

0 Table of contents 0 X Introduction Assumptions - I Background and overall Assumptions we made using problem the information given Solution Conclusion Steps we took to solve Strengths, weaknesses, the problem and justification.

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Problem Statement

Don't forget

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The dropout rate is 5%.

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The Epsilon School of Mathematics and Science is increasing in size from 490 students to 630 students. Because of this increase, they need to hire 7 new teachers and allocate them across the departments fairly.

Assumptions

- 1. Fair means having the same number of class sections per teacher per day.
- 2. Each student takes 1 English Class per year. This gives us the number of students per grade.
- 3. Students drop out after 11th grade but before 12th grade.
- 4. Teachers teach all grades.

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- 5. Students in different grades can be in the same class at the same time.
- 6. All subjects run the same number of sections per day (eg. 5 English
 - classes per day, 5 math classes per day, 5 music classes per day).
 - All classes are approximately the same size (+/- 20 students).
- 8. Language teachers teach all languages and the department is combined.

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Initial Variables And Hypothesis

The first few "variables" we used were:

- # of teachers in each department
- Class sizes (# of students per class)
- Graduating class size
- Percent that dropped out
- # of new students

Hypothesis:

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Before creating the model, we hypothesized that out of the 9 departments, we would add a single new teacher to the 7 departments with the greatest number of classes per teacher.



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Problem is sking how to hire faculty	````	What does the current ratio between teachers and students look like?		Many grades have class requirements, so distribution of students should be similar	, ,	What departments would be the most strained w/ current faculty?		Add faculty to these departments	
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Model Design

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For our model, we decided to find ratios of students in each grade and in each department and use that to determine how many classes each teacher must teach. Then, this information can be used to determine what departments need more support.

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Current # of students per grade

Part 1

10th grade: 183

11th grade: 155

12th grade: 152

Total number of students in school: 490

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Initial Calculations

Jncoming class = graduating class + increase in school size

New graduating class = (2nd to last grade) x (percent remaining after dropout)

Part 2

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Relative Frequency

Relative frequency of department of grade = # of students in department in grade / # of students in grade

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Relative Frequency Table (2024)

Example calculation

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Relative frequency of 10th grade art = 31/183 = 0.16939891

| Class          | 10th Grade | 11th Grade | 12th Grade |
|----------------|------------|------------|------------|
| Art            | 0.16939891 | 0.2129032  | 0.2302632  |
| Biology        | 1.08196721 | 0.6129032  | 0.1710526  |
| Chemistry      | 0.27868852 | 0.8129032  | 0.7171053  |
| English        | 1          | 1          | 1          |
| All Lang       | 0.60655738 | 0.516129   | 0.6052632  |
| Math           | 1.00546448 | 1.2967742  | 1.7236842  |
| Music          | 0.27322404 | 0.3612903  | 0.3223684  |
| Physics        | 0.27322404 | 0.3741935  | 1.2039474  |
| Social Studies | 0.98360656 | 0.8451613  | 0.3881579  |

Next Year Predictions

Predicted # of students in department in grade = (relative frequency of department of grade) x (# of students in grade)

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Example calculation

Predicted # of 10th grade art students = 0.16939891 x 292

Part 3

| Predicted Num Students per class (2025) | Class          | 10th Grade | 11th Grade | 12th Grade | т |
|-----------------------------------------|----------------|------------|------------|------------|---|
|                                         | Art            | 49.4644809 | 38.96129   | 33.90625   |   |
|                                         | Biology        | 315.934426 | 178.96774  | 25.1875    |   |
|                                         | Chemistry      | 81.3770492 | 148.76129  | 105.59375  |   |
|                                         | English        | 292        | 183        | 147.25     |   |
|                                         | All Lang       | 177.114754 | 94.451613  | 89.125     |   |
|                                         | Math           | 293.595628 | 237.30968  | 253.8125   |   |
|                                         | Music          | 79.7814208 | 66.116129  | 47.46875   |   |
|                                         | Physics        | 79.7814208 | 68.477419  | 177.28125  |   |
|                                         | Social Studies | 287.213115 | 154.66452  | 57.15625   |   |
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Part 4



Department Numbers

New

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Example Calculation

Art: 49.46448087 10th grade students + 38.96129032 11th grade students + 33.90625 12th grade students = 122.3320212 art students

