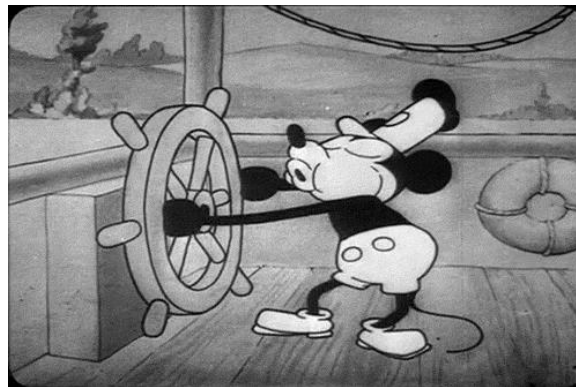


WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

STRESS ANALYSIS ES-2502, B'2025

We will get started soon...



23 October 2025



WORCESTER POLYTECHNIC INSTITUTE MECHANICAL ENGINEERING DEPARTMENT

STRESS ANALYSIS ES-2502, B'2025

Lecture 04: Unit 3: definition of normal and shear stress

23 October 2025



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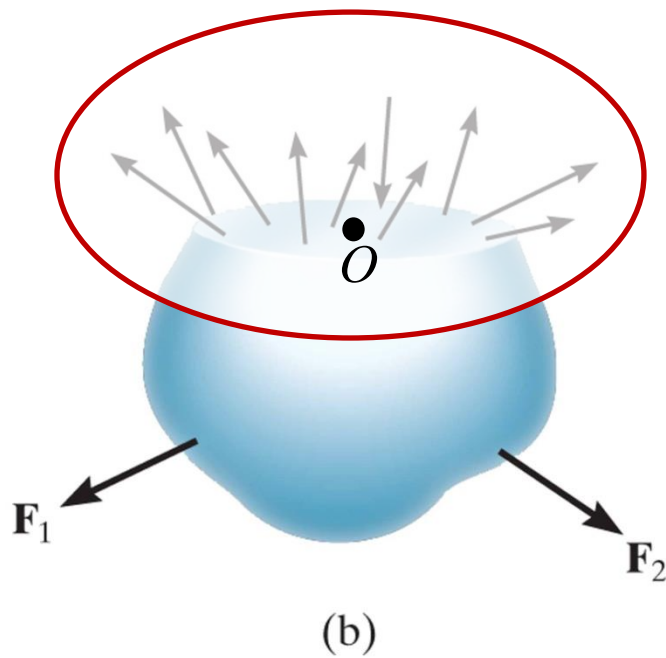
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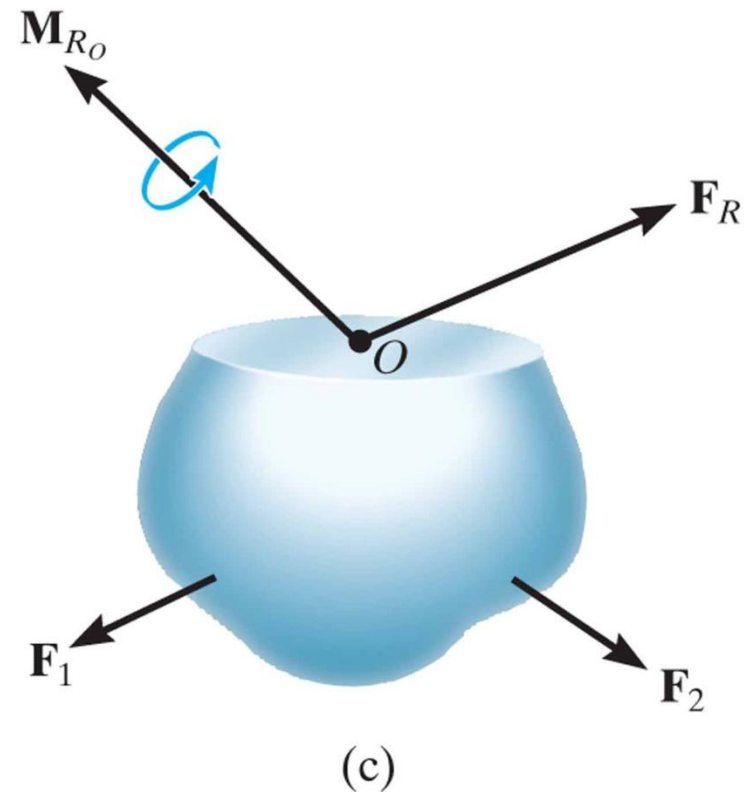


Stress: Definition: intensity of internal force: acting on a specific plane passing through a point

$$\mathbf{F}_R = \sum \mathbf{F}$$
$$\mathbf{M}_{R_o} = \sum \mathbf{M}_o$$

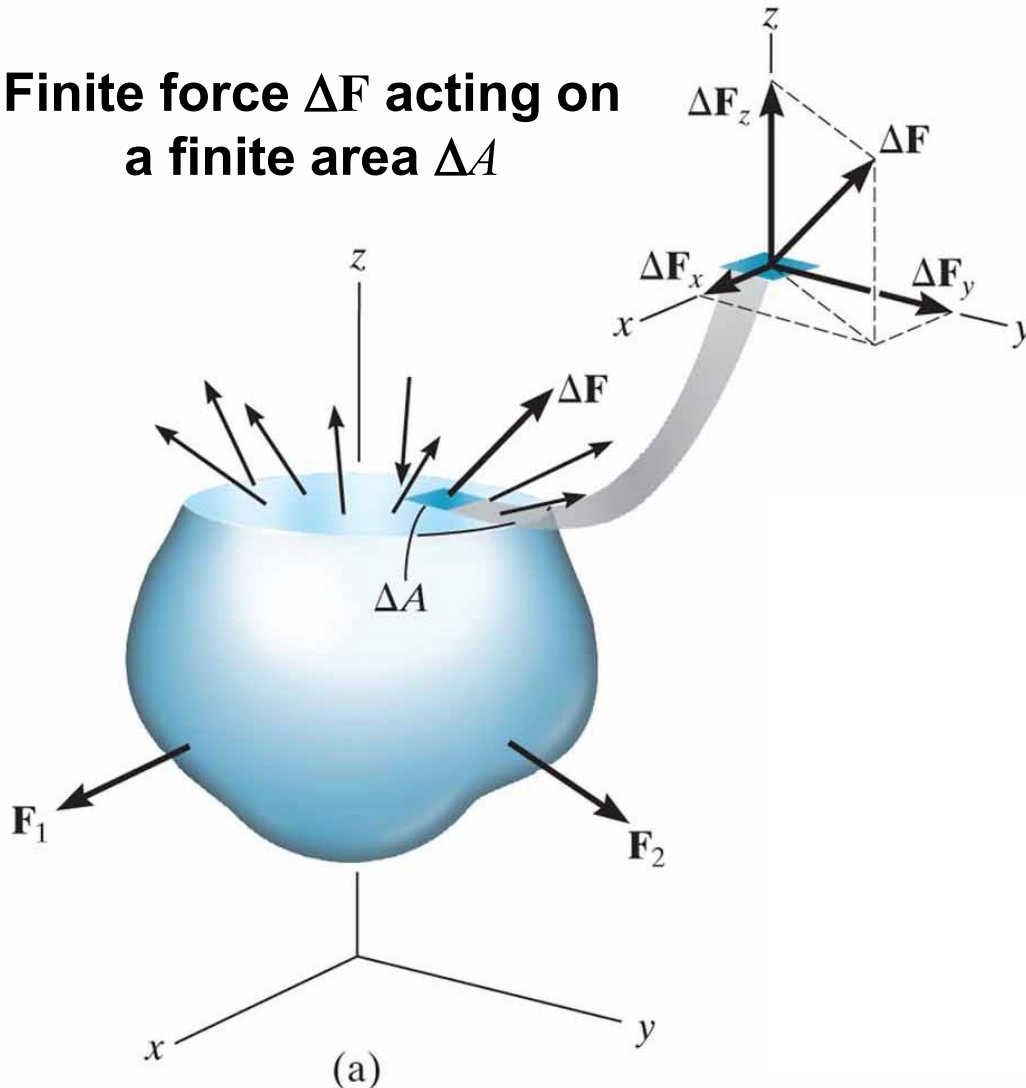


Equivalent
force and
moment at
the section



Stress: Definition: intensity of internal force: acting on a specific plane passing through a point

