

# WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

## STRESS ANALYSIS ES-2502, D'2020

**We will get started soon...**



**01 May 2020**



# WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

## STRESS ANALYSIS ES-2502, D'2020

We will get started soon...

Lecture 20:

Unit 15, 16: Bending of beams::  
*MV diagrams & MV general relationship*

01 May 2020



# General information

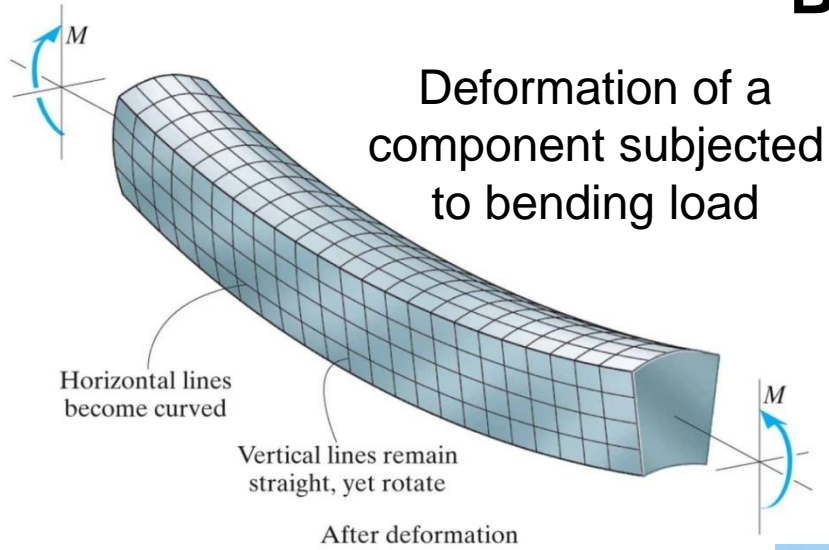
Instructor: Cosme Furlong  
HL-152  
(774) 239-6971 - Texting Works

