

# Epsilon School

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# Overview

## Problem Background:

- Problem statement
- Variables
- Assumptions

## Solution Process:

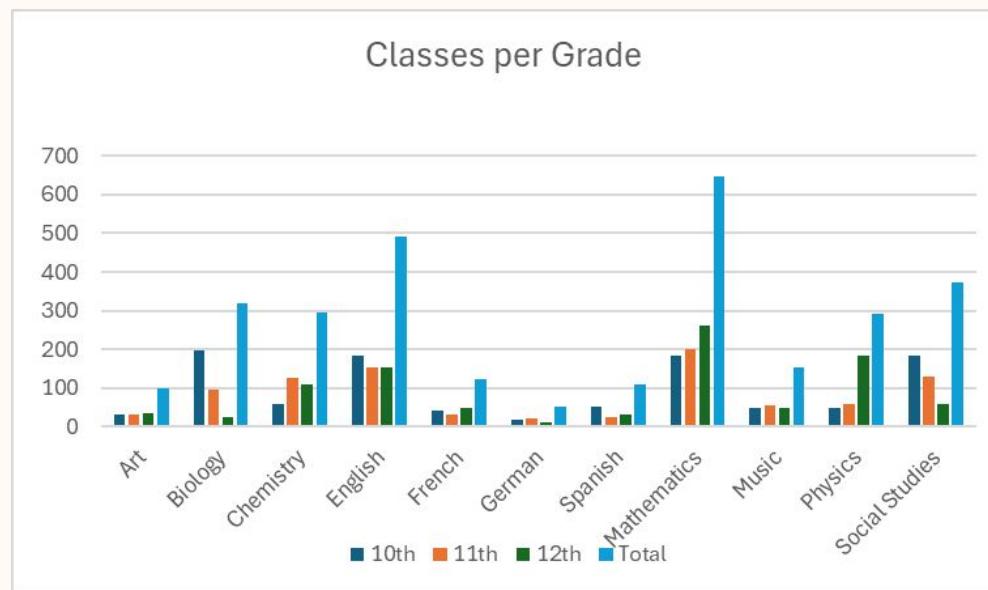
- Finding size of classes
- Predicting number of classes being taken for the incoming class
- Finding current student-teacher ratios
- Allocating teachers for new student-teacher ratios
- Conclusions

# Understanding the problem

- Central Question: What classes should receive an extra teacher (or multiple) given the larger incoming grade?
- Givens:
  - 7 new teachers
  - 140 new students in the sophomore class (referred to as “incoming”) compared to the graduating senior class
- What to consider:
  - Number of students taking a class→predicted number of classes taken next year
  - Student to teacher ratio→compare new to old
  - Where should new teachers be allocated based off new student-teacher ratios?

# Current Student Distribution

- Total classes are taken by students in each subject
- Shows what classes Sophomores are likely to take.
- Shows classes of greater importance.
- Found that each student takes approximately 6 classes (6.022 each)



# Assumptions and Variables

## Assumptions:

- There are 6 periods in every day. Each class is 1 period long.
- Each student takes 1 class per period.
- Each teacher teaches 1 class every period.
- Advancing grades have the exact same spread of classes as the previous class of that year
- Current student : teacher ratio in classes is working for the school

## Variables:

- Student Population per Grade
- Amount of classes taken per grade
- Old Student-Teacher Ratio
- New Student-Teacher Ratio
- New # of teachers in each class