Finite force ΔF acting on a finite area ΔA



Definition

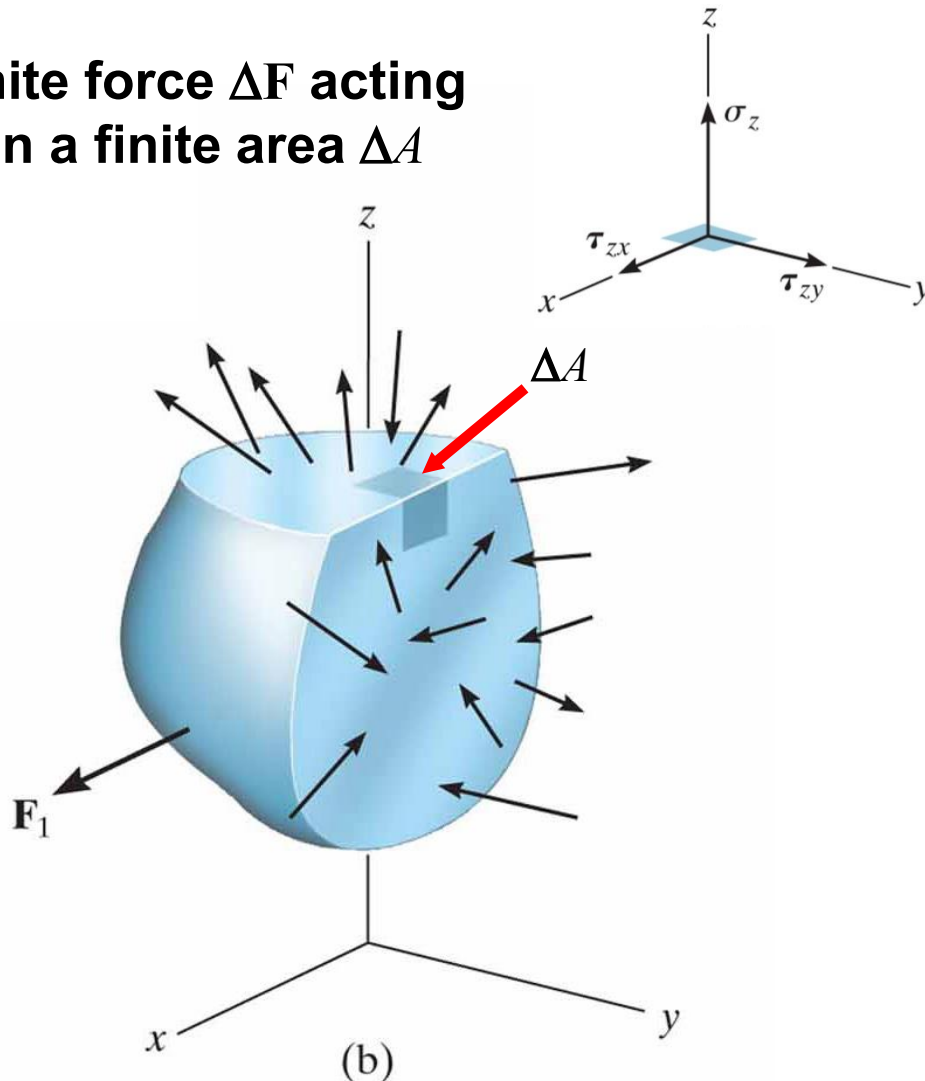
Normal stress:

$$\sigma_z = \lim_{\Delta A \rightarrow 0} \frac{\Delta F_z}{\Delta A}$$



Stress: Definition: intensity of internal force: acting on a specific plane passing through a point

Finite force ΔF acting
on a finite area ΔA



Definitions

Shear stresses:

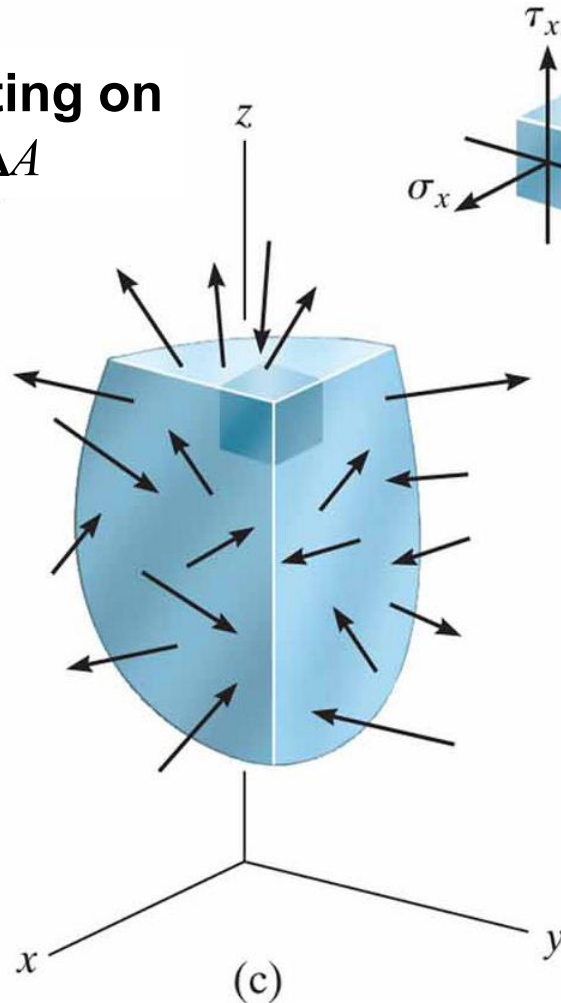
$$\tau_{zx} = \lim_{\Delta A \rightarrow 0} \frac{\Delta F_x}{\Delta A}$$

$$\tau_{zy} = \lim_{\Delta A \rightarrow 0} \frac{\Delta F_y}{\Delta A}$$



Stress: Definition: intensity of internal force: acting on a specific plane passing through a point