Email: cfurlong @ wpi.edu  
<http://www.wpi.edu/~cfurlong/es2502.html>

Teaching Assistant: Zachary Zolotarevsky  
Email: zjzolotarevsky @ wpi.edu



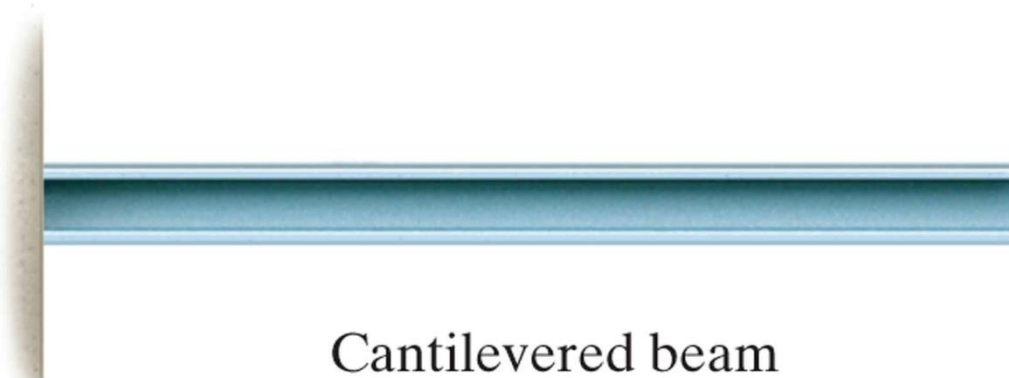
# Bending



# Bending: many real components are modeled as “beams”



Simply supported beam