# Student count

## Student Count

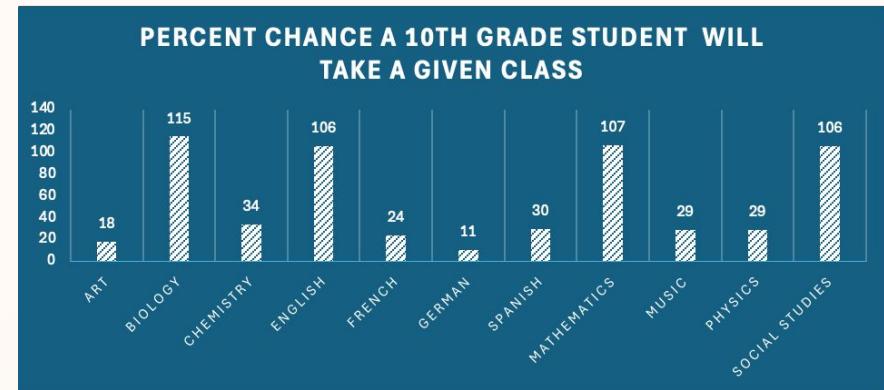
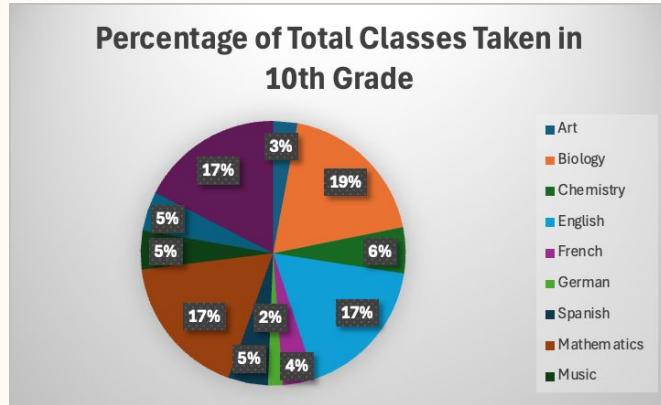
- Decrease of 5% every year (Geometric series)
- Incoming: # of seniors + 140
- Sophomores: X, Juniors:  $0.95X$  and Seniors:  $0.95^2X$
- Total number of students (sophomore – senior): 490

| By Year    | # of Students |
|------------|---------------|
| Incoming   | 295           |
| Sophomores | 172           |
| Juniors    | 163           |
| Seniors    | 155           |

## Class Count

- Simply the total number of classes that each grade is taking
- The classes that majority of sophomores take will increase by more

# Percentage of Sophomores



-Focus on sophomore year increase of students

Left graph:  $-\%$  of total classes taken = **# of classes taken** in subject by 10th graders / **total # of classes** taken by 10th graders

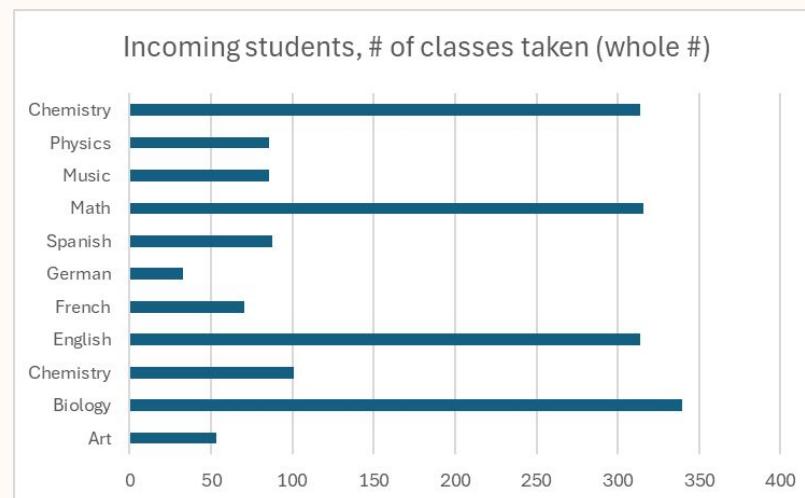
- % of each class taken will be same for current 10th graders + incoming students (just with more students)

Right graph:  $-\%$  of total classes taken = **# of classes taken by 10th graders (in subject)** / **total # of students in grade 10**.

- Percentages above 100: students are (on average) taking more than one class in that subject

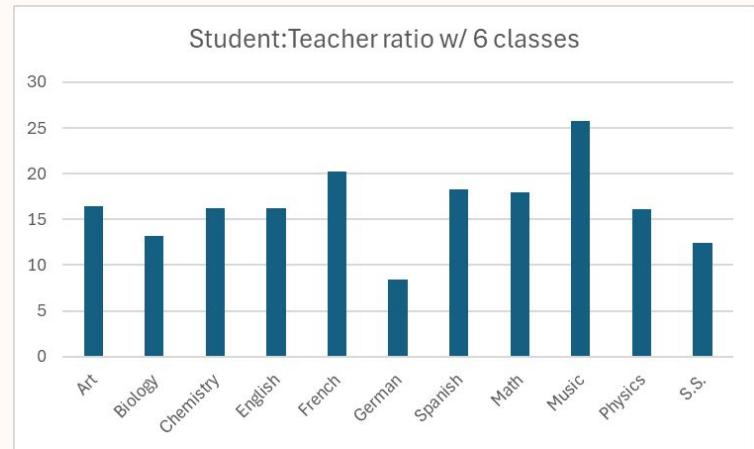
# New student classes

- Using our percentages from before we took that percentage and multiplied it by the size of the new sophomore class.
- This allowed us to get the total amount of student predicted to take a certain class next year
- We found that each class had a 171.5% increase from last year