| Predicted Num Students per class (2025 | Class          | 10th Grade | 11th Grade                                                                                                                                                                                                                                                                       | 12th Grade                                                                                                                                                                                                                                                                                                                                                                                                                | Total                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                             |
|----------------------------------------|----------------|------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|                                        | Art            | 49.4644809 | 38.96129                                                                                                                                                                                                                                                                         | 33.90625                                                                                                                                                                                                                                                                                                                                                                                                                  | 122.3320212                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                             |
|                                        | Biology        | 315.934426 | 178.96774                                                                                                                                                                                                                                                                        | 25.1875                                                                                                                                                                                                                                                                                                                                                                                                                   | 520.0896682                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                             |
|                                        | Chemistry      | 81.3770492 | 148.76129                                                                                                                                                                                                                                                                        | 105.59375                                                                                                                                                                                                                                                                                                                                                                                                                 | 335.7320895                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                             |
|                                        | English        | 292        | 183                                                                                                                                                                                                                                                                              | 147.25                                                                                                                                                                                                                                                                                                                                                                                                                    | 622.25                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                             |
|                                        | All Lang       | 177.114754 | 94.451613                                                                                                                                                                                                                                                                        | 89.125                                                                                                                                                                                                                                                                                                                                                                                                                    | 360.691367                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                                                                                                                                                                                                                                                                                                                                             |
|                                        | Math           | 293.595628 | 237.30968                                                                                                                                                                                                                                                                        | 253.8 <mark>1</mark> 25                                                                                                                                                                                                                                                                                                                                                                                                   | 784.7178058                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                             |
|                                        | Music          | 79.7814208 | 66.116129                                                                                                                                                                                                                                                                        | 47.46875                                                                                                                                                                                                                                                                                                                                                                                                                  | 193.3662998                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                             |
|                                        | Physics        | 79.7814208 | 68.477419                                                                                                                                                                                                                                                                        | 177.28125                                                                                                                                                                                                                                                                                                                                                                                                                 | 325.5400901                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                             |
|                                        | Social Studies | 287.213115 | 154.66452                                                                                                                                                                                                                                                                        | 57.15625                                                                                                                                                                                                                                                                                                                                                                                                                  | 499.0338809                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                             |
|                                        |                |            | Art         49.4644809           Biology         315.934426           Chemistry         81.3770492           English         292           All Lang         177.114754           Math         293.595628           Music         79.7814208           Physics         79.7814208 | Art         49.4644809         38.96129           Biology         315.934426         178.96774           Chemistry         81.3770492         148.76129           English         292         183           All Lang         177.114754         94.451613           Math         293.595628         237.30968           Music         79.7814208         66.116129           Physics         79.7814208         68.477419 | Art         49.4644809         38.96129         33.90625           Biology         315.934426         178.96774         25.1875           Chemistry         81.3770492         148.76129         105.59375           English         292         183         147.25           All Lang         177.114754         94.451613         89.125           Math         293.595628         237.30968         253.8125           Music         79.7814208         66.116129         47.46875           Physics         79.7814208         68.477419         177.28125 | Art49.464480938.9612933.90625122.3320212Biology315.934426178.9677425.1875520.0896682Chemistry81.3770492148.76129105.59375335.7320895English292183147.25622.25All Lang177.11475494.45161389.125360.691367Math293.595628237.30968253.8125784.7178058Music79.781420866.11612947.46875193.3662998Physics79.781420866.477419177.28125325.5400901 |

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Part 5



ratio

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Student to teacher ratio per department = new # of students in department / # of teachers in department

| Data from excel | 1 |
|-----------------|---|
|-----------------|---|

| Class          | Student to teacher ratio |
|----------------|--------------------------|
| Art            | 122.3320212              |
| Biology        | 130.022417               |
| Chemistry      | 111.9106965              |
| English        | 124.45                   |
| All Lang       | 120.2304557              |
| Math           | 130.786301               |
| Music          | 193.3662998              |
| Physics        | 108.5133634              |
| Social Studies | 99.80677618              |

Part 6

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# of class sections

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# of class sections
needed to run
department wide per
school day = new # of
students in department
/ class size

*Example* # of class sections needed to run in art

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department = 122.3320212 / 20

Data from excel

| 01             |                                                  |
|----------------|--------------------------------------------------|
| Class          | Class sections needed (divide by class size: 20) |
| Art            | 6.11660106                                       |
| Biology        | 26.00448341                                      |
| Chemistry      | 16.78660448                                      |
| English        | 31.1125                                          |
| All Lang       | 18.03456835                                      |
| Math           | 39.23589029                                      |
| Music          | 9.66831499                                       |
| Physics        | 16.27700451                                      |
| Social Studies | 24.95169404                                      |
| 1              |                                                  |

## $\rightarrow$ Classes per teacher

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# of classes per teacher per
 department = # of class
 sections department-wide /
# of teachers in department

Example Calculation:

Part f

**# of classes per art teacher =** 6.11660106/1 = 6.11660106

| Class sections needed (divide by class size: 20) | Number of classes each teacher has (divide by num of teachers) |
|--------------------------------------------------|----------------------------------------------------------------|
| 6.11660106                                       | 6.11660106                                                     |
| 26.00448341                                      | 6.501120852                                                    |
| 16.78660448                                      | 5.595534825                                                    |
| 31.1125                                          | 6.2225                                                         |
| 18.03456835                                      | 6.011522783                                                    |
| 39.23589029                                      | 6.539315049                                                    |
| 9.66831499                                       | 9.66831499                                                     |
| 16.27700451                                      | 5.425668169                                                    |
| 24.95169404                                      | 4.990338809                                                    |

Part 8



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## How we decided to increase teachers

We chose to add teachers to the departments with the highest number of classes. We checked how that affected the outcome, and adjusted our solution accordingly.

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# of classes per teacher
 per department = # of
class sections department wide / # of teachers in
 department (increased)

New Classes per teacher

| New # of classes each teacher has |             |
|-----------------------------------|-------------|
|                                   | 6.11660106  |
|                                   | 5.200896682 |
|                                   | 4.196651119 |
|                                   | 5.185416667 |
|                                   | 4.508642088 |
|                                   | 4.904486286 |
|                                   | 4.834157495 |
|                                   | 5.425668169 |
|                                   | 4.990338809 |
|                                   |             |

Solution

We added the following numbers of teachers to each department:

- 1 to Biology
- 1 to Chemistry
- 1 to English
- 1 to Foreign Languages
- 2 to Mathematics
- 1 to Music

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We believe that our model fairly distributes the new teachers because the departments with the most students per teacher now have similar ratios as other departments, and no teacher will have drastically more students than any other.



Strengths and Weaknesse's



Strengths

-schools often require similar classes every year, model predicted off of distribution

-model allocates teachers evenly (our definition of fair)

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Weaknesses

-model is based on previous numbers

-students might drop out sophomore year too

-model isn't currently applicable to every situation