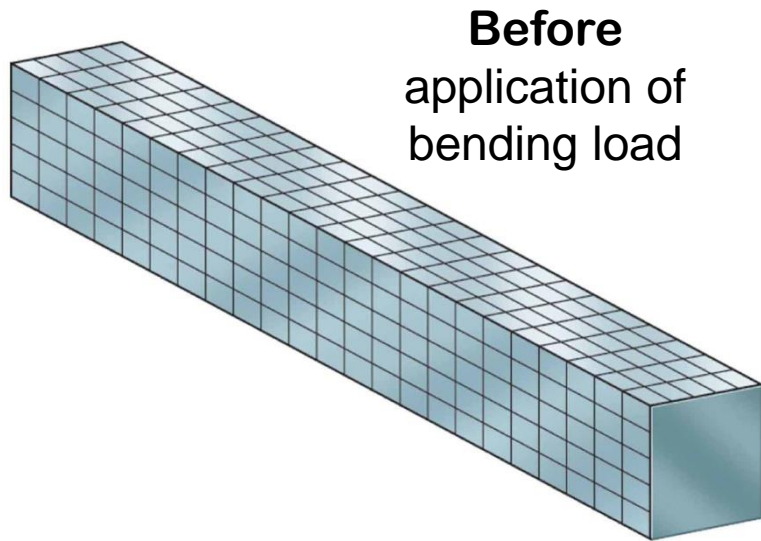
Cantilevered beam



Overhanging beam

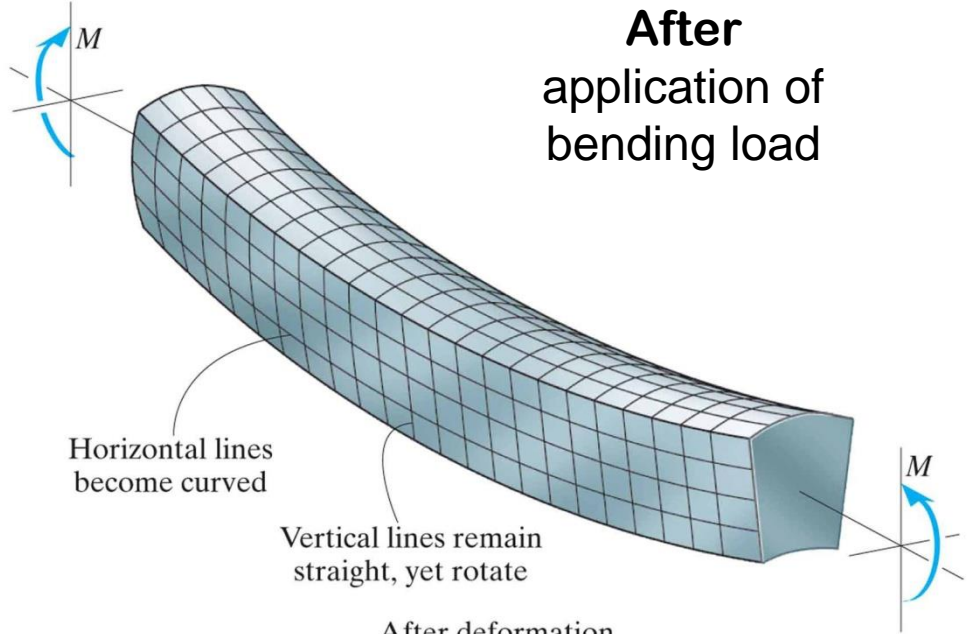


# Bending



Before application of bending load

Before deformation

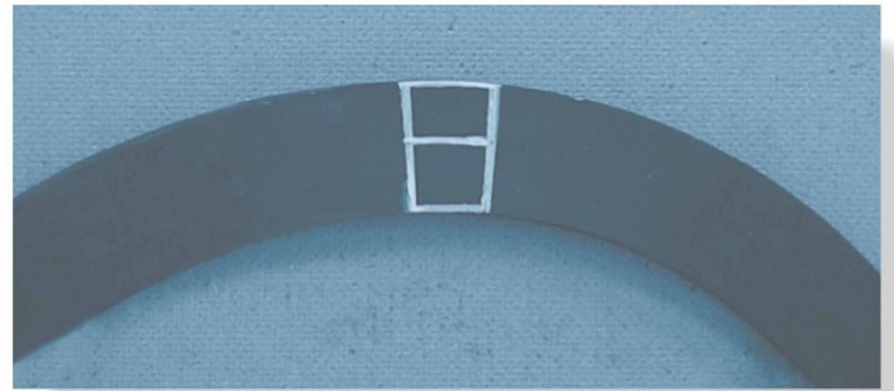
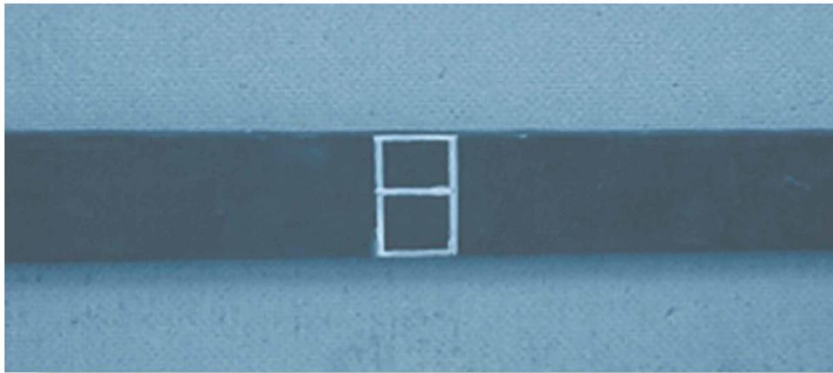