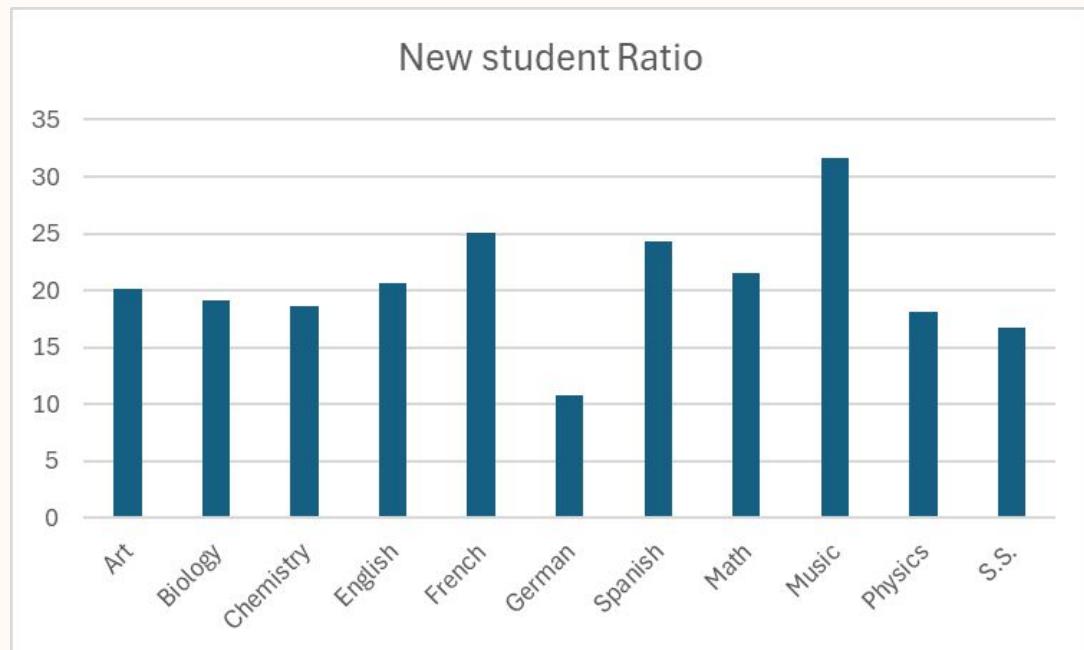
# Old Student Ratios

- We wanted to find the current student to teacher ratio
- See which teachers were having to teach the most and needed help
- We took the total number of classes and divided that by how many classes each student can take (~6.022), then divided it by number of teachers



# New Student Ratios

Using our new size of our sophomore class, we re-calculated our ratio



# Desired Student Ratios

## Wanted Ratio

Assumption: old class sizes were working for the school

Goal: all the ratios to be similar or better (less student : teacher) than the old ratios

Measuring: we can measure the success by subtracting the new student : teacher ratio from the old student : teacher ratio

Results: Statistic from measuring: negative is bad (increased student : teacher ratio - red), positive is good (decreased student : teacher ratio - green)

Additional Factors:

- Teacher teaches >10 students/class and <20 students/class (not fair to teachers)

# Factors for choosing teachers

## Factors

- Wanted all teacher to teach less than 20 kids per class
- No teachers should be teaching less than 10 students per class
- No outliers (10 student range)