Finite force ΔF acting on a finite area ΔA

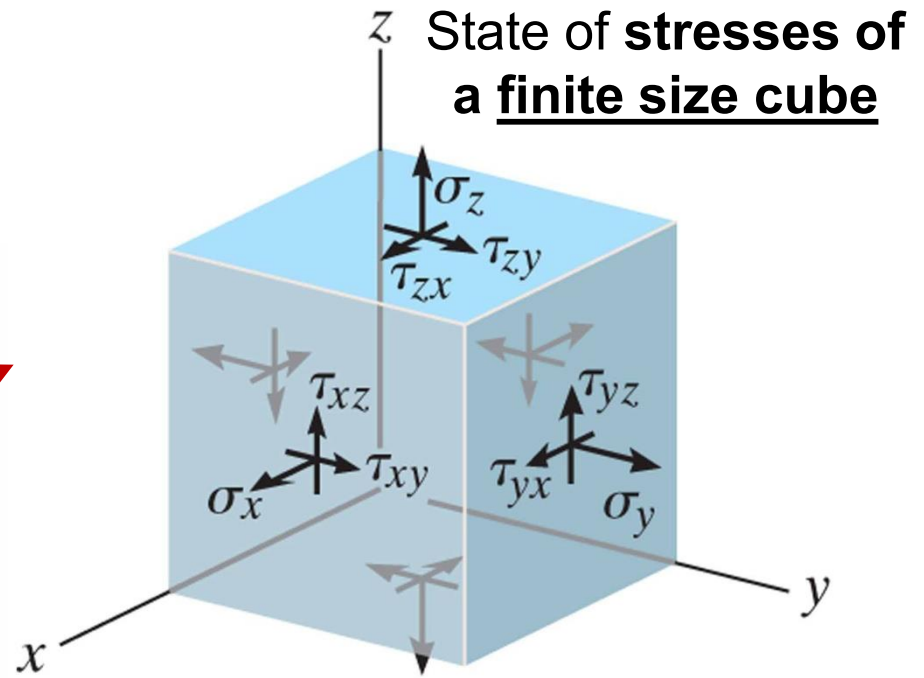
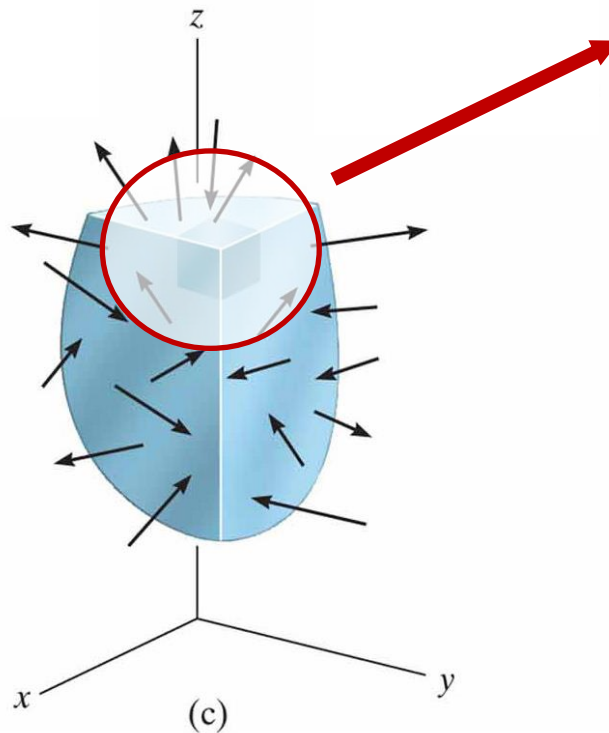


Normal and shear stresses on plane x



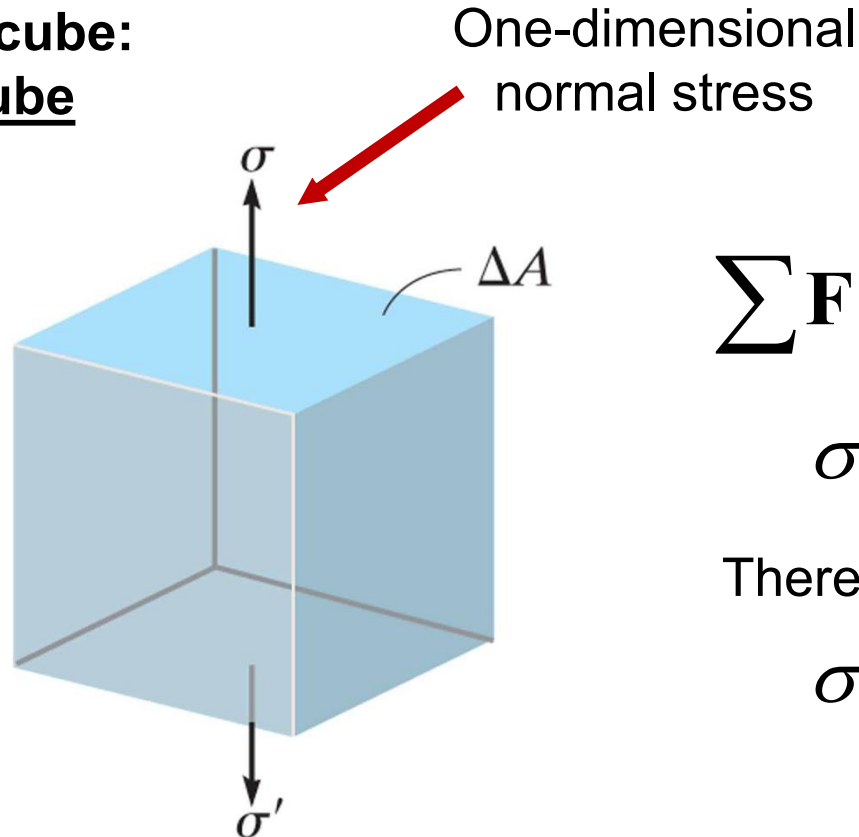
General state of stresses

Further sectioning leads to a “**stress cube**”



State of stresses: normal stress equilibrium (1D)

Finite size cube:
stress cube



$$\sum \mathbf{F} = \mathbf{0}; \Rightarrow$$

$$\sigma(\Delta A) = \sigma'(\Delta A)$$

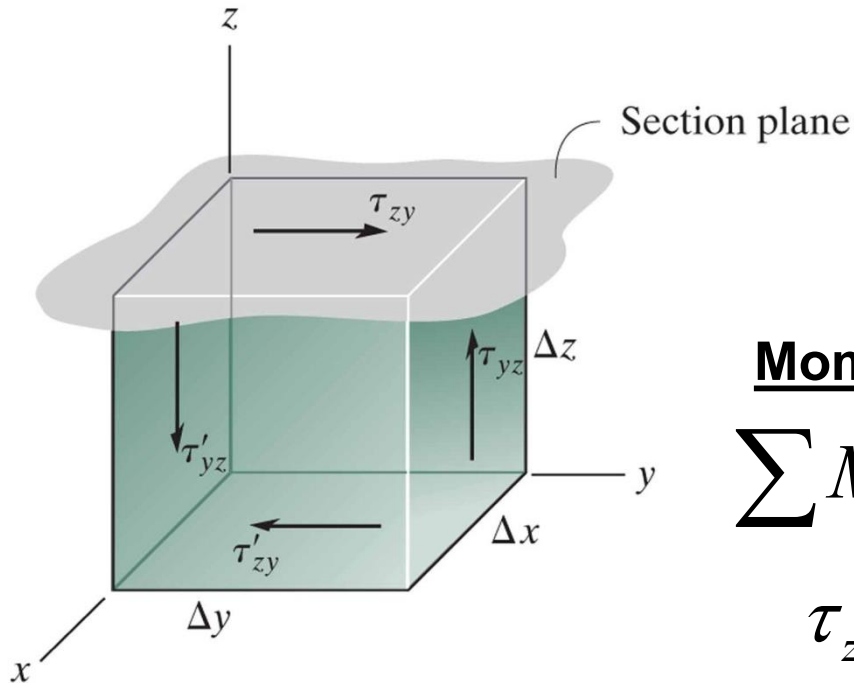
Therefore,

$$\sigma = \sigma'$$



State of stresses: shear stress equilibrium

Finite size cube:
stress cube



Forces:

$$\sum F_y = 0; \Rightarrow$$

$$\tau_{zy} (\Delta x \Delta y) = \tau'_{zy} (\Delta x \Delta y)$$

$$\text{Therefore, } \tau_{zy} = \tau'_{zy}$$

Moments:

