Proofs in Contemporary Math W. J. Martin March 28, 2009

MA196X Problem Set 2

Instructions: Please first read the rules on the presentation of assignments in the course. Then complete as many of these as you can by Thursday, April 2nd. After that, I will still accept problems until the sample solutions have been distributed.

Note: Always identify each problem by its problem number before stating the problem.

For each of the following five problems, first state the problem precisely and then give a proper proof of the statement using English sentences.

- 7. For all sets A, B and C, if $A \subseteq B$ and $A \subseteq C$, then $A \subseteq B \cap C$.
- 8. For all sets A, B and C, $C (A \cup B) = (C A) \cap (C B)$.
- 9. For all sets A, B and C, if $(A \cap B) \cup C \subseteq A \cap (B \cup C)$, then $C \subseteq A$.
- 10. For all sets A, B and C, (A B) C = A (B C) if and only if $A \cap C = \emptyset$.
- 11. For all sets A, B, C and D, if $A \subseteq C$ and $B \subseteq C \cup D$, then $A \cup B \subseteq C \cup D$.

12. Each of the following statements is false. For each, first write the statement, then write the negation of the statement in English and then provide a counterexample, with a brief explanation.

- (a) For all sets A and B, $A \cup B = (A B) \cup (B A)$.
- (b) For all sets A and B, $A \cap B \neq A B$.
- (c) For all sets A and B, if $A \cup B = A$, then $B = \emptyset$.
- (d) For all sets A, B and $C, A \cap (B \cup C) = (A \cap B) \cup C$.