of thermodynamics.

## **Illustrations of Work**

When a spring is compressed, energy is transferred to the spring by work.

► When a gas in a closed vessel is stirred, energy is transferred to the gas by work.



Gas

## **Energy Transfer by Work**

The symbol W denotes an amount of energy transferred across the boundary of a system by work.

Since engineering thermodynamics is often concerned with internal combustion engines, turbines, and electric generators whose purpose is to do work, it is convenient to regard the work done by a system as positive.

► W > 0: work *done by* the system

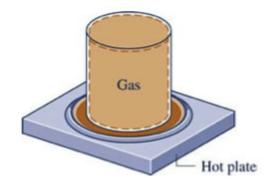
► W < 0: work done on the system

The same sign convention is used for the rate of energy transfer by work (power!), denoted by  $\dot{W}$ .

## **Energy Transfer by Heat**

Energy transfers by heat are induced only as a result of a temperature difference between the system and its surroundings.

Net energy transfer by heat occurs only in the direction of decreasing temperature.



## **Energy Transfer by Heat**

The symbol Q denotes an amount of energy transferred across the boundary of a system by heat transfer.

Heat transfer into a system is taken as positive and heat transfer from a system is taken as negative:

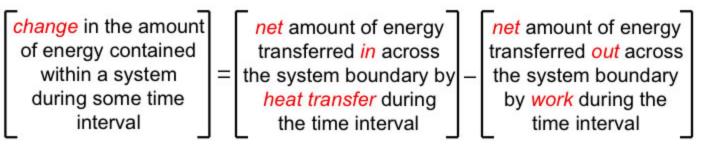
- ► Q > 0: heat transfer to the system
- ► Q < 0: heat transfer from the system

The same sign convention is used for the rate of energy transfer by heat, denoted by  $\dot{Q}$ .

If a system undergoes a process involving no heat transfer with its surroundings, that process is called adiabatic.

## Summary: Closed System Energy Balance

The energy concepts introduced thus far are summarized in words as follows:



► Using previously defined symbols, this can be expressed as:  $E_2 - E_1 = Q - W$  (Eq. 2.35a)

Alternatively,  $\Delta KE + \Delta PE + \Delta U = Q - W$  (Eq. 2.35b)

In Eqs. 2.35, a **minus sign** appears **before** *W* because energy transfer by work from the system to the surrounding is taken as positive.

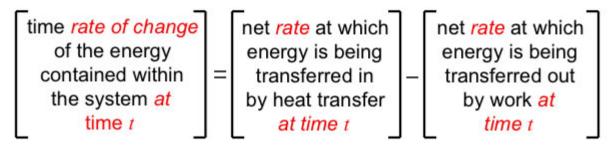
A video game style song of thermodynamics <u>http://www.wiziq.com/tutorial/42567-The-song-of-Thermodynamics</u>

## Summary: Closed System Energy Balance

The time rate form of the closed system energy balance is

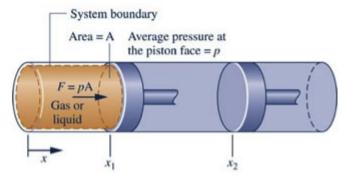
$$\frac{dE}{dt} = \dot{Q} - \dot{W} \qquad (Eq. 2.37)$$

The rate form expressed in words is



A case having many practical applications is a gas (or liquid) undergoing an expansion (or compression) process while confined in a piston-

cylinder assembly.



▶ During the process, the gas exerts a normal force on the piston, F = pA, where *p* is the pressure at the interface between the gas and piston and A is the area of the piston face.

From mechanics, the work done by the gas as the piston face moves from  $x_1$  to  $x_2$  is given by

$$W = \int F dx = \int p A dx$$

Since the product Adx = dV, where V is the volume of the gas, this becomes

$$W = \int_{V_1}^{V_2} p dV$$
 (Eq. 2.17)

► For a compression, *dV* is negative and so is the value of the integral, in keeping with the sign convention for work.

► To perform the integral of Eq. 2.17 requires a relationship between gas pressure at the interface between the gas and piston and the total gas volume.