# Ratio Analysis

| Our Solution | Old Student:Teacher Ratio | New Student:Teacher Ratio | New proposed teachers | New Ratio with Extra Teachers | Old ratio-new ratio |
|--------------|---------------------------|---------------------------|-----------------------|-------------------------------|---------------------|
| Art          | 16.44                     | 20.12                     | 1                     | 10.06                         | 6.38                |
| Biology      | 13.24                     | 19.12                     | 1                     | 15.30                         | -2.05               |
| Chemistry    | 16.27                     | 18.61                     |                       | 18.61                         | -2.34               |
| English      | 16.27                     | 20.62                     | 1                     | 17.18                         | -0.91               |
| French       | 20.26                     | 25.13                     | 0.5                   | 16.75                         | 3.51                |
| German       | 8.47                      | 10.72                     |                       | 10.72                         | -2.26               |
| Spanish      | 18.26                     | 24.32                     | 0.5                   | 16.21                         | 2.05                |
| Math         | 17.91                     | 21.55                     | 1                     | 18.47                         | -0.56               |
| Music        | 25.74                     | 31.67                     | 1                     | 15.84                         | 9.90                |
| Physics      | 16.11                     | 18.09                     |                       | 18.09                         | -1.98               |
| S.S.         | 12.39                     | 16.73                     | 1                     | 13.94                         | -1.56               |

We looked at the new student ration and saw that 6 teachers had over a 20 ratio.

We added one teacher to those classes and then got new ratio that were all under 20

We also made sure that there wasn't too big of a difference between the old ratio and new ratio

# Justification of our model

- All teachers now have classes with similar sizes to the old ratio.
- All teachers have a ratio around 10–20.
- Incorporates all existing teachers (nobody is fired)
- Doesn't force any teachers to teach more than 3 kids / class than before (red data)
- Low negative total of classes with increasing class size (Total Neg)

| Our Solution | Old Student:Teacher Ratio | New Student:Teacher Ratio | New proposed teachers | New Ratio with Extra Teachers | Old ratio-new ratio |
|--------------|---------------------------|---------------------------|-----------------------|-------------------------------|---------------------|
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| Music        | 25.74                     | 31.67                     | 1                     | 15.84                         | 9.90                |
| Physics      | 16.11                     | 18.09                     |                       | 18.09                         | -1.98               |
| S.S.         | 12.39                     | 16.73                     | 1                     | 13.94                         | -1.56               |
|              |                           |                           |                       |                               | Total Neg: -11.65   |

$$11.65/7=1.66 \text{ avg. extra students in neg classes}$$

| Alternative Setup: | New Student:Teacher Ratio | New proposed teachers                        | New Ratio with Extra Teachers | Old ratio-new ratio |
|--------------------|---------------------------|--|-------------------------------|---------------------|
| Art                | 20.12                     |  | 20.12                         | -3.68               |
| Biology            | 19.12                     | 2  | 12.75                         | 0.50                |
| Chemistry          | 18.61                     | 1  | 13.96                         | 2.32                |
| English            | 20.62                     | 2  | 14.73                         | 1.55                |
| French             | 25.13                     |  | 29.28                         | -9.02               |
| German             | 10.72                     | -1   | 0.00                          | 0.00                |
| Spanish            | 24.32                     |  | 28.64                         | -10.37              |
| Math               | 21.55                     | 2  | 16.16                         | 1.75                |
| Music              | 31.67                     |  | 31.67                         | -5.94               |
| Physics            | 18.09                     | 1  | 13.56                         | 2.54                |
| S.S.               | 16.73                     |  | 16.73                         | -4.35               |
|                    |                           | (Fire German Teacher)                        |                               | Total Neg: -33.36   |
|                    |                           | Add teachers to major classes                |                               |                     |
|                    |                           | German students split between french/spanish |                               |                     |

$$33.36/5=6.67 \text{ avg. extra students in neg classes}$$



# Our Solution

|                | Art | Bio | Chem | English | French | German | Spanish | Math | Music | Physics | Social Studies |
|----------------|-----|-----|------|---------|--------|--------|---------|------|-------|---------|----------------|
| Teachers Added | 1   | 1   | 0    | 1       | 0.5    | 0      | 0.5     | 1    | 1     | 0       | 1              |

# Strengths and Weaknesses

## Strengths

- Matches the old ratios well
- Easy to change data if more teachers can be added
- We have no outlier teacher ratios

## Weaknesses

- The assumptions have to hold true
- We didn't factor in a prep class for teacher
- We assume that all classes (within each subject) are the same size

# Thank You

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