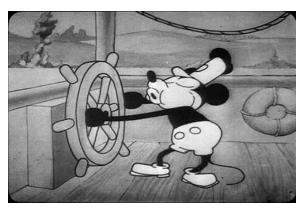
WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

STRESS ANALYSIS ES-2502, D'2020

We will get started soon...



05 May 2020





WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

STRESS ANALYSIS ES-2502, D'2020

We will get started soon...

Lecture 21: Unit 17: Bending of beams:: MV diagrams & MV general relationship

05 May 2020





General information

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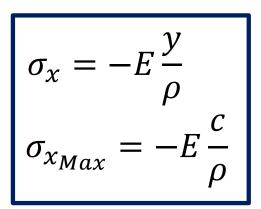


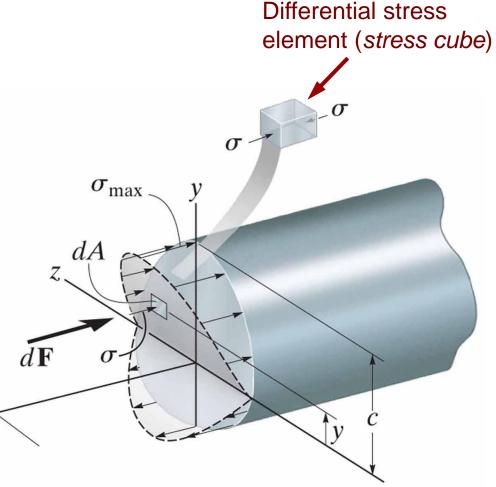
$$\sigma_{x} = \left(\frac{y}{c}\right) \cdot \sigma_{x_{Max}}$$

Normal stress variation as a function of *y* as predicted by flexure formula

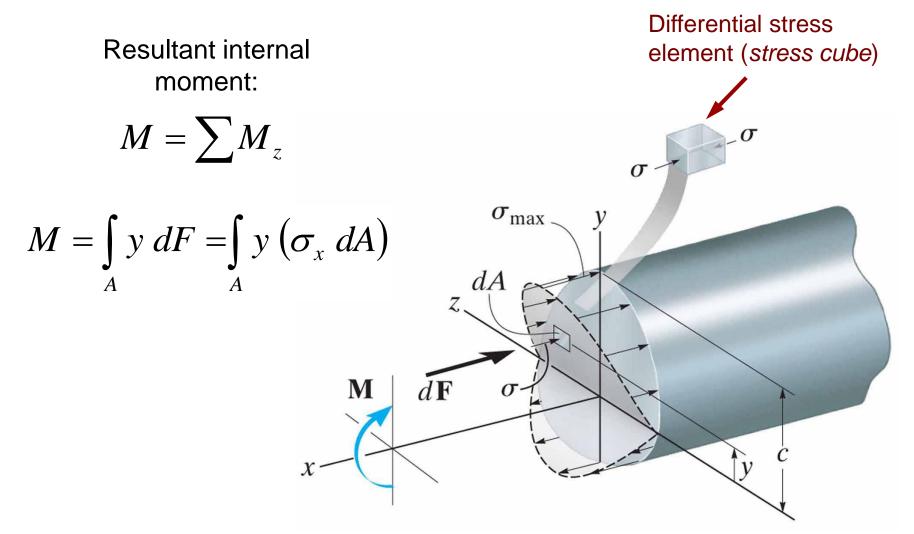
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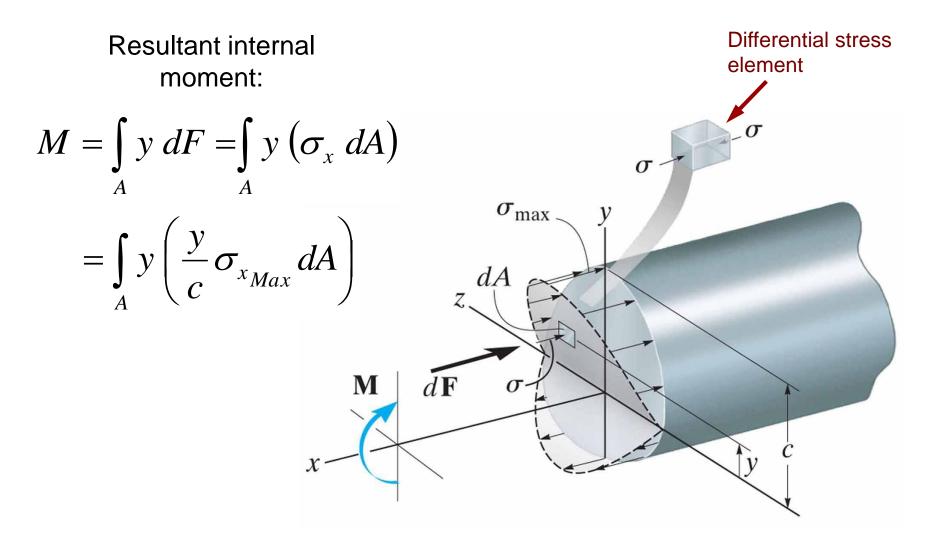