After application of bending load

Horizontal lines become curved

Vertical lines remain straight, yet rotate

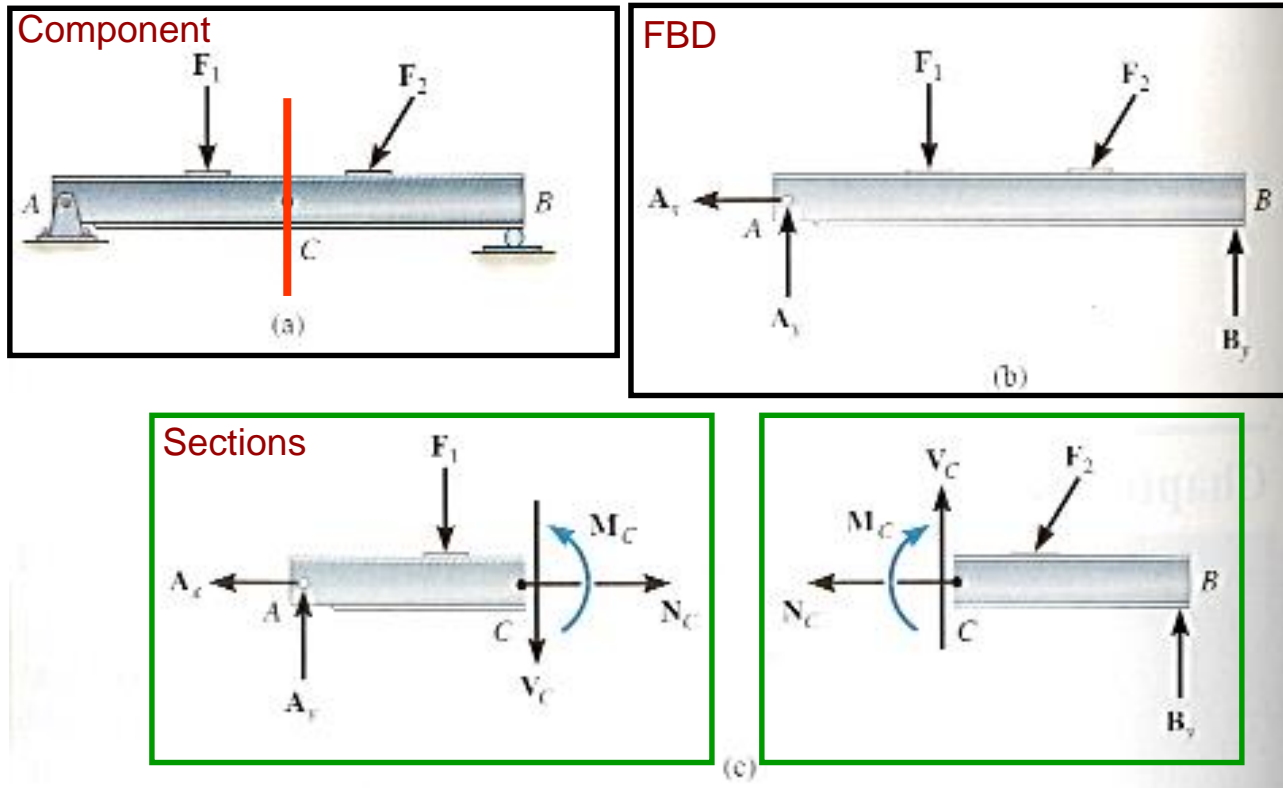
After deformation



# Internal forces and moments

## Shear and bending moments

Internal forces (determination of shear and moment diagrams)

