## MA 2051 Calculus Review Sampler

Questions like these arise throughout MA 2051. Your calculus skills must be sharp enough to answer them quickly and accurately.

- 1. Let  $y(t) = 7 \cos 3\pi t$ ; t is time in seconds.
  - (a) Sketch a graph of y.
  - (b) What is the maximum value of y? At which time(s) is the maximum achieved?
  - (c) What is the period of y? How many times does y repeat itself each second?
  - (d) Calculate y''. Then show that y is a solution of the differential equation  $y'' + 9\pi^2 y = 0$ . Repeat the process to show that  $Y(t) = A \cos 3\pi t$  solves the same DE for *any* value of the constant A.
  - (e) Answer the same questions for  $z(t) = 7 \sin 3\pi t$ .
- 2. Find the antiderivative. Differentiate to verify your result.

(a) 
$$\int \frac{du}{u}$$
  
(b)  $\int e^{u} du$   
(c)  $\int \frac{dx}{1+4x}$   
(d)  $\int e^{3t-1} dt$   
(e)  $\int te^{3t^{2}-1} dt$   
(f)  $\int \frac{dv}{(1-v)^{2}}$   
(g)  $\int \frac{dv}{g+kv/m}$ , where  $g, k, m$  are constants

- 3. Solve for C:  $e^{kt+C_1} = Ce^{kt}$ .
- 4. Solve for y:  $\ln |y| = kt + C$ .
- 5. Solve for v:  $\ln |g + kv/m| = kt/m + C$ .
- 6. Find value(s) of the constant r that make  $e^{rt}$  a solution of y'' + y' 2y = 0.