During an actual expansion of a gas such a relationship may be difficult, or even impossible, to obtain owing to non-equilibrium effects during the process – for example, effects related to combustion in the cylinder of an automobile engine.

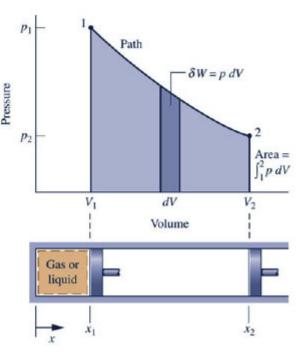
In most such applications, the work value can be obtained only by experiment.

▶ Eq. 2.17 can be applied to evaluate the work of idealized processes during which the pressure p in the integrand is the pressure of the entire quantity of the gas undergoing the process and not only the pressure at the piston face.

For this we imagine the gas undergoes a sequence of equilibrium states during the process. Such an idealized expansion (or compression) is called a *quasiequilibrium* process.

In a quasiequilibrium expansion, the gas moves along a pressure-volume curve, or path, as shown.

► Applying Eq. 2.17, the work done by the gas on the piston is given by the area under the curve of pressure versus volume.



When the pressure-volume relation required by Eq. 2.17 to evaluate work in a quasiequilibrium expansion (or compression) is expressed as an equation, the evaluation of expansion or compression work can be simplified.

An example is a quasiequilibrium process described by  $pV^n = constant$ , where *n* is a constant. This is called a *polytropic process*.

For the case n = 1, pV = constant and Eq. 2.17 gives

 $W = (constant) \ln \left(\frac{V_2}{V_1}\right)$  where  $constant = p_1 V_1 = p_2 V_2$ .

Since non-equilibrium effects are invariably present during actual expansions (and compressions), the work determined with quasiequilibrium modeling can at best approximate the actual work of an expansion (or compression) between given end states.

You will need to analyze the integral of PdV in order to estimate the work associated with volume expansions/compressions.

$$W = \int_{V_1}^{V_2} p \, dV$$

So, for polytropic situations:  $pV^n = constant$ , then

$$W = \int_{V_1}^{V_2} \frac{constant}{V^n} dV = constant \int_{V_1}^{V_2} V^{-n} dV$$

But, most gas situations will use Tables that have combined the Internal Energy (U) with the pV and a thermodynamic term (Enthalpy, H or h) is documented.

That is: H = U + pV

h = u + pv

(more on this when we reach Chapter 3)

Table	e A-4	(Continu	ied)					
T ℃	v m <sup>3</sup> /kg	u kJ/kg	h kJ/kg	s kJ/kg · K	v m <sup>3</sup> /kg	u kJ/kg	h kJ/kg	s kJ/kg · K
		= 5.0 bar	-			= 7.0 ba	-	-
	r		151.86°C)		P		164.97°C)	
Sat.	0.3749	2561.2	2748.7	6.8213	0.2729	2572.5	2763.5	6.7080
180	0.4045	2609.7	2812.0	6.9656	0.2847	2599.8	2799.1	6.7880
200	0.4249	2642.9	2855.4	7.0592	0.2999	2634.8	2844.8	6.8865
240	0.4646	2707.6	2939.9	7.2307	0.3292	2701.8	2932.2	7.0641
280	0.5034	2771.2	3022.9	7.3865	0.3574	2766.9	3017.1	7.2233
320	0.5416	2834.7	3105.6	7.5308	0.3852	2831.3	3100.9	7.3697
360	0.5796	2898.7	3188.4	7.6660	0.4126	2895.8	3184.7	7.5063
400	0.6173	2963.2	3271.9	7.7938	0.4397	2960.9	3268.7	7.6350
440	0.6548	3028.6	3356.0	7.9152	0.4667	3026.6	3353.3	7.7571
500	0.7109	3128.4	3483.9	8.0873	0.5070	3126.8	3481.7	7.9299
600	0.8041	3299.6	3701.7	8.3522	0.5738	3298.5	3700.2	8.1956
700	0.8969	3477.5	3925.9	8.5952	0.6403	3476.6	3924.8	8.4391

## Modes of Heat Transfer

For any particular application, energy transfer by heat can occur by one or more of three modes:

- conduction
- radiation
- convection

## **Thermodynamic Cycles**

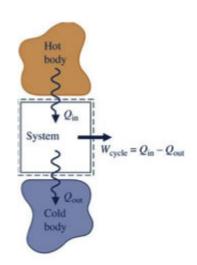
A thermodynamic cycle is a sequence of processes that begins and ends at the same state.

