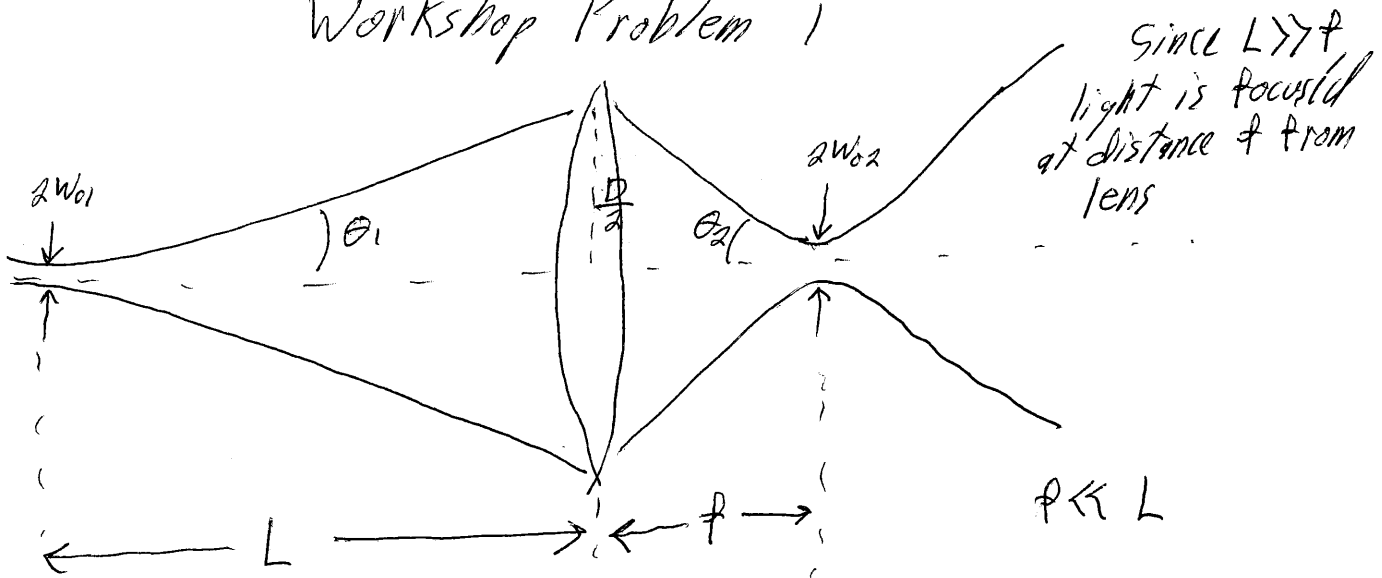


PH 2502 Lasers

Workshop Problem 1



$$a) \theta_1 \approx \frac{\lambda}{\pi W_{01}}, \quad W_{01} = \frac{\lambda}{\pi \theta_1} = \frac{1.064 \cdot 10^{-6} \text{ m}}{\pi (2.5 \cdot 10^{-3})} = 1.35 \cdot 10^{-4} \text{ m} = \boxed{0.135 \text{ mm}}$$

$$b) \theta_1 \approx \frac{D/2}{L}, \quad L \approx \frac{D/2}{2\theta_1} = \frac{1.25 \cdot 10^{-2} \text{ m}}{2(2.5 \cdot 10^{-3})} = \boxed{2.5 \text{ m}} \quad L \gg f$$

$$c) \mathcal{B} = \frac{P}{A_s \Omega} = \frac{15 \text{ W}}{\pi (1.35 \cdot 10^{-4} \text{ m})^2 \pi (2.5 \cdot 10^{-3})^2} = \boxed{1.334 \cdot 10^{13} \frac{\text{W}}{\text{m}^2 \cdot \text{sr}}}$$

$$d) \theta_2 \approx \frac{D/2}{f} = \frac{\lambda}{\pi W_{02}}, \quad W_{02} = \frac{2\lambda f}{\pi D} = \frac{2(1.064 \cdot 10^{-6} \text{ m})(0.025 \text{ m})}{\pi (0.0125 \text{ m})}$$

$$\theta_2 \approx \frac{0.025}{2.5} = 0.01 \text{ rad}, \quad W_{02} = 1.35 \cdot 10^{-6} \text{ m} = \boxed{1.35 \text{ }\mu\text{m}}$$

$$e) I_{\text{peak}} = \frac{2P}{\pi W_{02}^2} = \frac{2(15 \text{ W})}{\pi (1.35 \cdot 10^{-6} \text{ m})^2} = \boxed{5.24 \cdot 10^{12} \frac{\text{W}}{\text{m}^2}}$$

$$f) \mathcal{B} = \frac{15 \text{ W}}{\pi (1.35 \cdot 10^{-6} \text{ m})^2 \pi (0.01)^2} = \boxed{1.334 \cdot 10^{13} \frac{\text{W}}{\text{m}^2 \cdot \text{sr}}}$$

g) Beam radius can increase by at most $\sqrt{2}$ (area doubles) so tolerance is $z = f \pm z_0$

$$W_2 = W_{02} \sqrt{2} \text{ at } z = z_0, \quad z_0 = \frac{\pi W_{02}^2}{\lambda} = \frac{\pi (1.35 \cdot 10^{-6} \text{ m})^2}{1.064 \cdot 10^{-6} \text{ m}} = \boxed{5.4 \cdot 10^{-6} \text{ m}}$$