## WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

STRESS ANALYSIS ES-2502, D'2020

We will get started soon...



30 March 2020





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Lecture 03: Unit 3: definition of normal and shear stress

30 March 2020





### General information

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### **Free-body diagrams**

# Operator applies 20-lb to pedal stretching spring by 1.5 in.



#### Actual mechanism

#### Schematic representation:



#### Free-body diagram:



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#### Force analysis. Free-body diagrams

Is this a statically indetermined case ?







### Force analysis. Free-body diagrams





#### Force analysis. Free-body diagrams























### Internal resultant loading: example A

Determine resultant internal loading acting on the cross section at C of the cantilever shown:



#### Approach:

- 1) Define free-body diagrams
- 2) Apply equilibrium equations





#### Internal resultant loading: example A



### Internal resultant loading: example B

Determine resultant internal loading acting on the cross section at *C* of the machine shaft shown. Shaft is supported by bearings at A and B, which only exert radial forces on the shaft



#### Approach:

- 1) Define free-body diagrams
- Apply equilibrium equations: reactions at bearings
- Apply equilibrium equations: internal loading





### Internal resultant loading: example B





### Internal resultant loading: example B











### Internal resultant loading: example C

Determine the resultant internal torque acting on the cross sections through points *C* and *D*. Supports *A* and *B* allow free turning of the shaft



#### Approach:

- 1) Define free-body diagram
- 2) Apply equilibrium equations



#### Internal resultant loading: example D

The force  $F = 80 \ lb_f$  acts on the gear tooth. Determine the resultant internal loadings on the root of the tooth, i.e., at the centroid point *A* of section *a*-*a* 



a

#### Approach:

- 1) Define free-body diagram
- 2) Apply equilibrium equations

0.16 in.



Stress. Definition: intensity of internal force: acting on a specific plane passing through a point





Stress. Definition: intensity of internal force: acting on a specific plane passing through a point



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#### **General state of stresses**





Figure: 02-01-A-UN Note the before and after positions of three different line segments on this rubber membrane which is subjected to tension. The vertical line is lengthened, the horizontal line is shortened, and the inclined line changes its length and rotates. is shortened, and the inclined line changes its length and rotates.



#### Figure: 02-01-B-UN

Note the before and after positions of three different line segments on this rubber membrane which is subjected to tension. The vertical line is lengthened, the horizontal line











$$+\uparrow F_{Rz}=\sum F_{z}$$

$$\int dF = \int_{A} \sigma \, dA$$
$$P = \sigma \, A$$

Average normal stress:  

$$\sigma = \frac{P}{A}$$







### **Reading assignment**

- Chapter 1 of textbook
- Review notes and text: ES2001, ES2501





### Homework assignment

• As indicated on webpage of our course