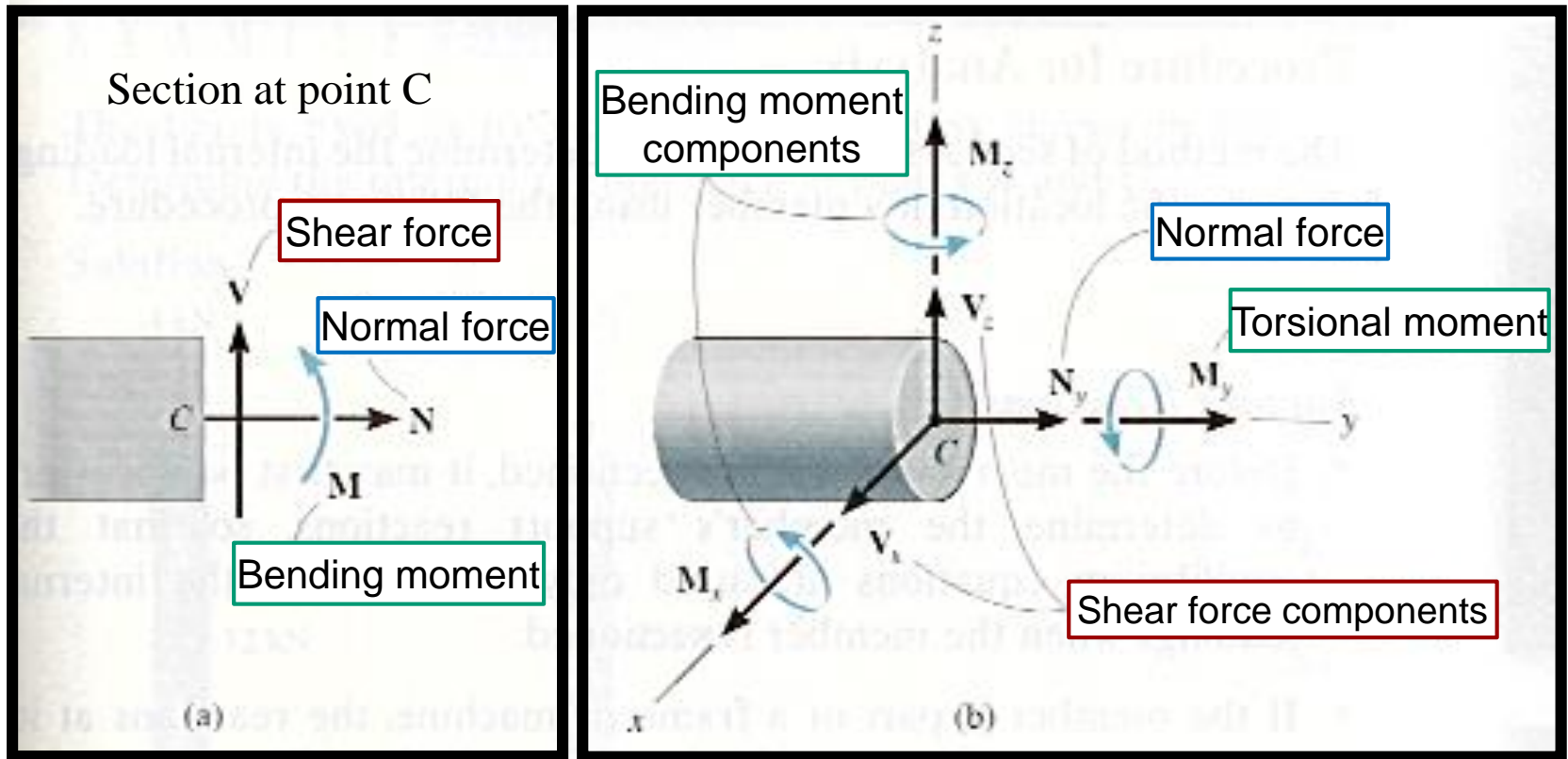


Internal: moments, shear, and normal forces at point  $C$



# Internal forces and moments

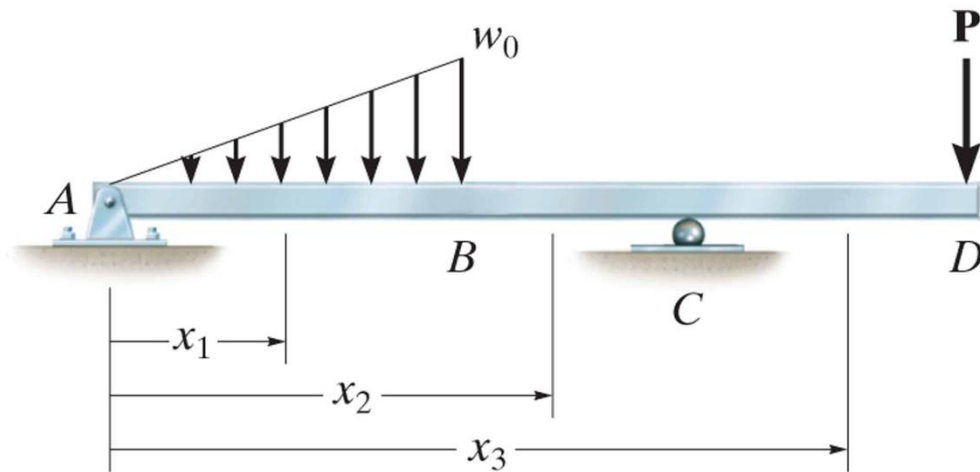
## Shear and bending moments



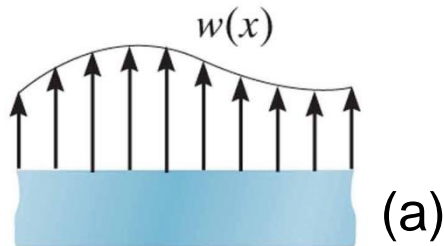


# Shear and bending diagrams

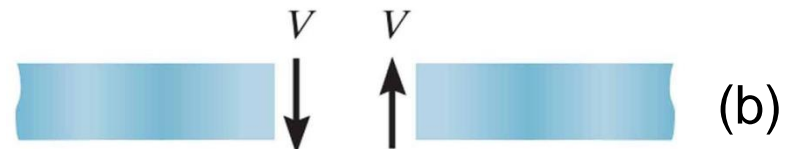
Diagrams are determined for *each region* of the beam *between* any two discontinuities of loading