$$\sum M_x = 0; \Rightarrow$$

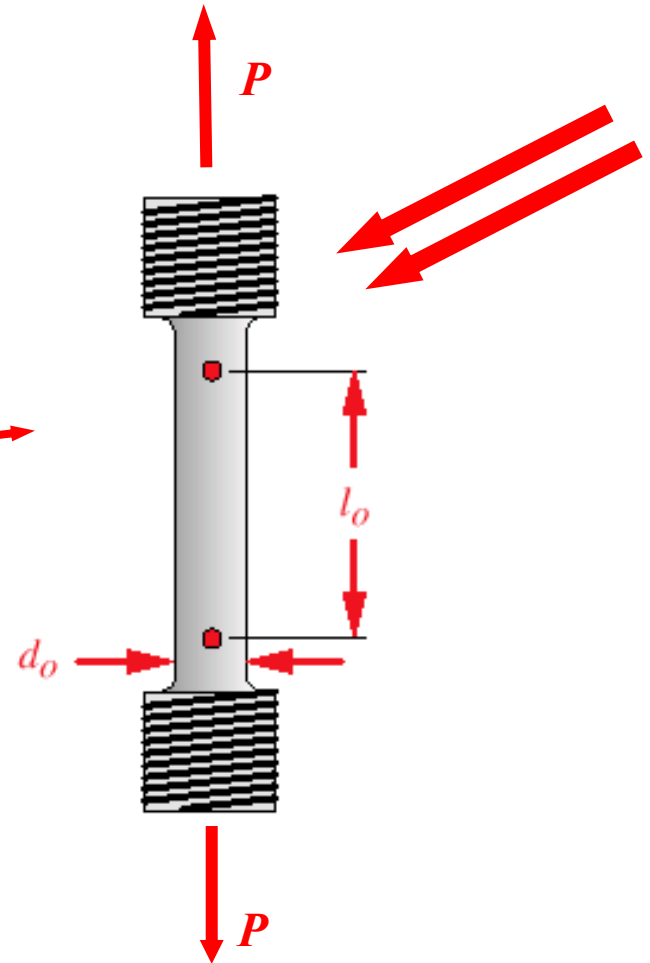
$$\tau_{zy} (\Delta x \Delta y) \cdot \Delta z = \tau_{yz} (\Delta x \Delta z) \cdot \Delta y$$

$$\text{Therefore, } \tau_{zy} = \tau_{yz}$$



Average normal stress in an axially loaded bar

Tensile test



Average normal stress in an axially loaded bar

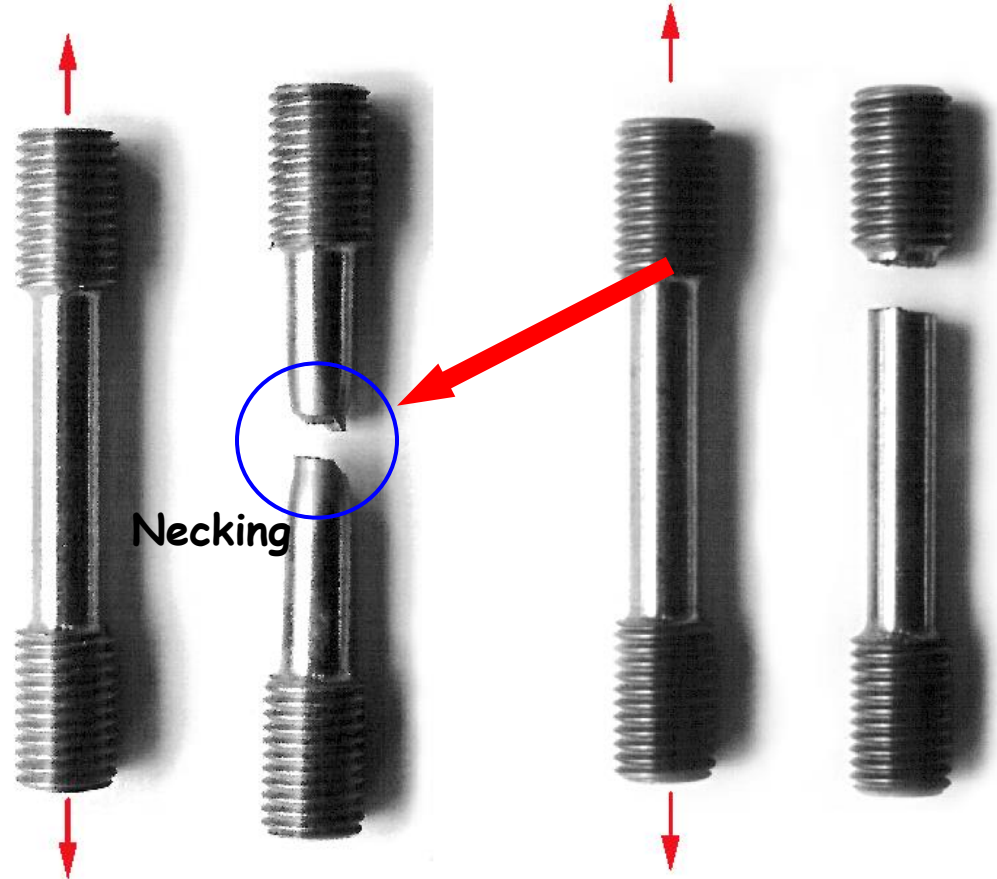
Tensile test



Typical results

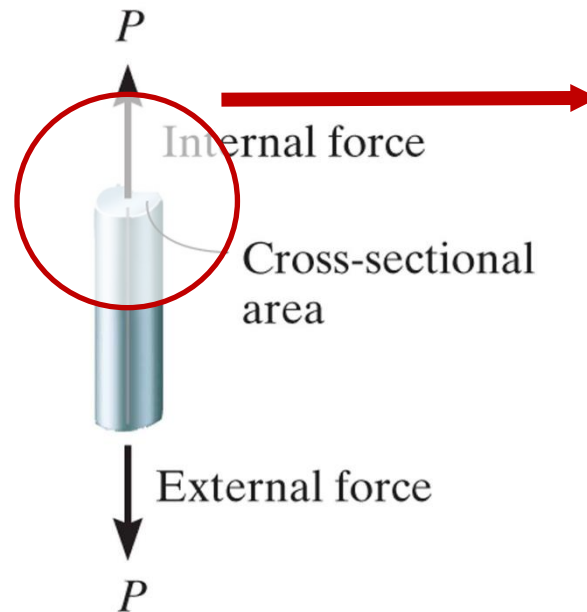
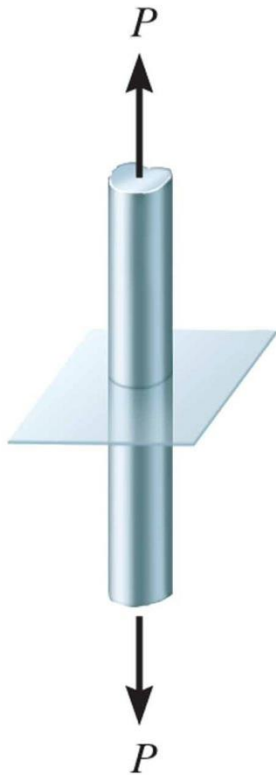
Ductile material

