

## Study Guide 4

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/	Objective 13	The Biot-Savart Law	\
/			\
/	a)	Calculate the contribution made to the magnetic field at a	\
/		specified point by a current element, given the current, location,	\
/		and orientation of the element.	\
/			\
/	b)	Use the Biot-Savart law to calculate the net magnetic field	\
/		produced at a point by a combination of wires containing both	\
/		straight and circular sections.	\
/			\
/	c)	Calculate the magnetic force between two parallel conductors	\
/			\
/	d)	Use the superposition principle to calculate the total magnetic	\
/		field at a point due to a combination of current carrying wires	\
/		and externally applied magnetic fields.	\

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## Suggested Study Procedures

Read Sec. 28-2, paying particular attention to the units and constants which are introduced. Study Sec. 28-3, which is an important application of the Biot-Savart Law. While the mathematics is somewhat complicated, pay attention to the direction of the field at P (in Fig. 28.5) due to the current element, the fact that the distances of the current elements to P change as one moves along the wire, and that the field produced by a very long wire reduces to a simple expression. We will use this result frequently, and later derive it in another way. Study Examples 28-3 and 28-4, in which the superposition principle is used to determine the total magnetic field.

Study Sec. 28-4, in which the force between two current carrying wires is derived. This force is the basis for the definition of the ampere. Study Example 28-5.

## Suggested Problems Related to Objective 13:

Chapter 28: Problems 12, 22, 23, 36, 37, 61, 67, 69, 74, 78

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/	Objective 14	Ampere's Law	\
/			\
/	a)	Describe the meaning of the line integral (sometimes called the circulation) of $B$ around a closed path.	\
/			\
/	b)	Given two or more wires carrying specified current, determine the circulation of $B$ on a given closed path.	\
/			\
/	c)	Use Ampere's Law to determine the magnetic field distribution for wires and coaxial cables having cylindrical symmetry.	\
/			\
/	d)	Know how to calculate the magnetic field of a solenoid and understand its features	\
/			\

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#### Suggested Study Procedures

Study Secs. 28-6 and 28-7. Examples 28-7 and 28-8 use Ampere's Law to derive the magnetic field inside and outside a long straight current-carrying wire. This same type of analysis can also be applied to any problem with circular symmetry. Example 28-9 illustrates another important application of Ampere's law, that of a solenoid.

Suggested Problems Related to Objective 14:

Chapter 28: Problems 42, 45 (also consider  $r < a$ ,  $b < r < c$ ), 46, 49, 51

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/	Objective 15	Magnetic Flux	\
/			\
/	a)	Define magnetic flux	\
/			\
/	b)	Define an area as a vector	\
/			\
/	c)	Calculate the magnetic flux through an area positioned in a magnetic field	\
/			\

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#### Suggested study Procedure

Study Sec. 27-3 and Example 27-2. Review Sec. 22-2 on pages 729-730 to recall how an area can be represented by a vector. Note also that although the definition of flux implies something passing through an area and having a direction, flux is defined explicitly as a scalar quantity. Note that the definition of magnetic flux is similar to our previous definition of electric flux. Look again at Figure 22.6, imagining now that the object is in a uniform magnetic field. Although it is an abstract concept, magnetic flux plays a crucial role in understanding Faraday's law of induction, which in turn is the basis for many practical devices such as electric generators.

### Suggested Problems Related to Objective 15:

Chapter 27: Problems 11, 14

More calculations of flux will be encountered in the problems assigned under Objective 16.

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/               Objective 16   Faraday's Law and Lenz's Law           \
/                                                                 \
/   Given a circuit in a magnetic field where                       \
/                                                                 \
/   a) the B-field changes with time; or                             \
/                                                                 \
/   b) the area of the circuit changes with time, or                 \
/                                                                 \
/   c) the orientation of the circuit in the B-field changes with time; \
/       determine:                                                  \
/                                                                 \
/       i) the flux of the magnetic field intercepted by the circuit at a \
/           specified instant;                                         \
/       ii) the emf induced in the circuit;                          \
/       iii) the current in the circuit (assuming the resistance is known). \
/                                                                 \
/   For the situations above, use Lenz's Law to determine the directions of \
/   the induced currents.                                           \
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### Suggested Study Procedures

Study Secs. 29-1 to 29-3. In this course, we will determine the direction of induced emf mostly using Lenz's law, rather than by the sign convention implicit in Eq. 29.3. We will generally use Eq. 29.3 without the minus sign, for the magnitude of emf, and use Lenz's law to get the direction.

Examples 29-1 and 29-2 involve a magnetic field changing in time, while Examples 29-5 and 29-6 involve a changing area. Similar examples will be discussed in lecture. In each case, make sure that you understand how to determine the induced current direction using Lenz's Law.

Examples 29-3 and 29-4 illustrate an important application of Faraday's law of induction. Electric generators develop an emf because of the changing angle between the area of a loop and the magnetic field. In this case, it is helpful to use the sign convention discussed on p. 962 to determine the induced current direction, rather than Lenz's law.