## Beam sign convention



Positive external distributed load



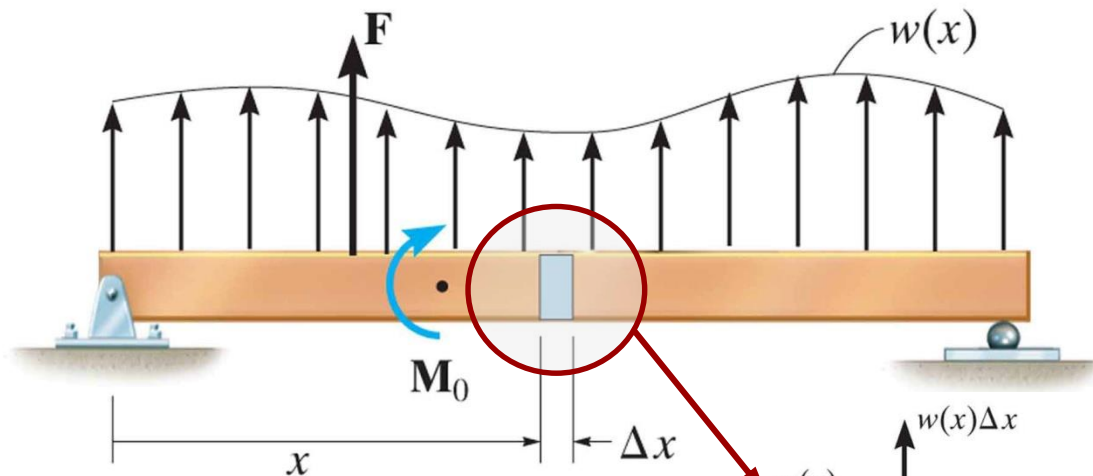
Positive internal shear



Positive internal moment



# Shear and bending diagrams: regions with distributed load

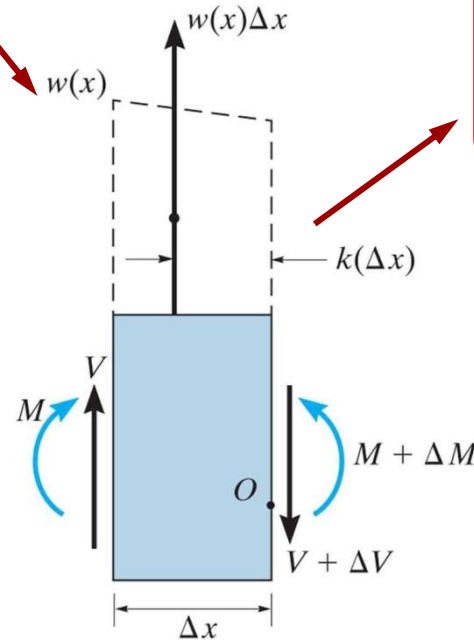


**Important to remember!!** 😊

$$\frac{dV}{dx} = w(x);$$

$$\frac{dM}{dx} = V(x)$$

Free body diagram of element  $\Delta x$ :



Free-body diagram of segment  $\Delta x$



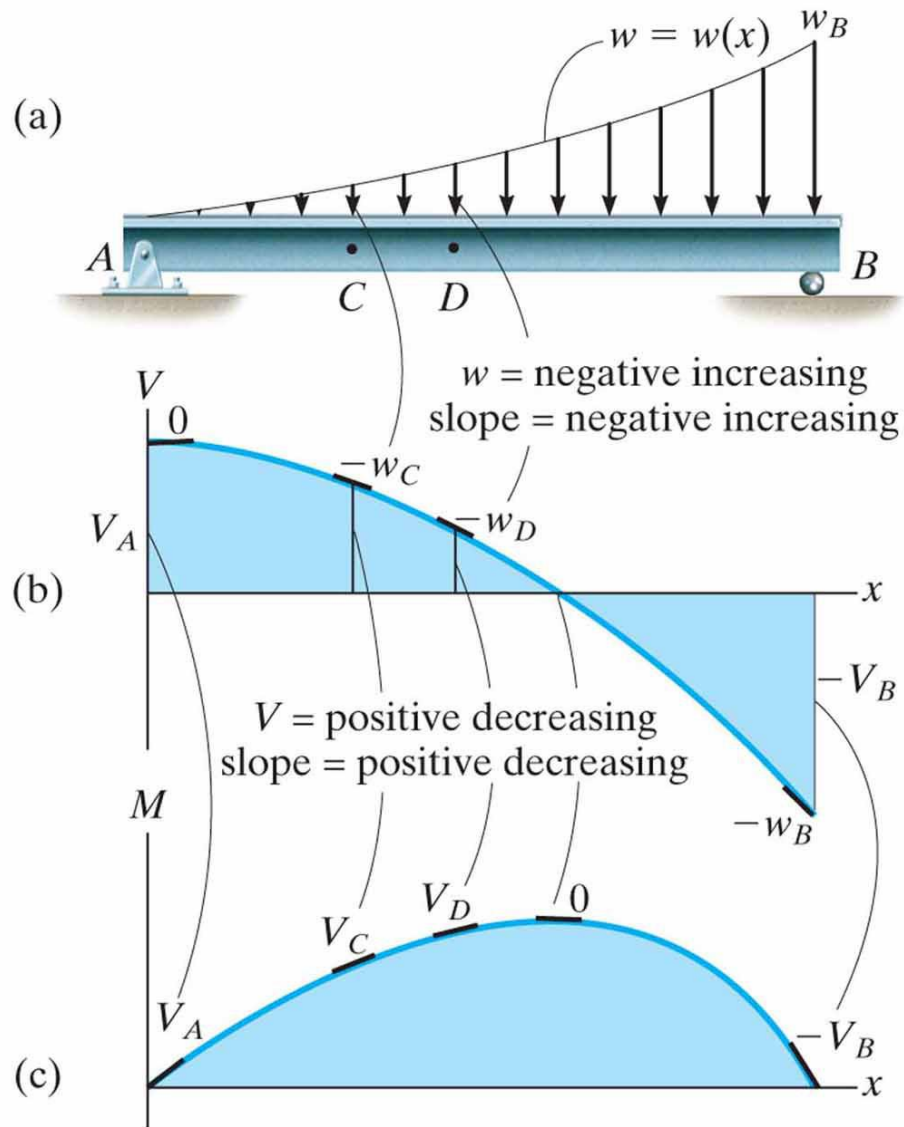
# Shear and bending diagrams: regions with distributed load