Brittle material

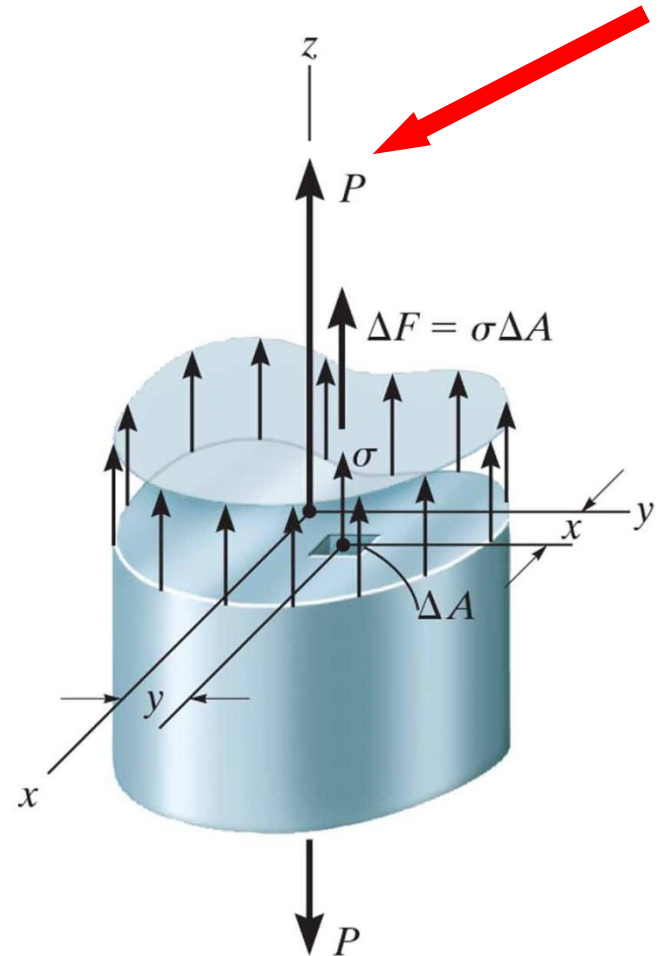


Average normal stress in an axially loaded bar

Bar subjected to axial load

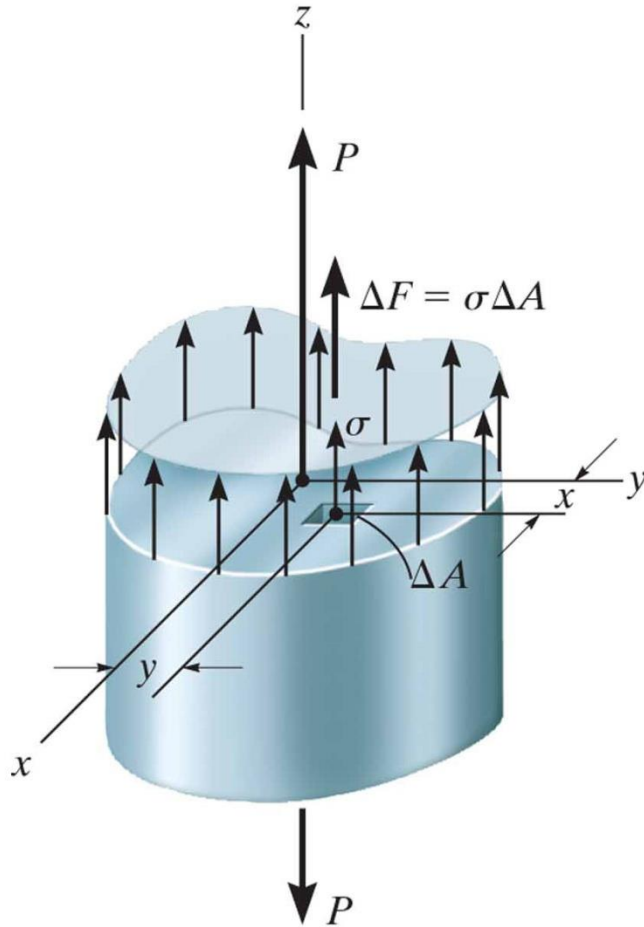


Internal distribution of forces



Average normal stress in an axially loaded bar

Internal distribution
of forces



$$+ \uparrow F_{Rz} = \sum F_z$$

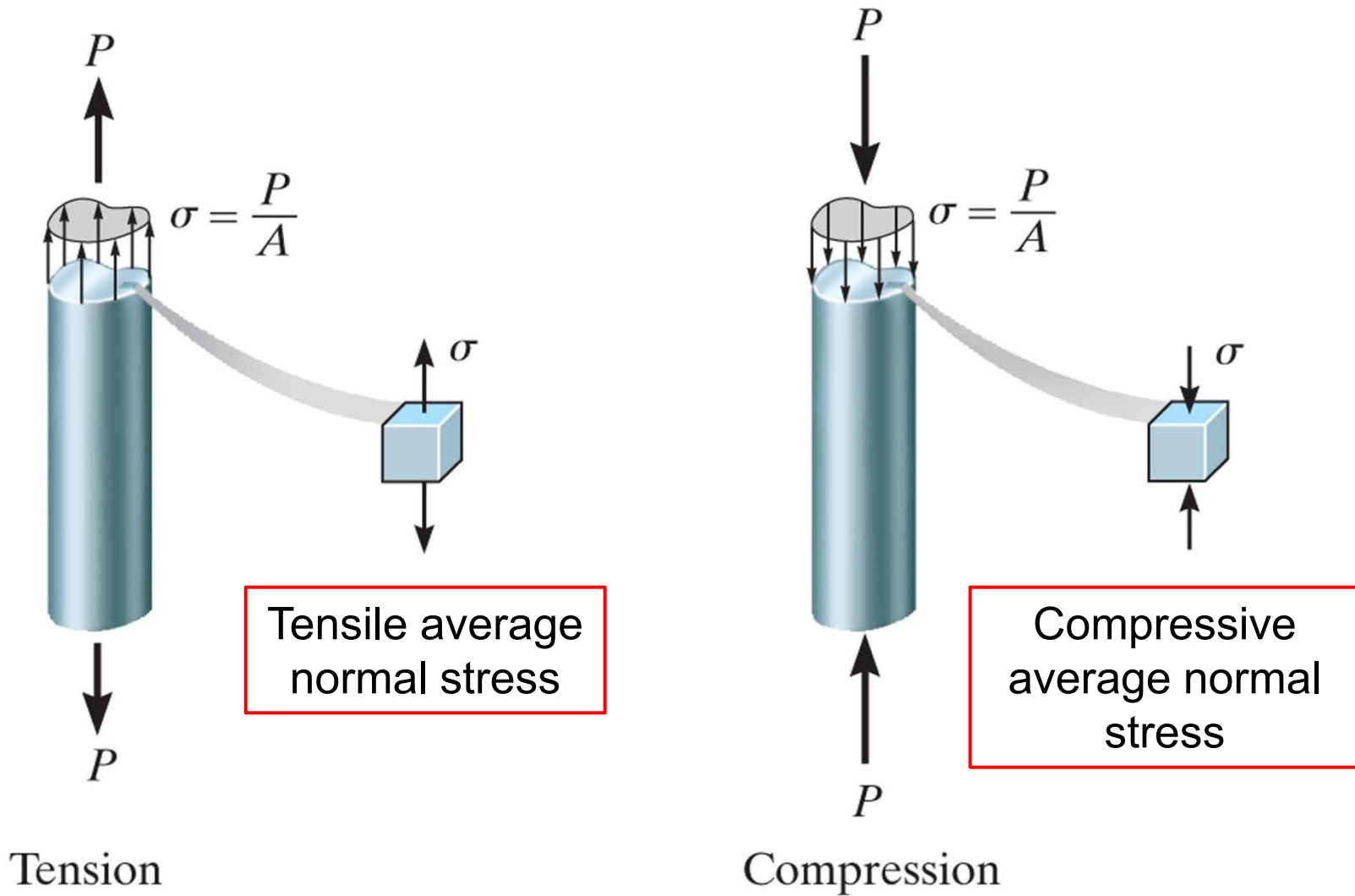
$$\int dF = \int_A \sigma dA$$
$$P = \sigma A$$