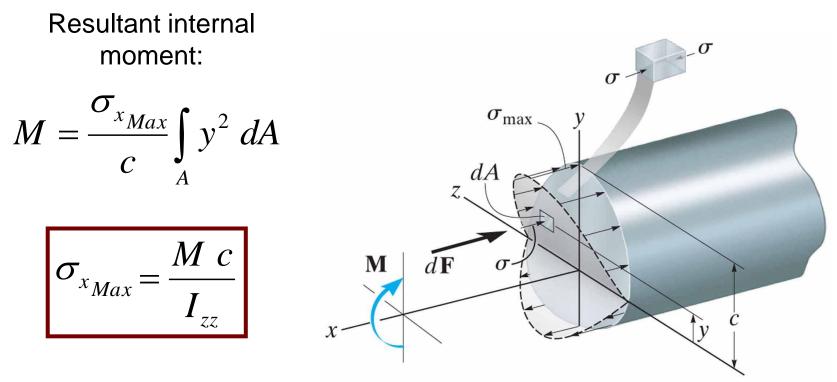










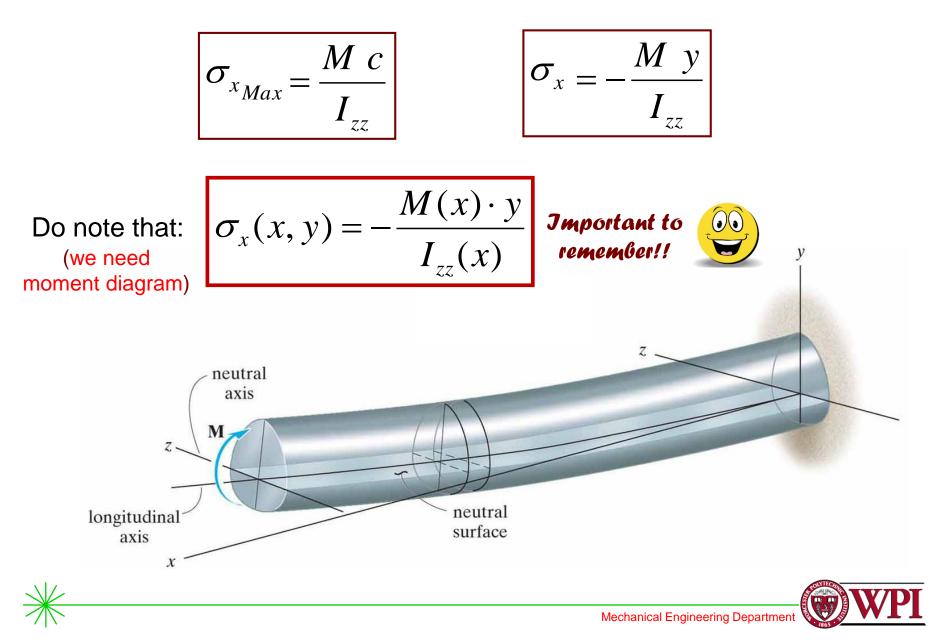


$$I_{zz} = \int_{A} y^2 \, dA$$

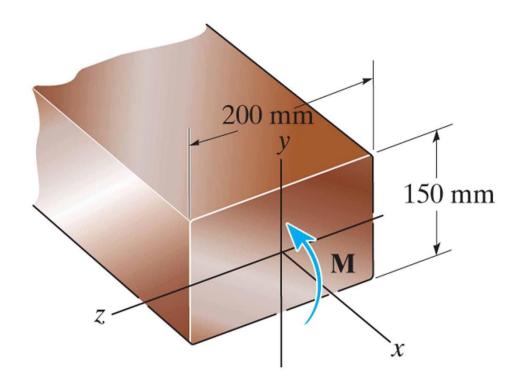
Area moment of inertia wrt to *z*-axis







A member having the dimensions shown is used to resist an internal bending moment of $M = 90 \text{ kN} \cdot \text{m}$. Determine the maximum stress in the member if the moment is applied (a) about the *z*-axis (as shown); and (b) about the *y*-axis. Sketch the stress distribution for each case.





