

Linear Algebra
C Term, Sections C01-C04
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Linear Algebra Assignment 2

DUE DATE: Friday, January 24, 4pm. Submit in class or to mail slot in SH108.

N.B. No late assignments will be accepted for credit.

N.B. Keep in mind Professor Martin's rules for completing assignments (reproduced on the back of this sheet).

Please complete the following four problems:

1. (SIMPLE EXAMPLE OF A LINEAR PROGRAMMING PROBLEM)

(a) The Dixie Chicks Widget company produces three models, P_1 , P_2 and P_3 , of widget in its Worcester manufacturing facility. Each of these is made of steel and plastic. Each unit of P_1 requires two units of steel and three units of plastic. Each unit of P_2 requires two units of steel and one unit of plastic. Each unit of model P_3 requires one unit each of steel and plastic. If, on a particular day, 1800 units of steel and 1500 units of plastic are available for production, determine all possible production schedules which fully utilize the resources.

(b) Suppose now that DCW Co. makes a profit of \$150 on each unit of model P_1 it produces, a profit of \$110 on each unit of P_2 and \$60 on each unit of P_3 . Among the solutions found in part (a), which production schedule will maximize profit? Display your decision in a table, showing how much of each resource will be devoted to each model as well.

2. (a) Find all values of r for which the matrix

$$A = \begin{pmatrix} r & 3 & 3 \\ 3 & r & 3 \\ 3 & 3 & r \end{pmatrix}$$

is singular.

(b) For all other values of r , compute A^{-1} . Show the steps in your row reduction. (HINT: In your answer, r will appear in some entries; i.e., the matrix A^{-1} is a function of r .)

3. Do exercise #27 on page 89.
4. Do problem T.12 on page 65.

PROFESSOR MARTIN'S RULES FOR LINEAR ALGEBRA ASSIGNMENTS:
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- Write neatly, using correct English.
- Use **only one side** of each sheet of paper. Ink on the back of the page deteriorates the readability of what is on the front.
- Explain your steps. A correct answer with no explanation will earn a grade of zero.
- Use a stapler when you submit more than one sheet and want them all back. There is a stapler for public use in the Mathematical Sciences Department Office (SH108).