Average normal stress:

$$\sigma = \frac{P}{A}$$



Average normal stress in an axially loaded bar



Average normal stress in an axially loaded bar

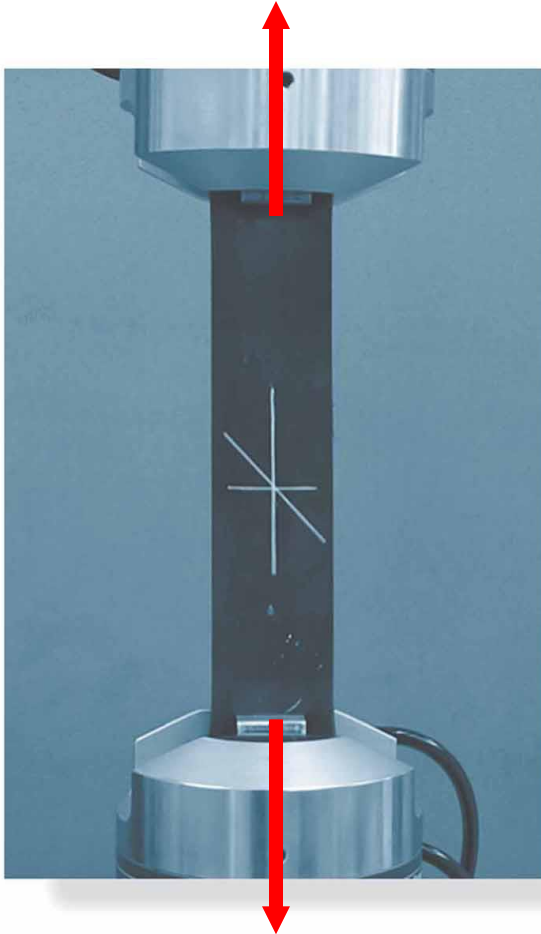


Figure: 02-01-A-UN

Note the before and after positions of three different line segments on this rubber membrane which is subjected to tension. The vertical line is lengthened, the horizontal line is shortened, and the inclined line changes its length and rotates.

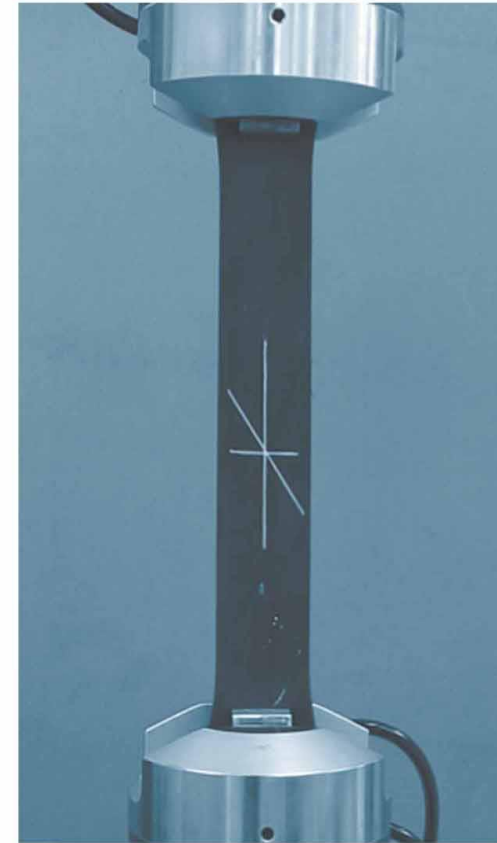


Figure: 02-01-B-UN

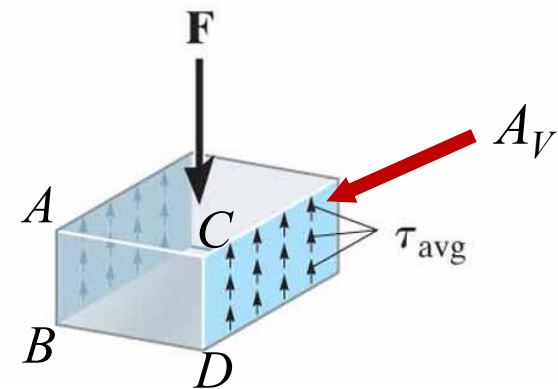
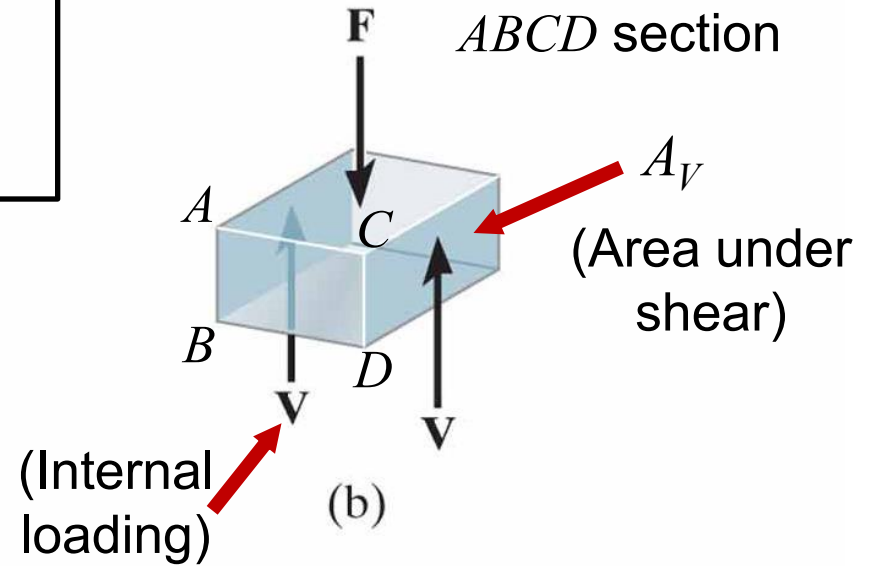
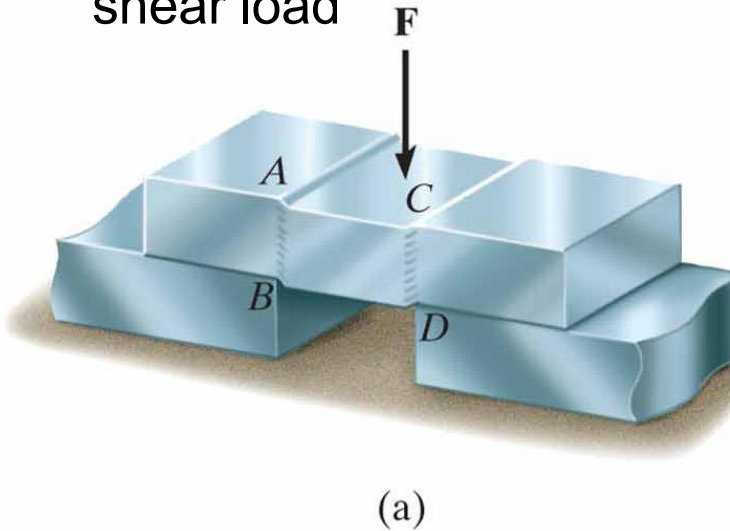
Note the before and after positions of three different line segments on this rubber membrane which is subjected to tension. The vertical line is lengthened, the horizontal line is shortened, and the inclined line changes its length and rotates.



Average direct shear stress

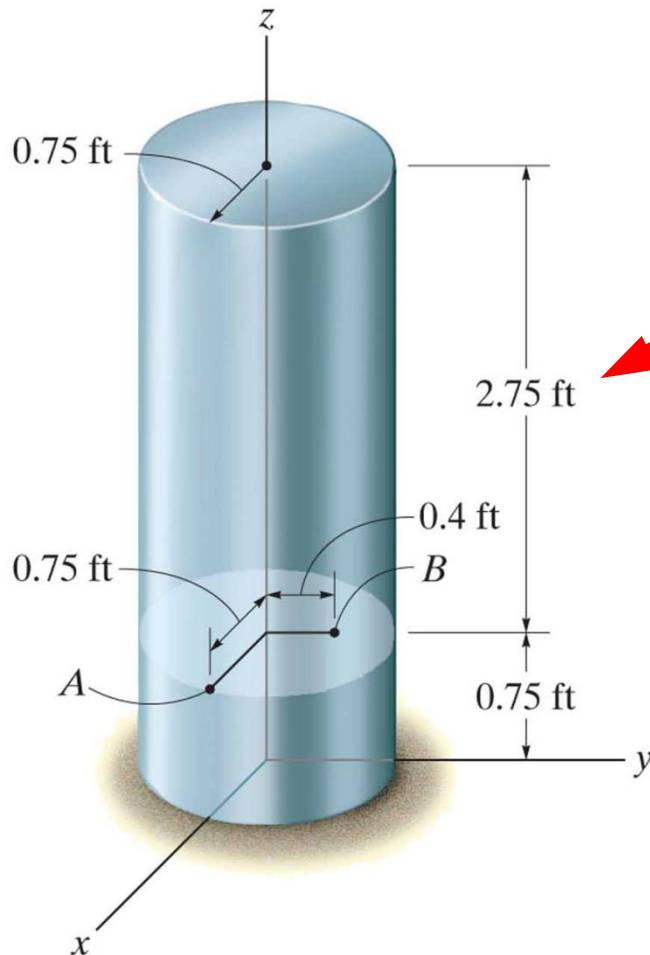
$$\tau_{avg} = \frac{V}{A_V}$$

Bar subjected to shear load



Average **normal** stress: example A

The casting shown is made of steel having a specific weight of $\gamma_{st} = 490 \text{ lb}_f/\text{ft}^3$. Determine the average compressive stress acting at points *A* and *B*.



