WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

STRESS ANALYSIS ES-2502, D'2020

We will get started soon...



30 April 2020





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STRESS ANALYSIS ES-2502, D'2020

We will get started soon...

Lecture 19: Unit 12, 13: Torsion of shafts: circular cross-section: statically indeterminate & stress concentrations

30 April 2020



General information

<u>Instructor</u>: Cosme Furlong HL-152 (774) 239-6971 – Texting Works

Email: cfurlong @ wpi.edu http://www.wpi.edu/~cfurlong/es2502.html

<u>Teaching Assistant</u>: Zachary Zolotarevsky Email: zjzolotarevsky @ wpi.edu





Statically indeterminate torque-loaded members







Statically indeterminate torque-loaded members

<u>Compatibility</u> equation: (Same angle of twist)

$$\frac{T_A L_{AC}}{J G} = \frac{T_B L_{BC}}{J G}$$







Statically indeterminate torque-loaded members

Solution with: two equations for two unknowns (T_A and T_B):







Statically indeterminate torque-loaded members: example A

The A-36 steel shaft has a diameter of 60 mm and is fixed at its ends *A* and *B*. If it is subjected to the torques shown, determine the absolute maximum shear stress in the shaft



Approach:

1)

- Apply equilibrium equations
- 2) Apply compatibility equations (*two possible methods*)
- 3) Solve for stresses





Statically indeterminate torque-loaded members: example B

The steel shaft is made from two segments: *AC* has a diameter of 0.5 in, and *CB* has a diameter of 1 in. If it is fixed at its ends *A* and *B* and subjected to a torque of 500 lb·in, determine the maximum shear stress in the shaft. $G_{st} = 10.8$ Mpsi.







Statically indeterminate torque-loaded members: example C

The shaft is made from a solid steel section *AB* and a tubular portion made of steel and having a brass core. If it is fixed to a rigid support at *A*, and a torque of T = 50 lb·ft is applied to it at *C*, determine the angle of twist that occurs at *C* and compute the maximum shear stress and maximum shear strain in the brass and steel. $G_{st} = 11.5$ Mpsi, $G_{br} = 5.6$ Mpsi.



Statically indeterminate torque-loaded members: example D

The A-36 steel shaft is made from two segments: *AC* has a diameter of 0.5 in and *CB* has a diameter of 1 in. If the shaft is fixed at its ends *A* and *B* and subjected to a uniform distributed torque of 60 $lb_{f'}in/in$ along segment *CB*, determine the absolute maximum shear stress in the shaft



Approach:

- 1) Apply equilibrium equations
- 2) Apply compatibility equations
- 3) Solve for stresses





Statically indeterminate torque-loaded members: example E

If the shaft is subjected to a uniform distributed torque of $20 \text{ kN} \cdot \text{m/m}$, determine the maximum shear stress developed in the shaft. The shaft is made of 2014-T6 aluminum alloy and is fixed at *A* and *C*.



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Approach:

- 1) Apply equilibrium equations
- 2) Apply compatibility equations
- 3) Solve for max. stress
 EXTRA CREDIT
 3-points in Exam Grade
 Due: Monday, May 04th

Before 11:00 am

(<u>No partial credit</u>)









Locations with stress concentrations







$$(\tau_{\max})_{amplified} = K \tau_{\max} = K \frac{T c}{J}$$

Stress concentration factor: K
(amplification factor)











Stress concentrations, torsion: example A

The assembly is subjected to a torque of $710 \text{ lb}_{f} \cdot \text{in}$. If the allowable shear stress for the material is $\tau_{\text{allow}} = 12 \text{ ksi}$, determine the radius of the smallest size fillet that can be used to transmit the torque.







Stress concentrations, torsion: example A





Reading assignment

- Chapter 5 of textbook
- Review notes and text: ES2001, ES2501





Homework assignment

• As indicated on webpage of our course