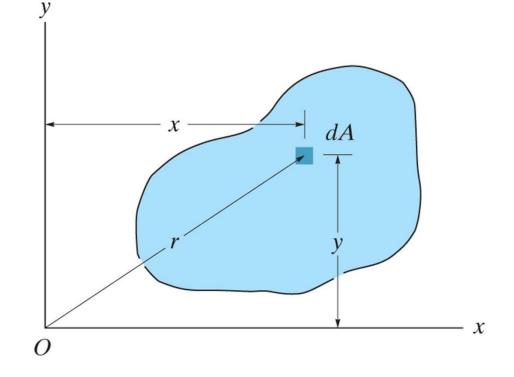


Area moment of inertia (**aka**, 2nd area moment of inertia):

$$I_{xx} = \int_{A} y^2 \, dA ,$$
$$I_{yy} = \int_{A} x^2 \, dA$$

Polar area moment of inertia:

$$J_O = I_{xx} + I_{yy}$$



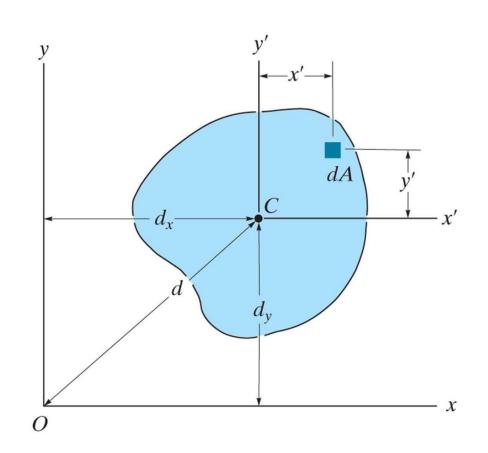


<u>Area moment of inertia:</u> *parallel-axis theorem*:

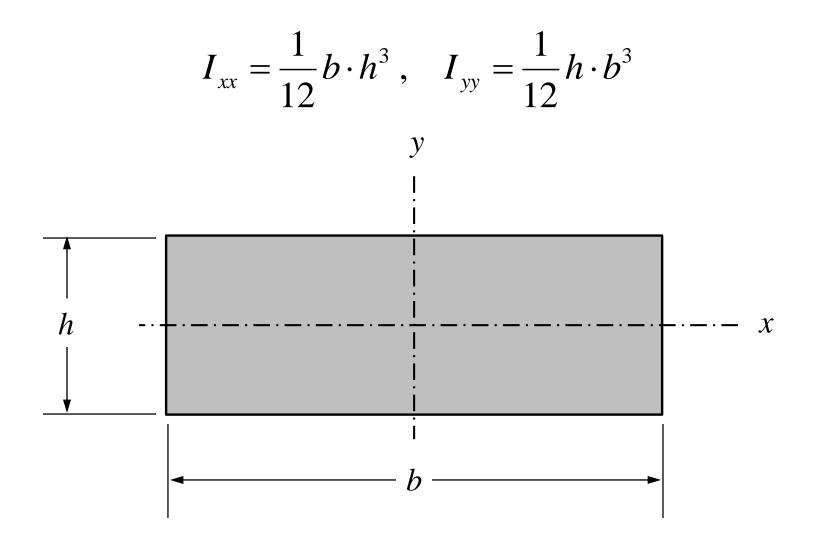
$$I_{xx} = \overline{I}_{x'x'} + A \cdot d_y^2,$$
$$I_{yy} = \overline{I}_{y'y'} + A \cdot d_x^2$$