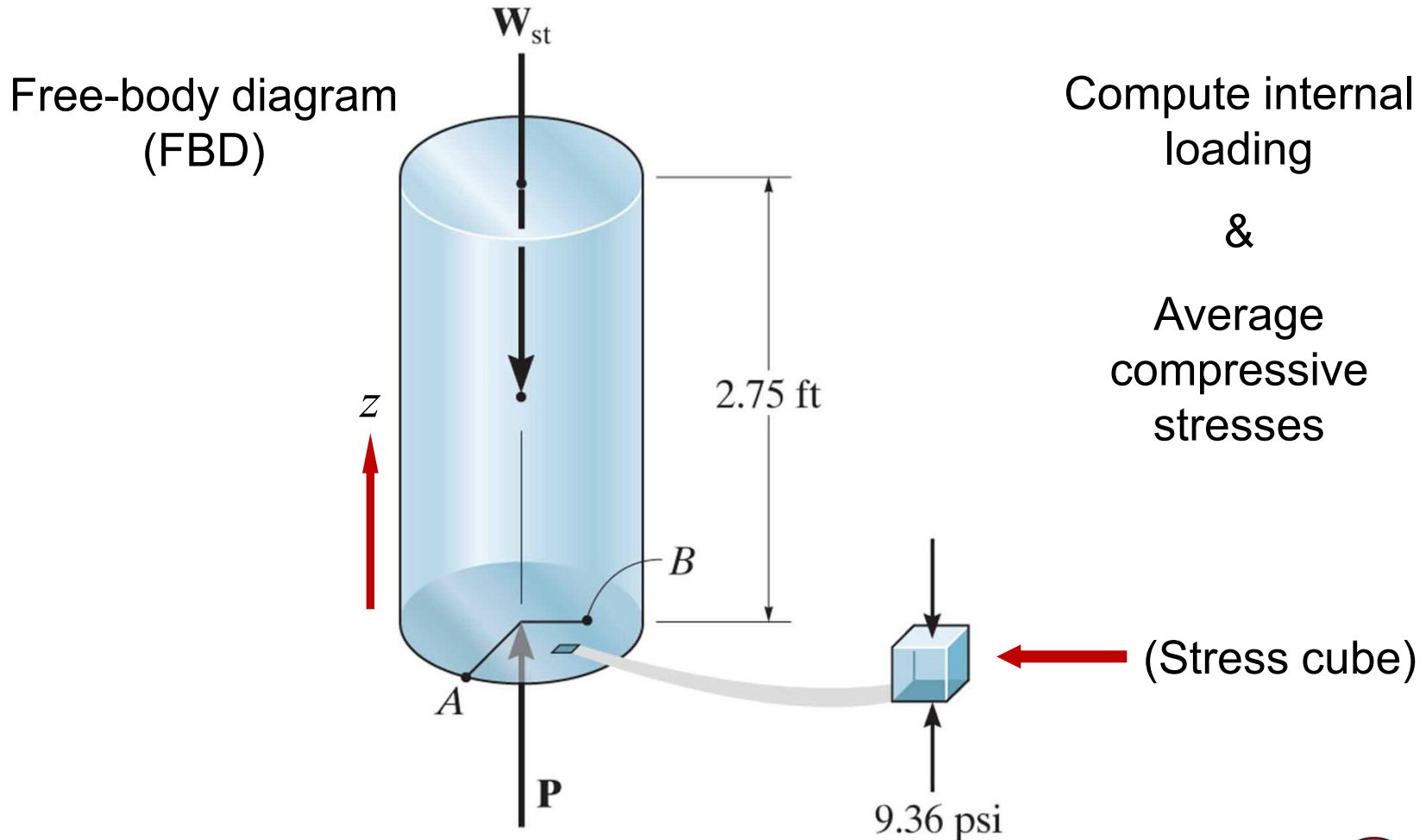
Approach:

- 1) Define free-body diagrams
- 2) Determine internal loadings
- 3) Compute average stresses



Average **normal** stress: example A

The casting shown is made of steel having a specific weight of $\gamma_{st}=490 \text{ lb}_f/\text{ft}^3$. Determine the average compressive stress acting at points *A* and *B*.

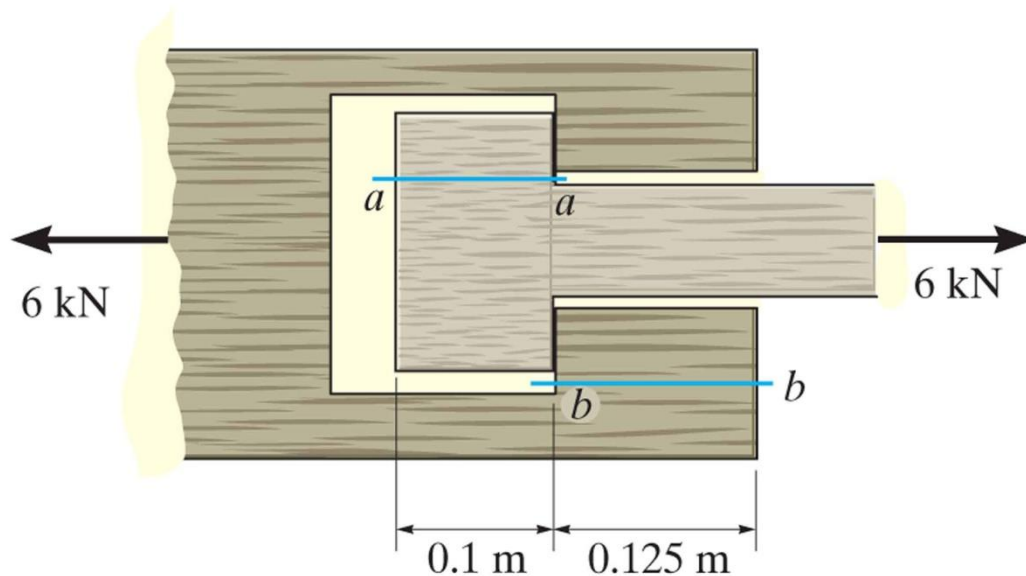


Average **shear** stress: example B

Wood joints 150 mm deep (perpendicular to the plane) are loaded as shown. Determine the average shear stress developed along planes $a-a$ and $b-b$.