**Important to remember!!**

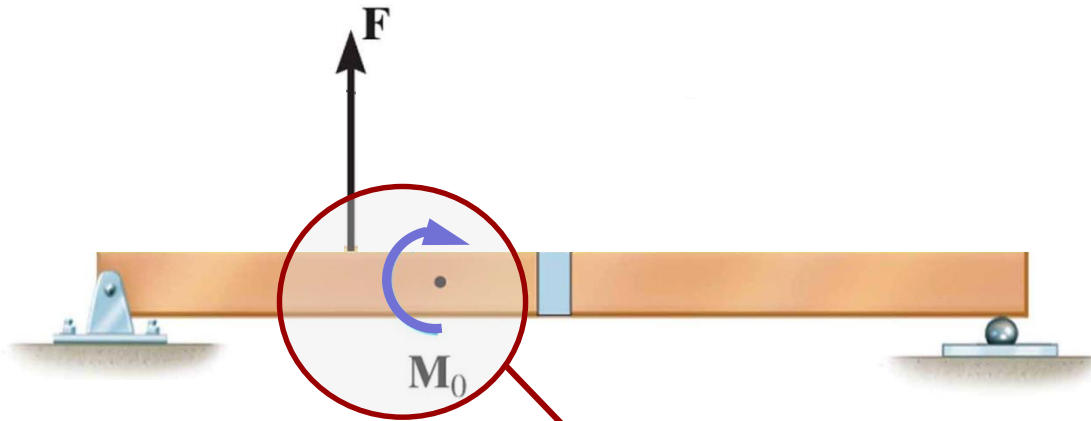


$$\frac{dV}{dx} = w(x);$$

$$\frac{dM}{dx} = V(x)$$



# Shear and bending diagrams: regions with concentrated force and moment



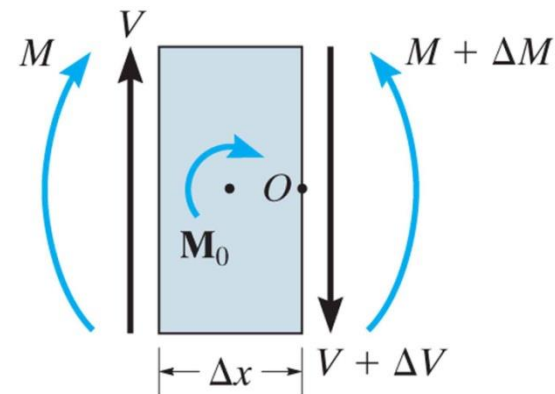
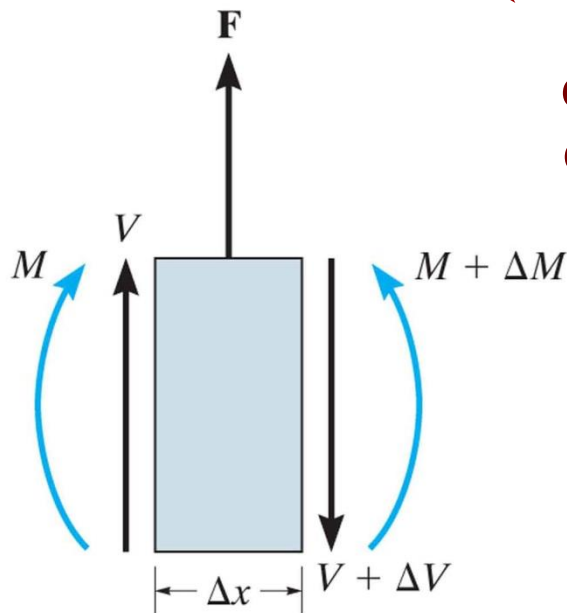
*Important to  
remember!!*