### Suggested Problems Related to Objective 16:

Chapter 29: Problems 2, 5, 6, 15, 17, 18, 28, 54, 57, 71, 77\*

\*(a challenge)

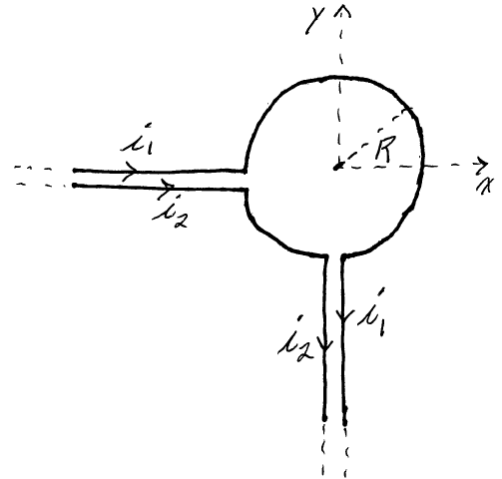
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HOMEWORK ASSIGNMENTS FOR STUDY GUIDE 4

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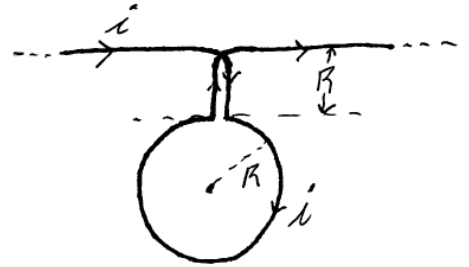
Homework Assignment #13 - due in lecture Friday, April 24

1. Two wires carrying currents  $i_1 = 1.2$  A and  $i_2 = 6$  A are bent as shown into arcs of a circle of radius  $R = 3.2$  cm, with the straight sections heading toward or away from the center of the circle at  $(x=0, y=0)$ . Calculate the contribution of the current element of length  $0.15$  mm at  $(x=R, y=0)$  to the B-field at the following points (express as a vector):



- a)  $x=0, y=0$
- b)  $x=2R, y=0$
- c)  $x=R, y=R$
- d) Determine the total magnetic field (magnitude and direction) at  $(x=0, y=0)$

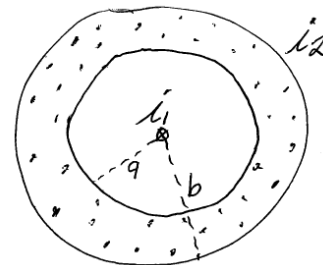
2. A long wire carrying a current  $i = 1.7$  A is bent into straight sections and circular sections of radius  $R = 25$  mm as shown. Determine the magnitude and direction of the magnetic field at the center of the loop. (you can assume that the vertical straight sections are directly over and in line with the center of the circle.)




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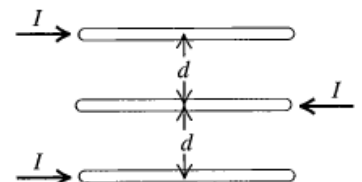
Homework Assignment #14 - due in lecture Monday, April 27

1. A hollow metal pipe of inner radius  $a$  and outer radius  $b$  is carrying current  $i_2$  out of the page, and a thin wire along the axis of the pipe is carrying current  $i_1$  into the page as shown. Determine the magnitude (and sketch the direction) of the magnetic field produced in the regions:



- a)  $r < a$
- b)  $a < r < b$
- c)  $r > b$

2. Three long, parallel wires are oriented in the same plane as shown, carrying currents of the same magnitude  $I$  in the directions indicated. Determine: (a) The magnetic field at the location of each wire due to the currents in the other two, and (b) The force per unit length on each wire.



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**Homework Assignment #15 - due at 5:00 pm Wednesday, April 29**

This assignment is to be submitted via the web. In your web browser, go to [www.masteringphysics.com](http://www.masteringphysics.com). Then login using the username and password you have chosen.

After logging in, click on Assignment List and select Homework #15. If you need any review, you can always do that by repeating Assignment 0, a brief, noncredit tutorial on how to enter answers in Mastering Physics.

In Homework #15, you will get 10 chances to submit a correct answer for each problem. If your first answer is incorrect, you should consider making use of the hints. There is no penalty for opening a hint, and no penalty for giving a wrong answer to a hint. However, if you request an answer to a hint, you will lose some points.

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**Homework Assignment #16 - due at 5:00 pm Friday, May 1**

This assignment is to be submitted via the web. In your web browser, go to [www.masteringphysics.com](http://www.masteringphysics.com). Then login using the username and password you have chosen.

After logging in, click on Assignment List and select Homework #16. If you need any review, you can always do that by repeating Assignment 0, a brief, noncredit tutorial on how to enter answers in Mastering Physics.

In Homework #16, you will get 10 chances to submit a correct answer for each problem. If your first answer is incorrect, you should consider making use of the hints. There is no penalty for opening a hint, and no penalty for giving a wrong answer to a hint. However, if you request an answer to a hint, you will lose some points.