

Steps:

1. Find position when acceleration stops
2. Use sin and cos to find Δx and Δy in first stage
3. Find velocity, v_x , and v_y when acceleration stops
4. Find max height and how long it takes to get there
5. Use time to max height and v_x to find Δx between end of acceleration and max height
6. Find time for y to decrease by 60m from max height
7. Use time from 6 to find Δx using v_x from max height to parachute
8. Find time using v_y to hit the ground
9. Use time and v_x given to calculate Δx in final stage
10. Add the 4 Δx values calculated to get the final position

Launch Angle = 41°

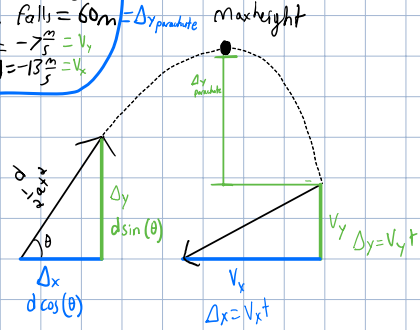
Engine burn time = $7.3s = t$

Acceleration while rocket burns = $6.2 \frac{m}{s^2} = a$

Vertical fall before parachute falls = $60m = \Delta y_{parachute}$ Max height

Parachute constant vertical speed = $-7 \frac{m}{s} = v_y$

Parachute constant horizontal speed = $-13 \frac{m}{s} = v_x$



Stage 1

Given:

$t = 7.3s$
 $a = 6.2 \frac{m}{s^2}$

$d = \frac{1}{2} a t^2$

$d = \frac{1}{2} (6.2 \frac{m}{s^2}) (7.3s)^2$

$d = 165.199$

$\Delta x = 165.199 \cos(41^\circ) = 124.68$
 $\Delta y = 165.199 \sin(41^\circ) = 108.38m$

$v_f^2 = v_i^2 + 2ad$

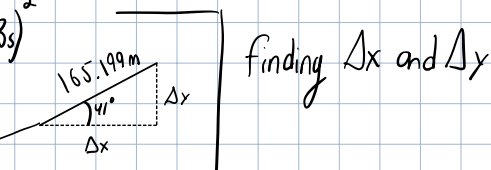
$v_f^2 = 2ad$

$v_f^2 = 2(6.2)(165.199)$

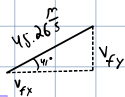
$v_f = 45.26 \frac{m}{s}$

$v_{fx} = 45.26 \cos(41^\circ) = 34.16 \frac{m}{s}$

$v_{fy} = 45.26 \sin(41^\circ) = 29.69 \frac{m}{s}$



finding Δx and Δy



finding final velocities Stage 1

Stage 2

Given:

$v_{0x} = 34.16 \frac{m}{s}$

$v_{0y} = 29.69 \frac{m}{s}$

$v_f^2 = v_i^2 + 2a\Delta y$

$-v_i^2 = 2a\Delta y$

$\frac{-v_i^2}{2a} = \Delta y$

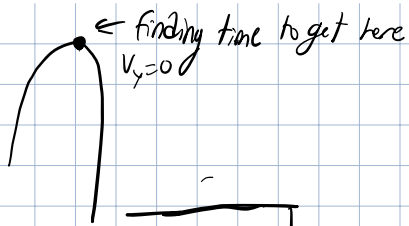
$\frac{-(29.69 \frac{m}{s})^2}{-19.6 \frac{m}{s^2}} = \Delta y$

$\Delta y = 44.97m$

$\Delta y_{stage 2} + \Delta y_{stage 1} = y_{max}$

$124.68m + 44.97m = 153.35 = y_{max}$

Finding Max Height



$$v_y = v_{oy} + at$$

$$\frac{-v_{oy}}{a} = \frac{at}{a} \quad \frac{-v_{oy}}{a} = t$$

$$\frac{-29.69 \frac{m}{s}}{-9.8} = t = 3.030s$$

Time to get to max height

$$v_x = 34.16 \frac{m}{s}$$

Δx from end of stage 1 to max height

$$\Delta x_1 = 34.16 \frac{m}{s} (3.030s)$$

$$\Delta x_1 = 103.5m$$

$$\Delta x = v_{ox}t + \frac{1}{2}at^2$$

$$\Delta y = -60m$$

$$\Delta y = \frac{1}{2}at^2$$

Δx from max height to end stage 2

$$\frac{2\Delta y}{a} = t^2 \quad t = \sqrt{\frac{2\Delta y}{a}} \quad t = \sqrt{\frac{2(-60)}{-9.8}} \quad t = 3.497s$$

$$\Delta x_2 = v_x t \quad \Delta x_2 = 34.16 \frac{m}{s} (3.497s) = 119.4m$$

$$\Delta x_1 + \Delta x_2 = 222.9m \text{ in stage 2}$$

Stage 2

$$103.5m + 119.4m = 222.9m$$

Δx

Stage 3

$$v_y = 7 \frac{m}{s}$$

$$v_x = 13 \frac{m}{s}$$

$$\Delta y = v_y t$$

$$\Delta y = y_{max} - 60$$

$$t = \frac{\Delta y}{v_y}$$

$$\Delta y = 93.35m$$

$$t = \frac{93.35m}{7 \frac{m}{s}} = 13.34s$$

Solving for time on stage 3

$$\Delta x = v_x t$$

$$\Delta x = 13(13.34s)$$

$$\Delta x = 173.42m$$

backwards

Δx Stage 3

$$\Delta x_{\text{Stage 1}} + \Delta x_{\text{Stage 2}} + \Delta x_{\text{Stage 3}}$$

$$108.38 + 222.9 - 173.42$$

$$x_{\text{Final}} = 157.86m$$

Δx altogether