Examples of thermodynamic cycles include

- Power cycles that develop a net energy transfer by work in the form of electricity using an energy input by heat transfer from hot combustion gases.
- Refrigeration cycles that provide cooling for a refrigerated space using an energy input by work in the form of electricity.
- Heat pump cycles that provide heating to a dwelling using an energy input by work in the form of electricity.

A system undergoing a power cycle is shown at right.

► The energy transfers by heat and work shown on the figure are each positive in the direction of the accompanying arrow. This convention is commonly used for analysis of thermodynamic cycles.



W<sub>cycle</sub> is the net energy transfer by work from the system per cycle of operation – in the form of electricity, typically.
 Q<sub>in</sub> is the heat transfer of energy to the system per cycle from the hot body – drawn from hot gases of combustion or solar radiation, for instance.

Q<sub>out</sub> is the heat transfer of energy from the system per cycle to the cold body – discharged to the surrounding atmosphere or nearby lake or river, for example.

Applying the closed system energy balance to each cycle of operation,

$$\Delta E_{\text{cycle}} = Q_{\text{cycle}} - W_{\text{cycle}} \qquad \text{(Eq. 2.39)}$$

Since the system returns to its initial state after each cycle, there is no net change in its energy:  $\Delta E_{cycle} = 0$ , and the energy balance reduces to give

$$W_{\rm cycle} = Q_{\rm in} - Q_{\rm out}$$
 (Eq. 2.41)

In words, the net energy transfer by work from the system equals the net energy transfer by heat to the system, each per cycle of operation.

► The performance of a system undergoing a power cycle is evaluated on an energy basis in terms of the extent to which the energy added by heat,  $Q_{in}$ , is converted to a net work output,  $W_{cycle}$ . This is represented by the ratio

$$\eta = \frac{W_{\text{cycle}}}{Q_{\text{in}}}$$
 (power cycle) (Eq. 2.42)

called the thermal efficiency.

Introducing Eq. 2.41, an alternative form is obtained

$$\eta = \frac{Q_{\text{in}} - Q_{\text{out}}}{Q_{\text{in}}} = 1 - \frac{Q_{\text{out}}}{Q_{\text{in}}} \text{ (power cycle)} \quad \text{(Eq. 2.43)}$$

► Using the second law of thermodynamics (Chapter 5), we will show that the value of thermal efficiency must be less than unity:  $\eta < 1$  (< 100%). That is, only a portion of the energy added by heat,  $Q_{in}$ , can be obtained as work. The remainder,  $Q_{out}$ , is discharged.

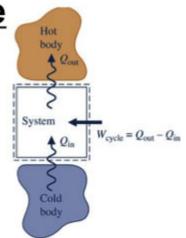
**Example**: A system undergoes a power cycle while receiving 1000 kJ by heat transfer from hot combustion gases at a temperature of 500 K and discharging 600 kJ by heat transfer to the atmosphere at 300 K. Taking the combustion gases and atmosphere as the hot and cold bodies, respectively, determine for the cycle, the net work developed, in kJ, and the thermal efficiency.

Substituting into Eq. 2.41,  $W_{cycle} = 1000 \text{ kJ} - 600 \text{ kJ} = 400 \text{ kJ}$ . Then, with Eq. 2.42,  $\eta = 400 \text{ kJ}/1000 \text{ kJ} = 0.4 (40\%)$ . Note the thermal efficiency is commonly reported on a percent basis.