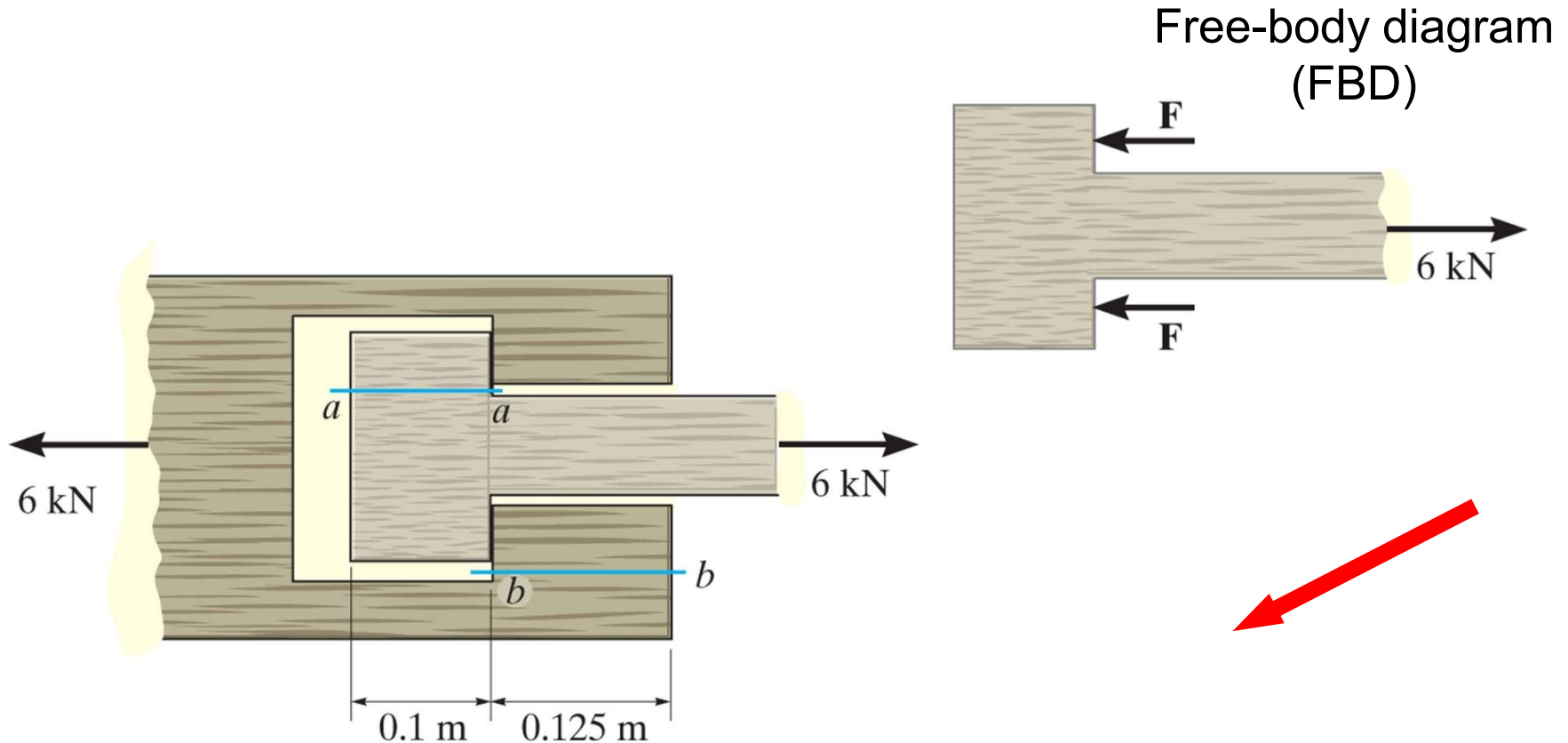
Approach:

- 1) Define free-body diagrams
- 2) Determine internal loadings
- 3) Compute average stresses



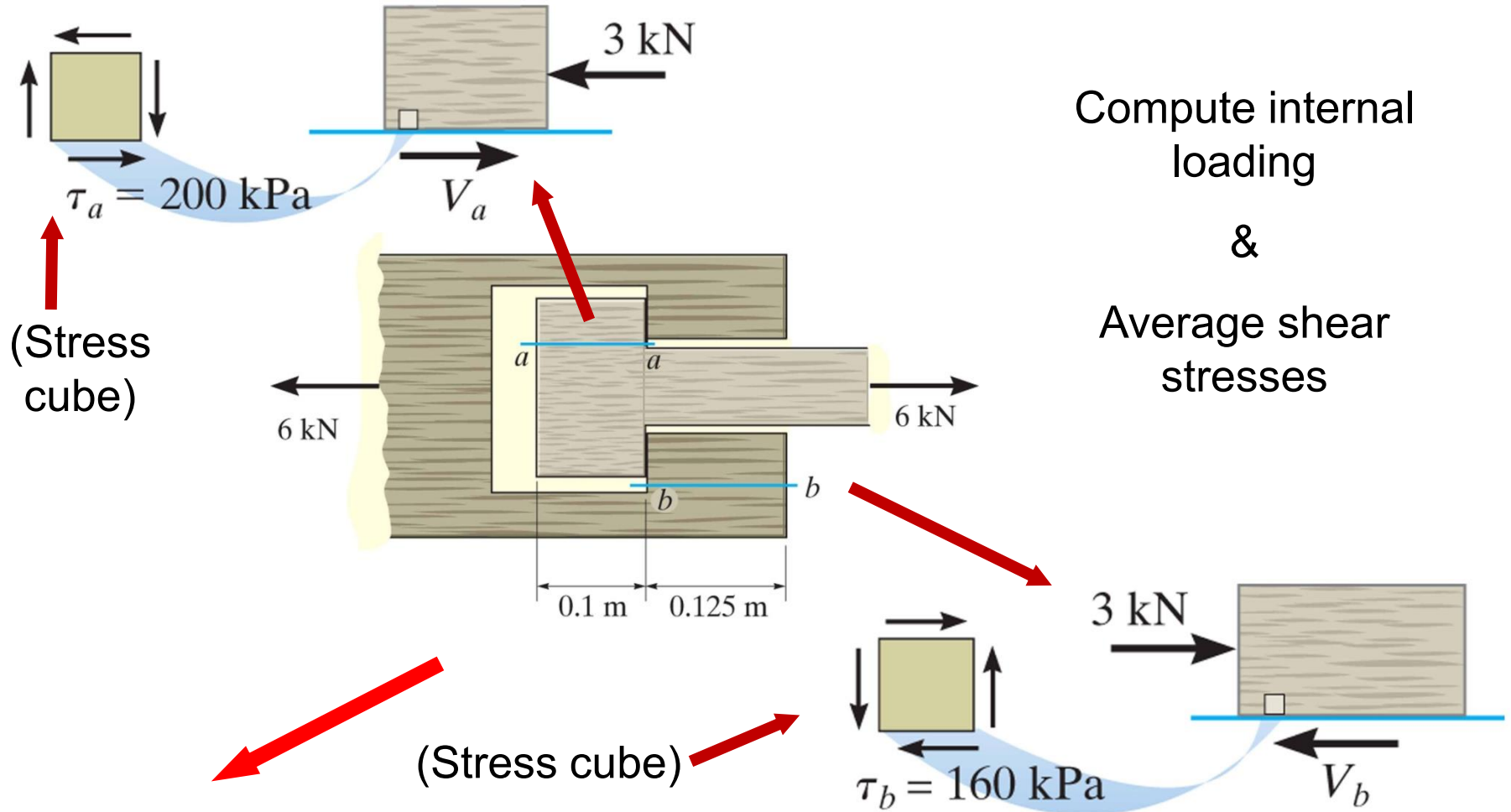
Average **shear** stress: example B

Wood joints 150 mm deep (perpendicular to the plane) are loaded as shown. Determine the average shear stress developed along planes $a-a$ and $b-b$.



Average **shear** stress: example B

Wood joints 150 mm deep (perpendicular to the plane) are loaded as shown. Determine the average shear stress developed along planes $a-a$ and $b-b$.



Reading assignment

- Chapter 1 of textbook
- Review notes and text: ES2001, ES2501



Homework assignment

- As indicated on webpage of our course