Polar area moment of inertia: parallel-axis theorem:

$$J_o = \overline{J}_c + A \cdot d^2$$

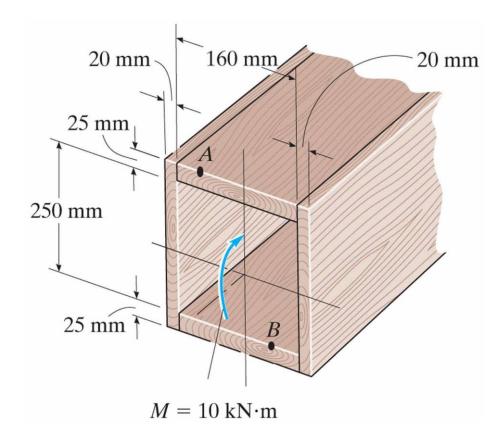


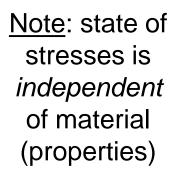






A box beam is constructed from four pieces of wood, glued together as shown. If the moment acting on the cross-section is $10 \text{ kN} \cdot \text{m}$, determine the stresses at points *A* and *B* and show the results acting on volume elements located at these points.

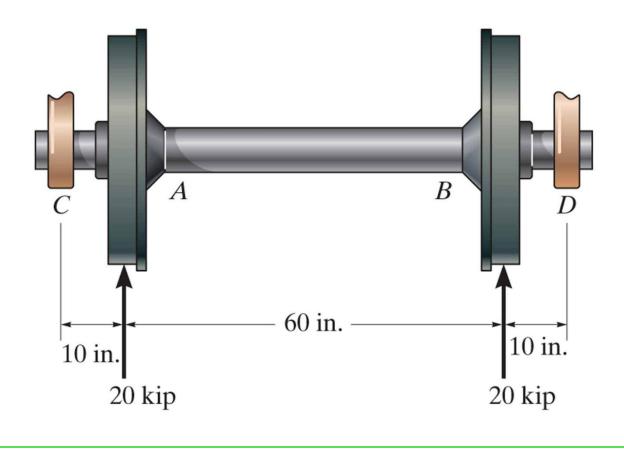








The axle of the freight car is subjected to wheel loadings of 20 kip. If it is supported by two journal bearings at C and D, determine the maximum bending stress developed at the center of the axle, where the diameter is 5.5 in. Apply two different methods