## **Refrigeration Cycle**

A system undergoing a refrigeration cycle is shown at right.

► As before, the energy transfers are each positive in the direction of the accompanying arrow.



W<sub>cycle</sub> is the net energy transfer by work to the system per cycle of operation, usually in the form of electricity.
 Q<sub>in</sub> is the heat transfer of energy to the system per cycle from the cold body – drawn from a freezer compartment, for example.

 $\triangleright Q_{out}$  is the heat transfer of energy from the system per cycle to the hot body – discharged to the space surrounding the refrigerator, for instance.

## **Refrigeration Cycle**

Since the system returns to its initial state after each cycle, there is no net change in its energy:  $\Delta E_{cycle} = 0$ , and the energy balance reduces to give

$$W_{\rm cycle} = Q_{\rm out} - Q_{\rm in}$$
 (Eq. 2.44)

In words, the net energy transfer by work to the system equals the net energy transfer by heat from the system, each per cycle of operation.

## **Refrigeration Cycle**

► The performance of a system undergoing a refrigeration cycle is evaluated on an energy basis as the ratio of energy drawn from the cold body,  $Q_{in}$ , to the net work required to accomplish this effect,  $W_{cycle}$ :

$$\beta = \frac{Q_{\text{in}}}{W_{\text{cycle}}}$$
 (refrigeration cycle) (Eq. 2.45)

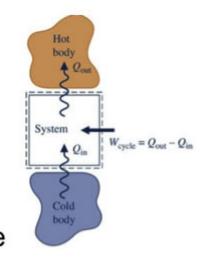
called the coefficient of performance for the refrigeration cycle.

Introducing Eq. 2.44, an alternative form is obtained

$$\beta = \frac{Q_{\text{in}}}{Q_{\text{out}} - Q_{\text{in}}}$$
 (refrigeration cycle) **(Eq. 2.46)**

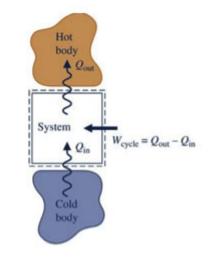
The heat pump cycle analysis closely parallels that given for the refrigeration cycle. The same figure applies:

But now the focus is on Q<sub>out</sub>, which is the heat transfer of energy from the system per cycle to the hot body – such as to the living space of a dwelling.



►  $Q_{in}$  is the heat transfer of energy to the system per cycle from the cold body – drawn from the surrounding atmosphere or the ground, for example.

As before,  $W_{cycle}$  is the net energy transfer by work to the system per cycle, usually provided in the form of electricity.



As for the refrigeration cycle, the energy balance reads

$$W_{\rm cycle} = Q_{\rm out} - Q_{\rm in}$$
 (Eq. 2.44)

► The performance of a system undergoing a heat pump cycle is evaluated on an energy basis as the ratio of energy provided to the hot body,  $Q_{out}$ , to the net work required to accomplish this effect,  $W_{cycle}$ :

$$\gamma = \frac{Q_{\text{out}}}{W_{\text{cycle}}}$$
 (heat pump cycle) (Eq. 2.47)

called the coefficient of performance for the heat pump cycle.

Introducing Eq. 2.44, an alternative form is obtained

$$\gamma = \frac{Q_{\text{out}}}{Q_{\text{out}} - Q_{\text{in}}}$$
 (heat pump cycle) (Eq. 2.48)

**Example**: A system undergoes a heat pump cycle while discharging 900 kJ by heat transfer to a dwelling at 20°C and receiving 600 kJ by heat transfer from the outside air at 5°C. Taking the dwelling and outside air as the hot and cold bodies, respectively, determine for the cycle, the net work input, in kJ, and the coefficient of performance.

Substituting into Eq. 2.44,  $W_{\text{cycle}} = 900 \text{ kJ} - 600 \text{ kJ} = 300 \text{ kJ}$ .

Then, with Eq. 2.47,  $\gamma = 900 \text{ kJ}/300 \text{ kJ} = 3.0$ . Note the coefficient of performance is reported as its numerical value, as calculated here.

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