

exercise 1:

9.2.2

exercise 2:

9.2.5

exercise 3:

11.4.2

exercise 4:

11.6.3

exercise 5:

11.6.4

exercise 6:

Let e_1, \dots, e_n be the natural basis of K^n . Let a_0, \dots, a_{n-1} be n scalars in K and M in $K^{n \times n}$ such that $Me_j = e_{j+1}$, if $j = 1, \dots, n-1$ and

$$Me_n = -a_0e_1 - a_1e_2 \dots - a_{n-1}e_n.$$

- (i). Write down the matrix M .
- (ii). Find M^je_1 for $j = 0, \dots, n$.
- (iii). Find the characteristic polynomial of M .

exercise 7:

Let V be a vector space and W, W_1, W_2, \dots, W_p be subspaces. Assume that $V = W_1 \oplus W$ and $W = W_2 \oplus \dots \oplus W_p$.
Show that $V = W_1 \oplus W_2 \oplus \dots \oplus W_p$.

exercise 8:

11.6.1. Additional question: are D and N unique?