

### SUMMARY HOMEWORK 1

NOTE: This page is similar to the cover sheet you will see on Exam 1. The summary homework problems begin on the next page.

Show ALL work in order to be eligible for full or partial credit. If you require more room, write the extra work on the preceding page ... the page facing the problem statement.

Numerical answers should be expressed to 3 significant digits. Answers should carry units, wherever necessary. Express vectors in **i, j, k** notation or else indicate their magnitude and direction unambiguously. Place your answer in the BOX, where provided.

50 minute duration; CLOSED BOOK, CLOSED NOTES.

Electron charge =  $-1.6 \times 10^{-19} \text{C}$

Electron mass =  $9.1 \times 10^{-31} \text{kg}$

Proton mass =  $1.672 \times 10^{-27} \text{kg}$ , Proton charge =  $1.6 \times 10^{-19} \text{C}$

Coulomb constant  $k = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$

$F_{12} = kq_1q_2/r_{12}^2$  in magnitude

$E = kq/r^2$  in magnitude

**F = qE, F = ma**

$v_x = v_{0x} + a_x t$

$x = x_0 + v_{0x} t + \frac{1}{2} a_x t^2$

$v_x^2 = v_{0x}^2 + 2a_x(x-x_0)$

1

2

3

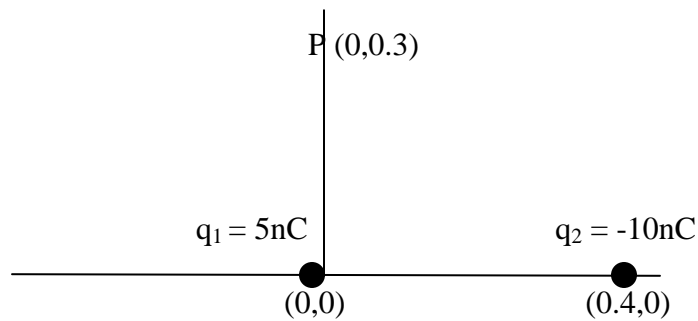
4

Total

**Problems carry the following points:**

**1 = 40, 2 = 40, 3 = 10, 4 = 10**

1. Charge  $q_1 = 5\text{nC}$  is at the origin and charge  $q_2 = -10\text{nC}$  is at the point  $(0.4,0)$ , where all coordinates are in meters (see sketch below). Point P has coordinates  $(0,0.3)$ . ( $1\text{nC} = 10^{-9}\text{C}$ ).



- (a) Calculate the components  $(E_{1x}, E_{1y})$  of the electric field at P due to the charge  $q_1$ .

|            |
|------------|
| $E_{1x} =$ |
| $E_{1y} =$ |

- (b) Calculate the components  $(E_{2x}, E_{2y})$  of the electric field at P due to the charge  $q_2$ .

|            |
|------------|
| $E_{2x} =$ |
| $E_{2y} =$ |

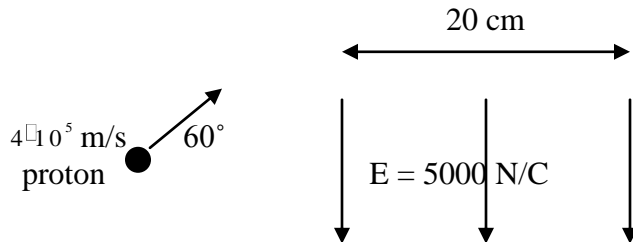
- (c) Calculate the components  $(E_x, E_y)$  of the total electric field at P due to the two charges.

|         |
|---------|
| $E_x =$ |
| $E_y =$ |

- (d) A charge  $q_3 = -10\text{nC}$  is placed at P. Calculate the magnitude and direction of the force experienced by it. Express the direction as a counterclockwise angle measured from the positive x-axis.

|         |
|---------|
| Mag. =  |
| Dirn. = |

2. A proton is fired with a velocity of  $4 \times 10^5$  m/s at an angle of  $60^\circ$  above the horizontal into a region containing a uniform electric field of 5000 N/C pointing vertically downwards, as shown below. The field region extends for a horizontal distance of 20cm. Choose a Cartesian coordinate system with its origin at the initial position of the proton, x-axis pointing to the right and y-axis pointing up, and ignore the effect of gravity in doing this problem.



(a) Calculate the acceleration of the proton in the field.

|                    |
|--------------------|
| $a_x =$<br>$a_y =$ |
|--------------------|

(b) Calculate the time spent by the proton in the field.

|        |
|--------|
| Time = |
|--------|

(c) Calculate the x- and y-components of velocity of the proton when it exits the field.

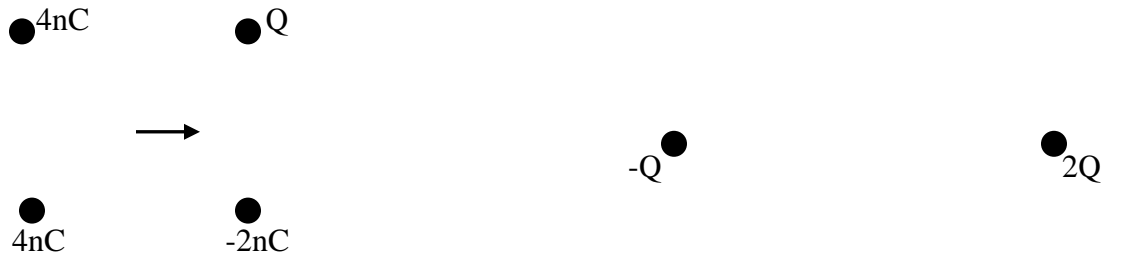
|                    |
|--------------------|
| $v_x =$<br>$v_y =$ |
|--------------------|

(d) Calculate the vertical displacement of the proton relative to its initial position when it exits the field, and state whether it is above or below the initial position.

|                            |
|----------------------------|
| Disp. =<br>Above or below? |
|----------------------------|

No calculations need be shown for any of the questions on this page.

3. (a) The left sketch below shows four point charges at the corners of a square. The electric field at the center of the square points horizontally to the right, as shown. Determine the magnitude and sign of the unknown charge  $Q$ . (5pts)



(b) The figure to the right above shows a positive charge  $2Q$  and a negative charge  $-Q$  a certain distance apart. Draw at least three field lines passing through both charges, and also indicate the arrows on them. (5pts)

4. PART A. Three plastic balls A, B and C are found to have the following properties: A and B strongly attract each other, and B and C neither attract nor repel each other. Ignore any polarization of the balls. Circle all of the following statements that correctly describe the properties of A and C. (5pts)

- (a) A is neutral and C is charged
- (b) A is charged and C is neutral
- (c) A and C repel each other
- (d) A and C attract each other
- (e) A and C neither attract nor repel.

PART B. A metal sphere isolated from its surroundings has some negative charge put on it. Circle all of the following statements that are correct. (5pts)

- (a) The electric field just outside the sphere vanishes
- (b) The electric field just outside the sphere is perpendicular to its surface and points inwards towards the center of the sphere
- (c) The electric field just outside the sphere is perpendicular to its surface and points outwards from the center of the sphere
- (d) The charge distributes itself uniformly throughout the volume of the sphere
- (e) The charge distributes itself uniformly over the surface of the sphere