$$\Delta V = F ;$$

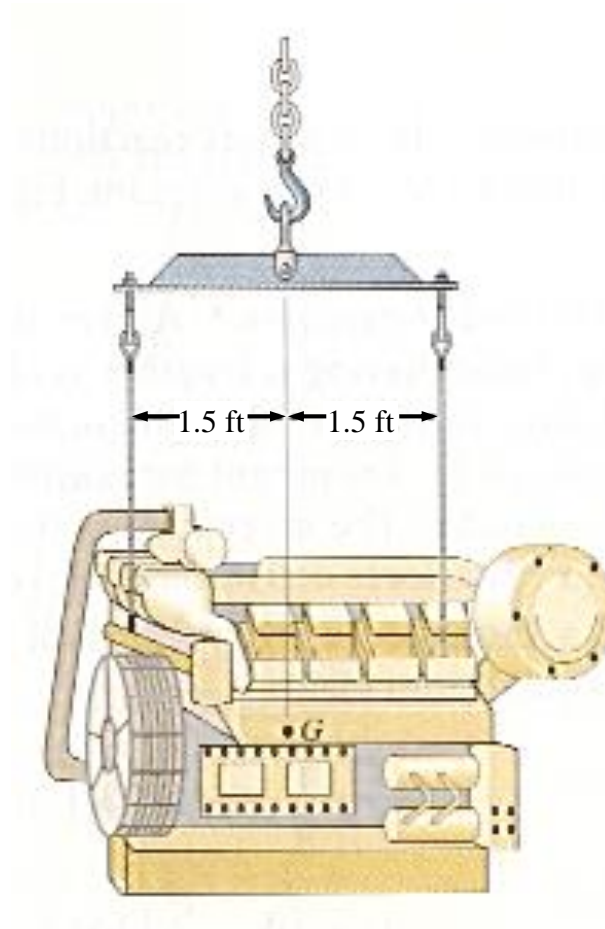
$$\Delta M = M_0$$

Free body  
diagrams of  
element  $\Delta x$ :



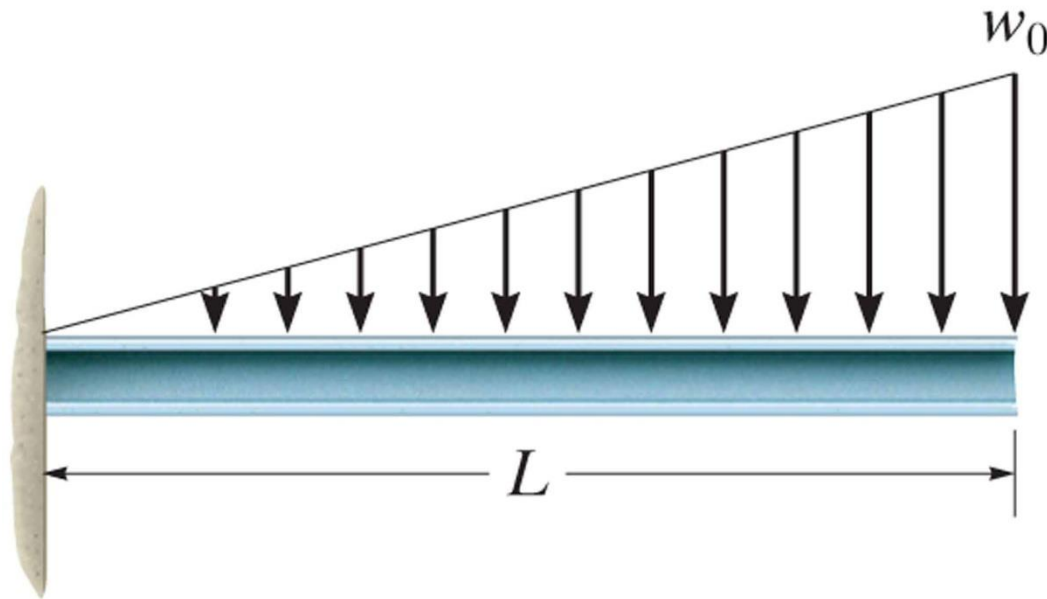
# Shear and bending diagrams: example A

A suspended bar supports a 600-lb engine. Plot the shear and moment diagrams for the bar



# Shear and bending diagrams: example B

Determine the shear and moment diagrams for the beam shown



# Reading assignment

- Chapter 6 of textbook
- Review notes and text: ES2001, ES2501



# Homework assignment

- As indicated on webpage of our course