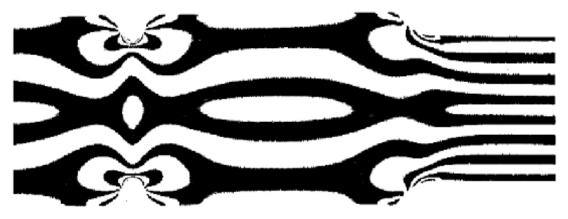


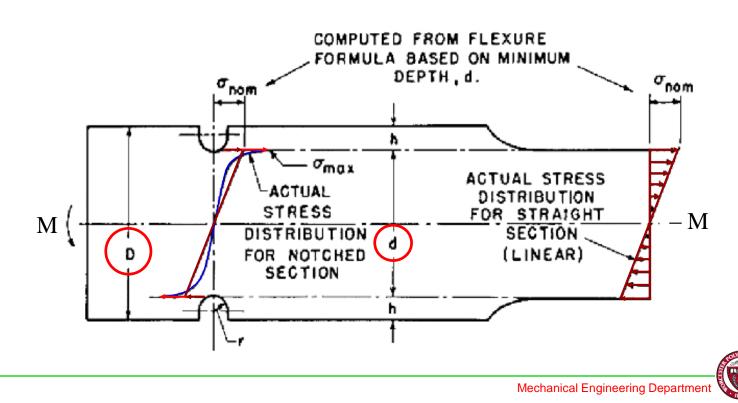




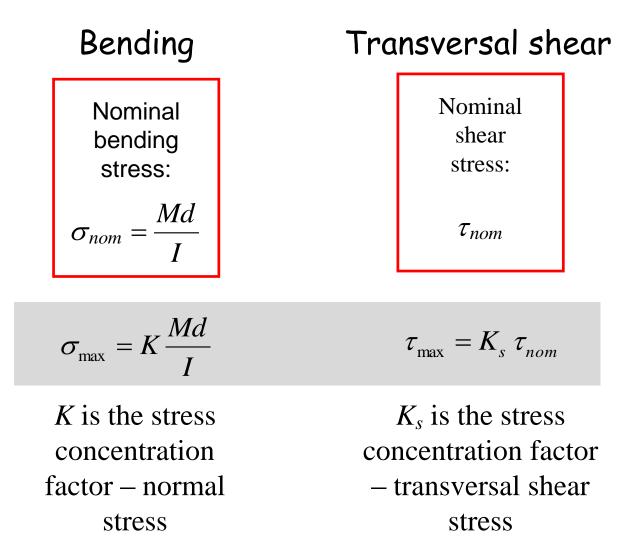
Stress concentrations: normal stresses: bending

Fringe pattern obtained with photoelasticity: pattern reveals distribution of internal stresses





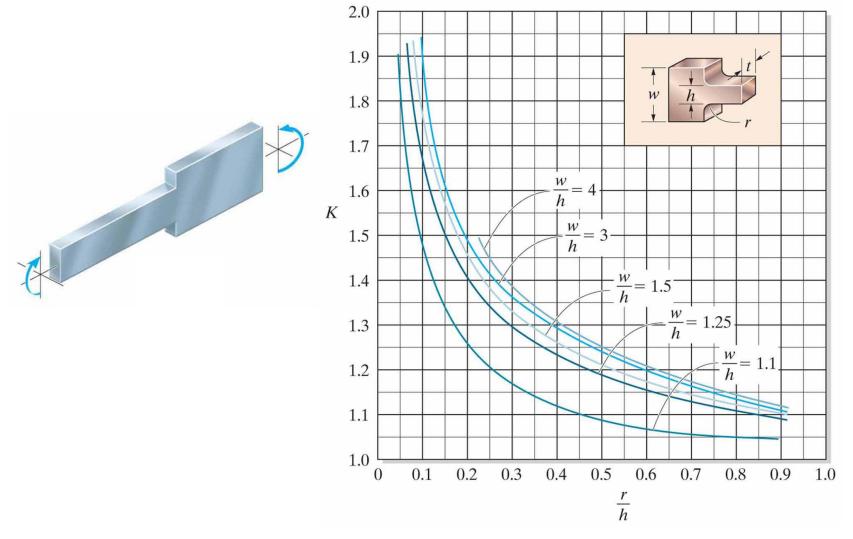
Stress concentrations: bending: normal stresses + shear







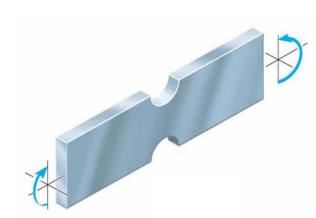
Stress concentrations: <u>normal stresses</u>: bending

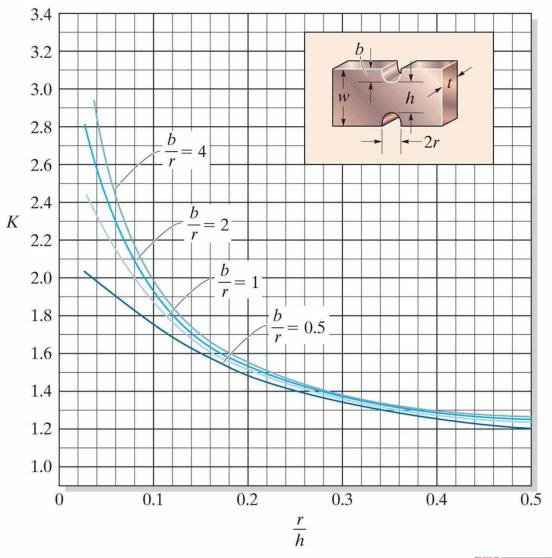






Stress concentrations: <u>normal stresses</u>: bending









Reading assignment

- Chapter 6 of textbook
- Review notes and text: ES2001, ES2501





Homework assignment

• As indicated on webpage of our course



