

### Exercises: Stirling's Formula

$$n! \sim (n/e)^n \sqrt{2\pi n}, \quad \lim_{n \rightarrow \infty} \frac{n!}{(n/e)^n \sqrt{2\pi n}} = 1$$

1. Use Stirling's formula to estimate  $2 \cdot 4 \cdot 6 \cdots 2n$ .
2. Use Stirling's formula to estimate  $1 \cdot 3 \cdot 5 \cdots (2n-1)$ .
3. Use the previous two exercises to compute

$$\lim_{n \rightarrow \infty} \frac{1 \cdot 3 \cdot 5 \cdots (2n-1)}{2 \cdot 4 \cdot 6 \cdots 2n}$$

4. Show that

$$\binom{3n}{n} \sim \frac{(27/4)^n \sqrt{3}}{2\sqrt{\pi n}}$$

5. Show that  $(1 + 1/n) \sim 1$ . Apply it to  $(1 + 1/n)^n$ . Is there a problem?