

Rocket problem Luke Lee

Engine Burn

$$\theta = 44^\circ$$

$$t = 9s$$

$$a = 63 \text{ m/s}^2$$

Find x & y

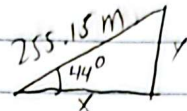
$$V_{xy} = V_0 + at$$

$$V_{xy} = 0 + 6.3 \cdot 9$$

$$V_{xy} = 56.7 \text{ m/s}$$

$$\Delta y_x = \left(\frac{v_0 + v}{2} \right) t$$

$$\Delta y_x = \left(\frac{0 + 56.7}{2} \right) 9 = 255.15 \text{ m}$$



$$\frac{x}{255.15} = \cos(44)$$

$$\frac{y}{255.15} = \sin(44)$$

$$x = 183.5395 \text{ m} \quad y = 177.242 \text{ m}$$

Free fall up

$$\theta = 44^\circ$$

$$V_0 = 56.7 \text{ m/s}$$

$$y_0 = 177.242 \text{ m}$$

$$a = -9.8 \text{ m/s}^2$$

$$V_y = 0$$

$$x_0 = 183.5395$$

Find: x & y

$$\Delta x = V_x t$$

$$\Delta x = 56.7 \cos 44^\circ t$$

$$\Delta x = 56.7 \cos(44) 4.01913$$

$$\Delta x = 163.9265137 \text{ m}$$

$$\text{total } x = x + x_0 =$$

$$347.4660637 \text{ m}$$

Y

$$V_y^2 = V_{0y}^2 + 2a\Delta y$$

$$0 = (56.7 \sin 44^\circ)^2 + 2(-9.8)\Delta y$$

$$19.6\Delta y = 1551.245979$$

$$\Delta y = 79.150305 \text{ m}$$

$$\Delta y = y + y_0 = 256.392405 \text{ m}$$

$$y = y_0 + V_{0y} t - \frac{1}{2} g t^2 \quad \text{Assume } y = 0$$

$$79.150305 = 0 + (56.7 \sin 44^\circ) t - 4.9 t^2$$

$$0 = -4.9 t^2 + 39.3871296 t - 79.150305$$

$$t = 4.01913 \text{ s}$$

Free fall down

$$\theta = 0^\circ$$

$$V_0 = 56.7 \text{ m/s}$$

$$y_0 = 256.392405 \text{ m}$$

$$a = -9.8 \text{ m/s}^2$$

$$V_{y0} = 0$$

$$x_0 = 347.4660637 \text{ m}$$

$$y = 256.392405 - 80$$

Find x

$$\Delta x = V_x t$$

$$\Delta x = 56.7 (\cos(44^\circ)) t$$

$$\Delta x = 56.7 \cos(44) 4.040610178$$

$$\Delta x = 164.802665 \text{ m}$$

Y

$$y = y_0 + V_{0y} t - \frac{1}{2} g t^2$$

$$176.392405 = 256.392405 + 0 - 4.9 t^2$$

$$-80 = -4.9 t^2$$

$$t = 4.040610178 \text{ s}$$

parachute

$$V_y = -6 \text{ m/s}$$

$$V_x = -15 \text{ m/s}$$

$$Y_0 = 176.392405$$

Find X

X

$$\Delta x = V_x t$$

$$\Delta x = -15t$$

$$\Delta x = (-15)(29.39873417)$$

$$\Delta x = -440.9810125 \text{ m}$$

Y

$$Y = Y_0 + V_{0y}t - \frac{1}{2}gt$$

$$0 = 176.392405 - 6t - 0$$

$$6t = 176.392405$$

$$t = 29.39873417 \text{ s}$$

Putting it all together

Engine burn variables: $X_1 = 183.53953 \text{ m}$, $Y_1 = 177.242 \text{ m}$, $a_1 = 53 \text{ m/s}^2$

$V_{x1} = 40.787 \text{ m/s}$, $V_{y1} = 39.387 \text{ m/s}$, $V_{xy} = 56.7 \text{ m/s}$, $t_1 = 9 \text{ s}$, $\theta = 44^\circ$

Free fall up: $X_2 = 163.9265137 \text{ m}$, $Y_2 = 79.150305 \text{ m}$

$$a_2 = -9.8 \text{ m/s}^2$$

$$t_2 = 4.01913 \text{ s}$$

Free fall down: $X_3 = 164.8026165 \text{ m}$, $Y_3 = -80 \text{ m}$, $t_3 = 4.0466102 \text{ s}$

parachute: $X_4 = -440.9810125 \text{ m}$, $Y_4 = -176.392405$, $t_4 = 29.39873417 \text{ s}$

$$V_{y2} = -6 \text{ m/s}$$

$$V_{x2} = -15 \text{ m/s}$$

Total X: $X_1 + X_2 + X_3 + X_4 \approx 1$

$$\text{Total X} = 183.5395 + 163.9265 + 164.8026 - 440.9810 = 71.2877 \text{ m East}$$

