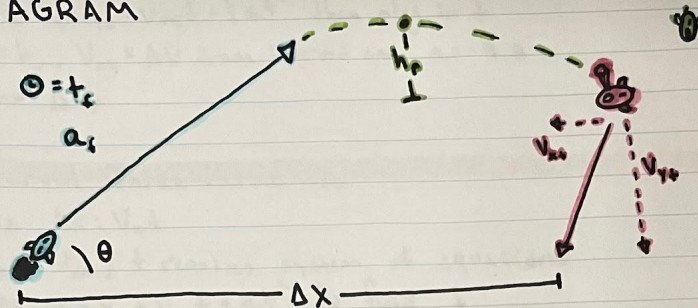


Cecilia Carbonell  
DIAGRAM

9.28.23



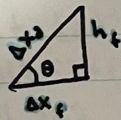
$$\begin{aligned}\theta &= 48^\circ \\ t_f &= 7.5 \text{ s} \\ a_f &= 6.1 \text{ m/s}^2 \\ h_p &= 70. \text{ m} \\ V_{yf} &= 9.0 \text{ m/s} \\ V_{xf} &= 15.0 \text{ m/s} \\ \Delta X &= ?\end{aligned}$$

### APPROACH

Break problem into three parts. Find horizontal distance over each interval and add to get final answer.

#### Interval One: Engine Firing

- Use  $\Delta x = v_0 t + \frac{1}{2} a t^2$
- $v_0 = 0$ ,  $t = t_f$ ,  $a = a_f$
- $\Delta x$  is total distance travelled, not horizontal distance



$$\begin{aligned}\cos \theta &= \frac{\Delta x_f}{h_f} \\ \sin \theta &= \frac{h_f}{\Delta x_f}\end{aligned}$$

- Find final velocity with  $\Delta v = at$

#### Interval Two: Projectile Motion

##### Part One: Find Max Height

- Use  $v^2 = v_0^2 + 2a\Delta y$
- $v = 0$ ,  $v_0 = \Delta v$  from interval one,  $a = a$ ,  $h_p = \Delta y$
- $h_f + \Delta y = \text{max height } (h_m)$

##### Part Two: Find height of parachute

- $h_m - h_p = \text{height of parachute } (h_r)$

##### Part Three: Horizontal Distance

- Use  $\Delta x = v_x t$
- $v_x = \Delta v$  from interval one, solve for  $t$  with...

- Use  $y = y_0 + v_{0y}t + \frac{1}{2}at^2$  then plug in  $t$
- $y = h_r$ ,  $v_{0y} = \Delta v$  from interval one,  $a = -9.8$
- Find  $\Delta x_p$

### Interval Three: Parachute

- Use  $\Delta x = v_x t$
- $v_x = -v_{xt}$ ,  $t$  requires system of equations
- Use  $y = y_0 + v_{0y}t + \frac{1}{2}at^2$  to find  $t$
- $y = 0$ ,  $y_0 = h_r$ ,  $v_{0y} = -v_{yt}$ ,  $a = 0$
- Use  $t$  to find  $\Delta x_p$

### Finale: Find Total Distance

- $\Delta x = \Delta x_e + \Delta x_p + \Delta x_t$

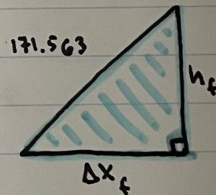
### MY SOLUTION

#### ① Engine Firing

$$\Delta x_e = v_0 t + \frac{1}{2}at^2$$

$$\Delta x_e = (0)(7.5) + \frac{1}{2}(0.1)(7.5)^2$$

$$\Delta x_e = 171.563$$



$$\cos 48 = \frac{\Delta x_e}{171.563}$$

$$171.563 \cos 48 = \Delta x_e$$

$$\Delta x_e = 114.798 \text{ m}$$

$$\sin 48 = \frac{h_e}{171.563}$$

$$171.563 \sin 48 = h_e$$

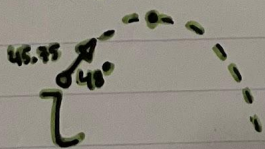
$$h_e = 127.496 \text{ m}$$

$$\Delta v = at$$

$$\Delta v = (0.1)(7.5)$$

$$\Delta v = 45.75 \text{ m/s}$$

#### ② Projectile Motion



#### ① Height of Chute

$$h_r = 186.472 - 70$$

$$h_r = 116.472 \text{ m}$$

#### ② Find Max Height

$$v^2 = v_0^2 + 2a\Delta y$$

$$0 = (45.75)^2 + (2)(-9.8)(\Delta y)$$

$$\Delta y = \frac{(45.75 \sin 48)^2}{19.6}$$

$$\Delta y = 58.9757 \text{ m}$$

$$\text{Total Height} = 186.472 \text{ m}$$

### ② Horizontal Distance

$$\Delta x = v_x t$$

$$\Delta x = 45.75 \cos 48 t$$

$$y = y_0 + v_{0y} t + \frac{1}{2} a t^2$$

$$116.472 = 127.496 + 45.75 \sin 48 t - 4.9 t^2$$

$$t = 7.25$$

$$\Delta x_p = 221.942 \text{ m}$$

### ③ Parachute



$$\Delta x = -15 t$$

$$y = y_0 + v_{0y} t + \frac{1}{2} a t^2$$

$$0 = 118.471 - 9 t$$

$$t = 13.1634$$

$$\Delta x_s = -197.452 \text{ m}$$

### ④ Final

$$\Delta x = \Delta x_f + \Delta x_p + \Delta x_s$$

$$\Delta x = 114.798 + 221.942 - 197.452$$

$$\Delta x = 138.838 \text{ m E}$$