

USING MATH MODELING TO IDENTIFY AND CORRECT GERRYMANDERING



Background

- Gerrymandering is a political issue that describes the manipulation of electoral borders to work in the favor of, or against, a specific party
- It is deeply undemocratic, but without objective evidence, action cannot be taken against it (Kirschenbaum & Li, 2021)
- There are two types of gerrymandering: packing and cracking
- Packing describes grouping several voters of the same party in one district to ensure that one district wins by a tremendous margin, but the surrounding districts are less competitive (Jones, 2018)
- Cracking also makes districts less competitive, but it does this by splitting a party's voters across several districts, making them a minority in each one (Jones, 2018)
- Section 2 of the Voting Rights Act states that redistricting to intentionally pack or crack minorities is strictly prohibited (Section 2 of the Voting Rights Act, 2015)

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Phrase 1

Existing mathematical redistricting models focus on compactness or geographical factors and do not account for fair representation of minorities, the purpose of the electoral college system.

Phrase 2

The goal of this project is to develop objective measures to identify and correct minority-targeted gerrymandering.

Identification Model

$$\text{Gerrymandering Score} = (\alpha \times \text{EG}) + (\beta \times \text{PVDA}) + (\gamma \times \text{PVDB})$$

$$\text{EG} = \frac{|(\text{Party A's wasted votes} - \text{Party B's wasted votes}) / \text{Total votes}|}{\text{Total districts}}$$

$$\text{PVDA} = \frac{|(\text{Total Party A votes} / \text{Total votes}) - (\text{Districts Party A won} / \text{Total districts})|}{\text{Total districts}}$$

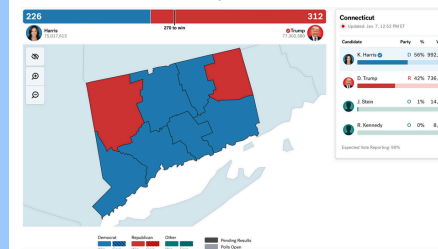
$$\text{PVDB} = \frac{|(\text{Total Party B votes} / \text{Total votes}) - (\text{Districts Party B won} / \text{Total districts})|}{\text{Total districts}}$$

Weights	
α	= 50%
β	= 25%
γ	= 25%

Existing Models

- Many use the efficiency gap, a mathematically accurate measure of the quantity of "wasted votes" (Stephanopoulos & McGhee, 2015)
- Gerrymandering is a combinatorial optimization problem so the solution is usually a rapid randomized algorithm (Chatterjee et al, 2018)
- Several accurate models, but they only account for compactness, preserving old district cores, and geographic symmetry
- They do not consider just representation of minorities

Case Study: Connecticut



Source: <https://abcnews.go.com/Elections/2024-us-presidential-election-results-live-map/>

Design Matrix

	Chatterjee et al's Model	Liu et al's Model	Guest et al's Model	Correction Model
Equal population	✓	✓	✓	✓
Geographic symmetry	✓			✓
Compactness	✓	✓	✓	
Preservation of historic district centers	✓		✓	
Just representation of minorities				✓

Discussion and Conclusion

Next Steps

- Continue developing the Correction Model; consider the addition of other factors
- Consult with experts in the field: Chatterjee, Guest, Liu, etc.
- Develop accessible app or website to view the extent of gerrymandering and how to fix it when given the user's region

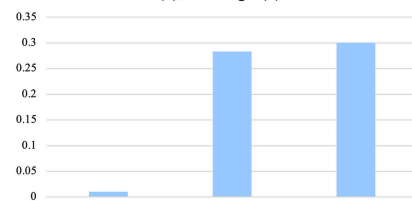
Significance

- Gerrymandering and unfair redistricting has devastating consequences on minority communities
- One of the primary purposes of retaining the archaic electoral system is to counteract the majority rule and provide just representation to minorities
- A mathematical model to identify and correct gerrymandering without human bias could revolutionize the redistricting process
- This research aims to protect the rights of minorities and ensure everyone's fundamental right to vote has an equal impact

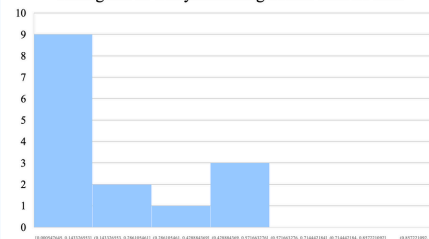
Methodology

- Define the Problem
- Make Assumptions
- Define Variables
- Solve
- Analyze the Solution

Gerrymandering Scores for Low (1), Medium (2), and High (3) Datasets



Histogram of Gerrymandering Scores after 20 runs



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